

***Source term estimation using
an adjoint model:
a comparison of two different algorithms***

***Gianni Tinarelli¹, Giuseppe Carlino² and
Francesco Ubaldi¹***

¹ ARIANET S.r.l., Milan, Italy

² SIMULARIA S.r.l., Turin, Italy

Introduction – **Source Term Estimation Algorithms**

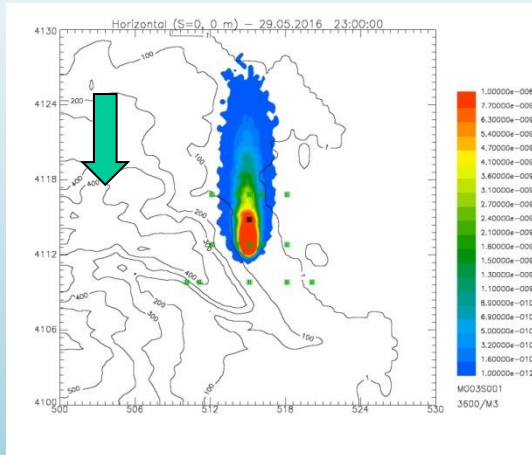
The reconstruction of unknown Source Terms of pollutants is one of the most challenging problems. The need of such a reconstruction is not so uncommon in many situations (emergency response, odor events)

A **STE** algorithm (in the worst case) given observations of pollutant concentration and meteorological information, should estimate:

- Source location
- Emission time series
- Emitted quantities

Two **STE** algorithms are tested, based on:

- The application of the adjoint Lagrangian Particle Dispersion model RetroSpray

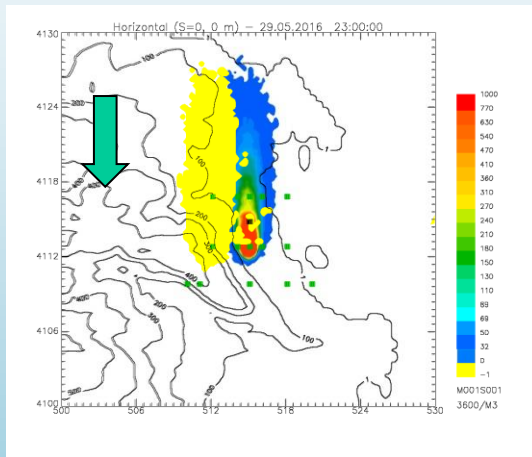


Backward trajectories starting from measuring stations identify possible emission zones and intensities
 Stations measuring zero identify exclusion zones

- different postprocessing systems
 - ✓ Simple (Maximum Overlap)
 - ✓ Complex (Variational Method)

Two **STE** algorithms are tested, based on:

- The application of the adjoint Lagrangian Particle Dispersion model RetroSpray

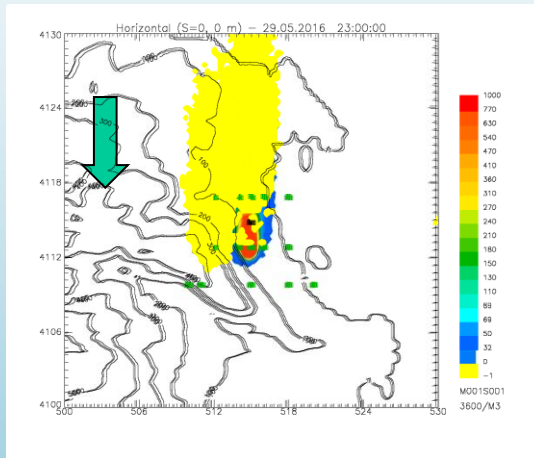


Backward trajectories starting from measuring stations identify possible emission zones and intensities
 Stations measuring zero identify exclusion zones

- different postprocessing systems
 - ✓ Simple (Maximum Overlap)
 - ✓ Complex (Variational Method)

Two **STE** algorithms are tested, based on:

- The application of the adjoint Lagrangian Particle Dispersion model RetroSpray

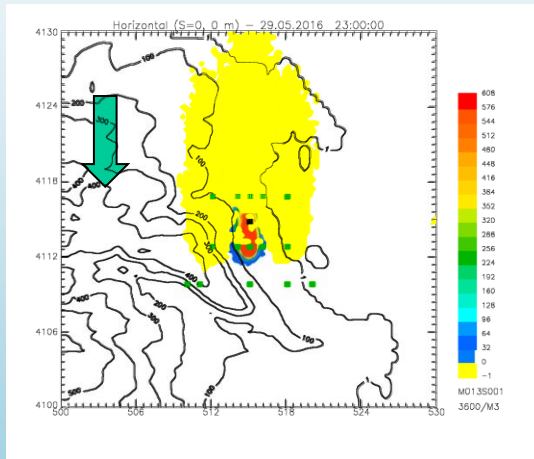


Backward trajectories starting from measuring stations identify possible emission zones and intensities
 Stations measuring zero identify exclusion zones

- different postprocessing systems
 - ✓ Simple (Maximum Overlap)
 - ✓ Complex (Variational Method)

Two **STE** algorithms are tested, based on:

- The application of the adjoint Lagrangian Particle Dispersion model RetroSpray



Backward trajectories starting from measuring stations identify possible emission zones and intensities
 Stations measuring zero identify exclusion zones

- different postprocessing systems
 - ✓ Simple (Maximum Overlap)
 - ✓ Complex (Variational Method)

Maximum Overlap vs Variational Method

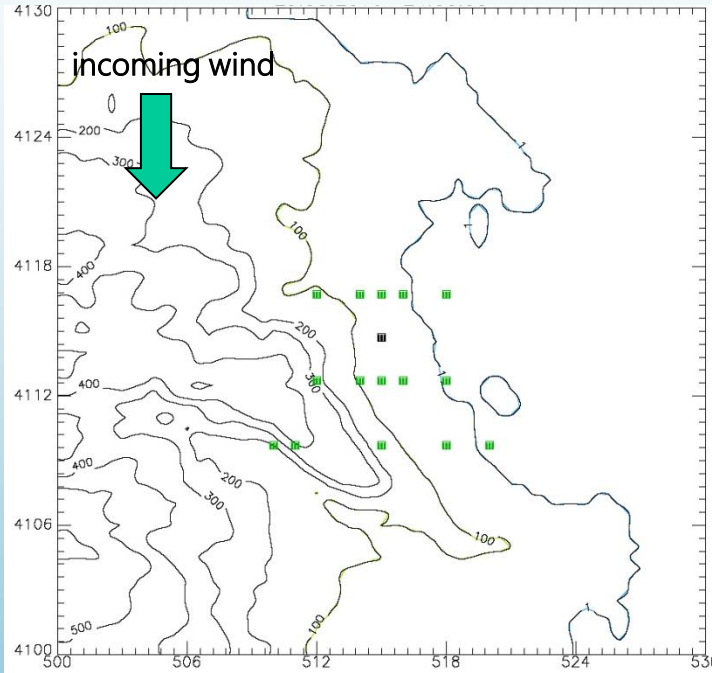
why two different systems?

- MO is conceptually simple, easy to implement and already operational
- VM is more complex to implement, but better in principle

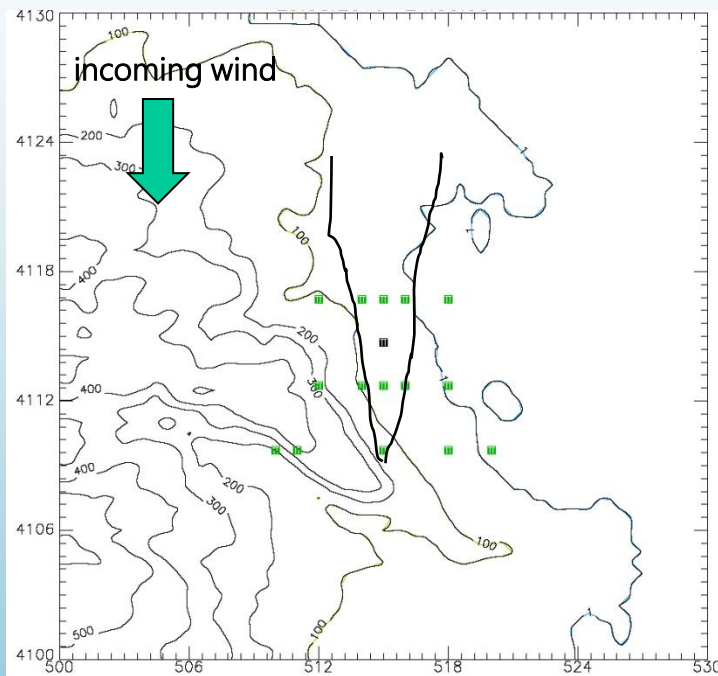
These two methods are compared in different conditions:

- data from the 'FFT07' field campaign
- synthetic cases in a real environment
- real cases

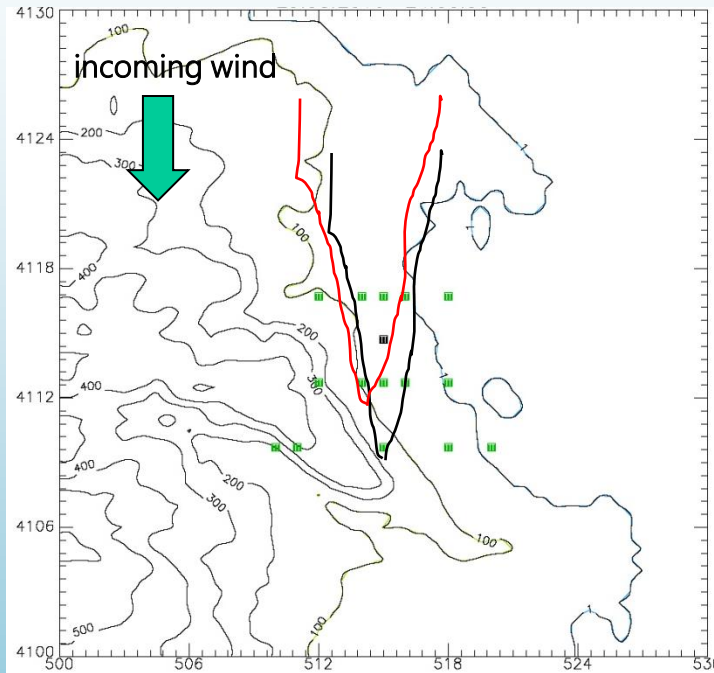
MO simply ‘counts’ at each point, during a certain time interval, the number of times that independent retroplumes coming from receptor points overlap



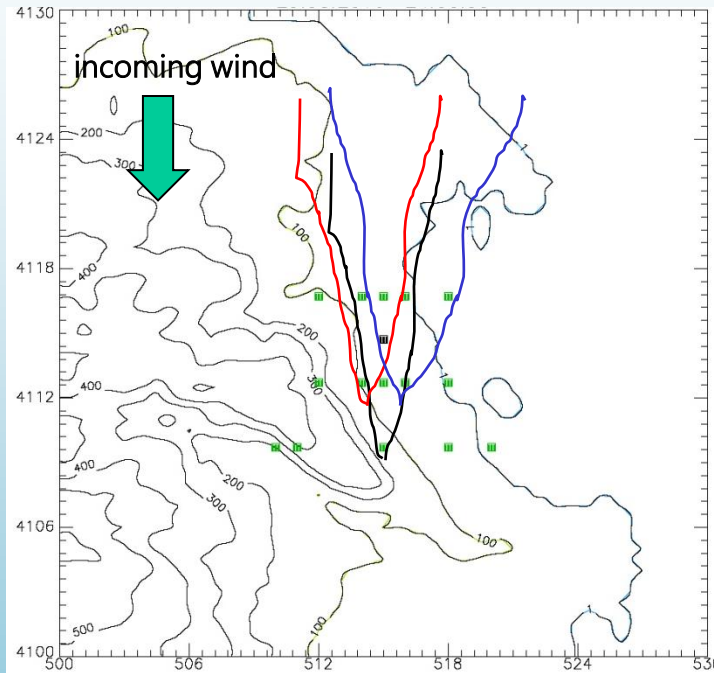
MO simply ‘counts’ at each point, during a certain time interval, the number of times that independent retroplumes coming from receptor points overlap



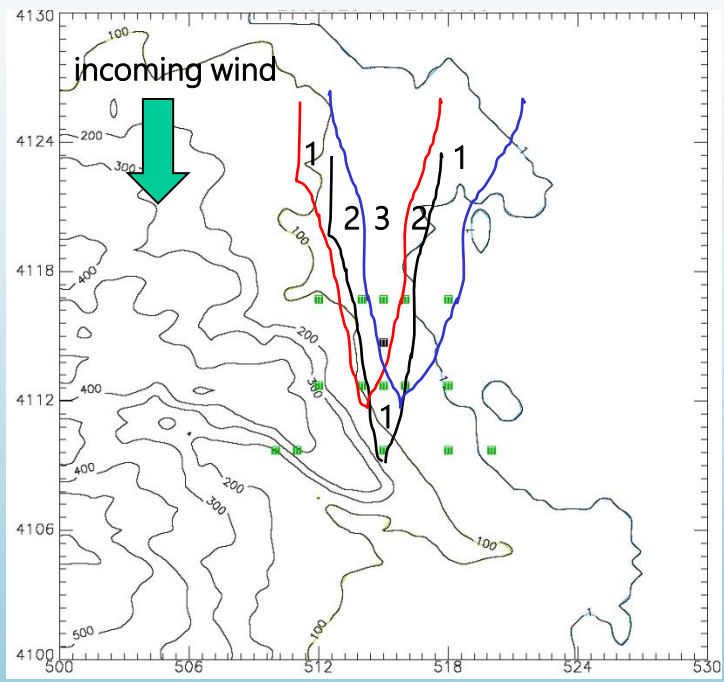
MO simply ‘counts’ at each point, during a certain time interval, the number of times that independent retroplumes coming from receptor points overlap



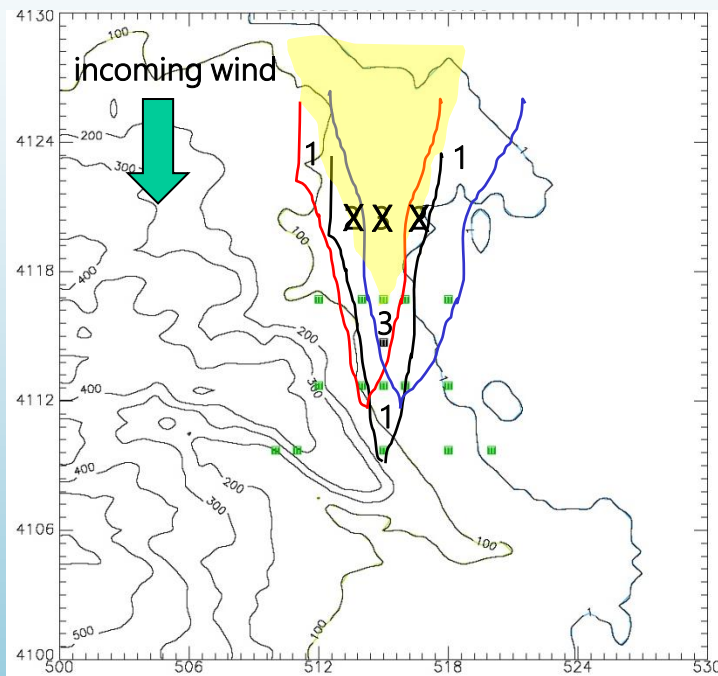
MO simply ‘counts’ at each point, during a certain time interval, the number of times that independent retroplumes coming from receptor points overlap



MO simply ‘counts’ at each point, during a certain time interval, the number of times that independent retroplumes coming from receptor points overlap

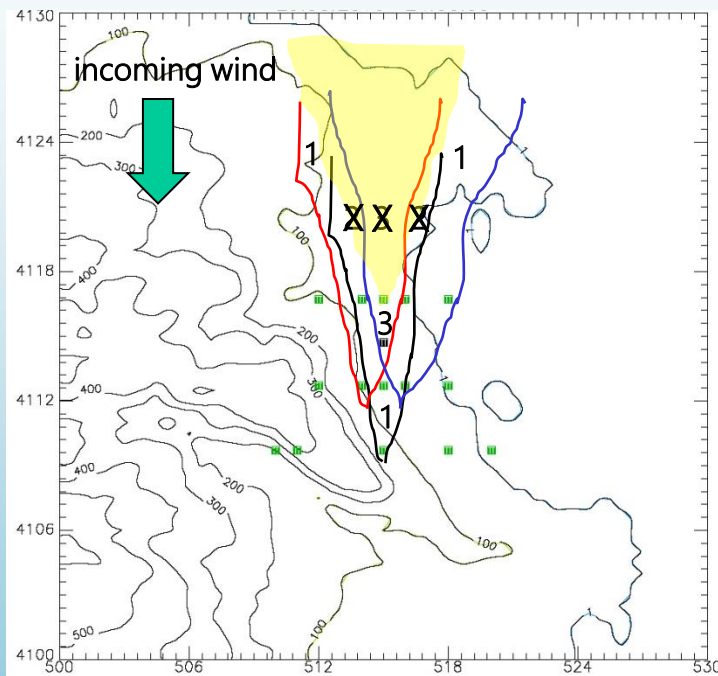


MO simply ‘counts’ at each point, during a certain time interval, the number of times that independent retroplumes coming from receptor points overlap

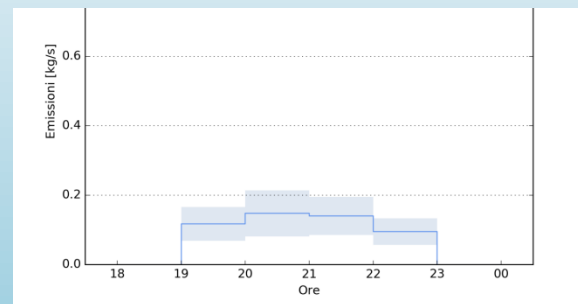


Zero observations (for example those upwind) are used to define ‘exclusion zones’ or zones that cannot include sources, zeroing the counter

MO simply ‘counts’ at each point, during a certain time interval, the number of times that independent retroplumes coming from receptor points overlap



Time by time, the emission flow computed inside the zone of maximum overlap using information from retro-plumes



Zero observations (for example those upwind) are used to define ‘exclusion zones’ or zones that cannot include sources, zeroing the counter

VM – a variational method for optimization

- A **SPRAY** forward integration defines a linear relation $\mathbf{x} = \mathbf{L} \mathbf{q}$

Where: \mathbf{q} = emissions (for example number of particles/time)

\mathbf{x} = estimated concentrations at obs times and locations

- Backward **RetroSPRAY** integration applies the **transpose** matrix \mathbf{L}^T
the Integration backward in time from obs time and locations enables the explicit computation of all \mathbf{L} matrix components
- To avoid estimating negative emissions \rightarrow transformation $\xi = \Phi(q)$, $\eta = \Phi(\mathbf{x})$

$$\phi(x) = \begin{cases} \ln(x) & x < x_{min} \\ x - 1 & x \geq x_{min} \end{cases}$$

- Estimate emissions by minimizing:

$$J(\xi) = \frac{1}{2} [\eta(\xi) - \eta^o]^T [\eta(\xi) - \eta^o] = \text{MIN}$$

...at each gridbox \rightarrow (minimized) objective function map

A comparison

FFT07 – Trial 54

Fusion Field Trial 2007 (Platt and Deriggi, 2012)

Experiments in Utah, U.S.A., 2009

Tracer (propylene) released in prescribed quantities from a source located upstream of 100 concentration detectors set in a regular array, flat orography

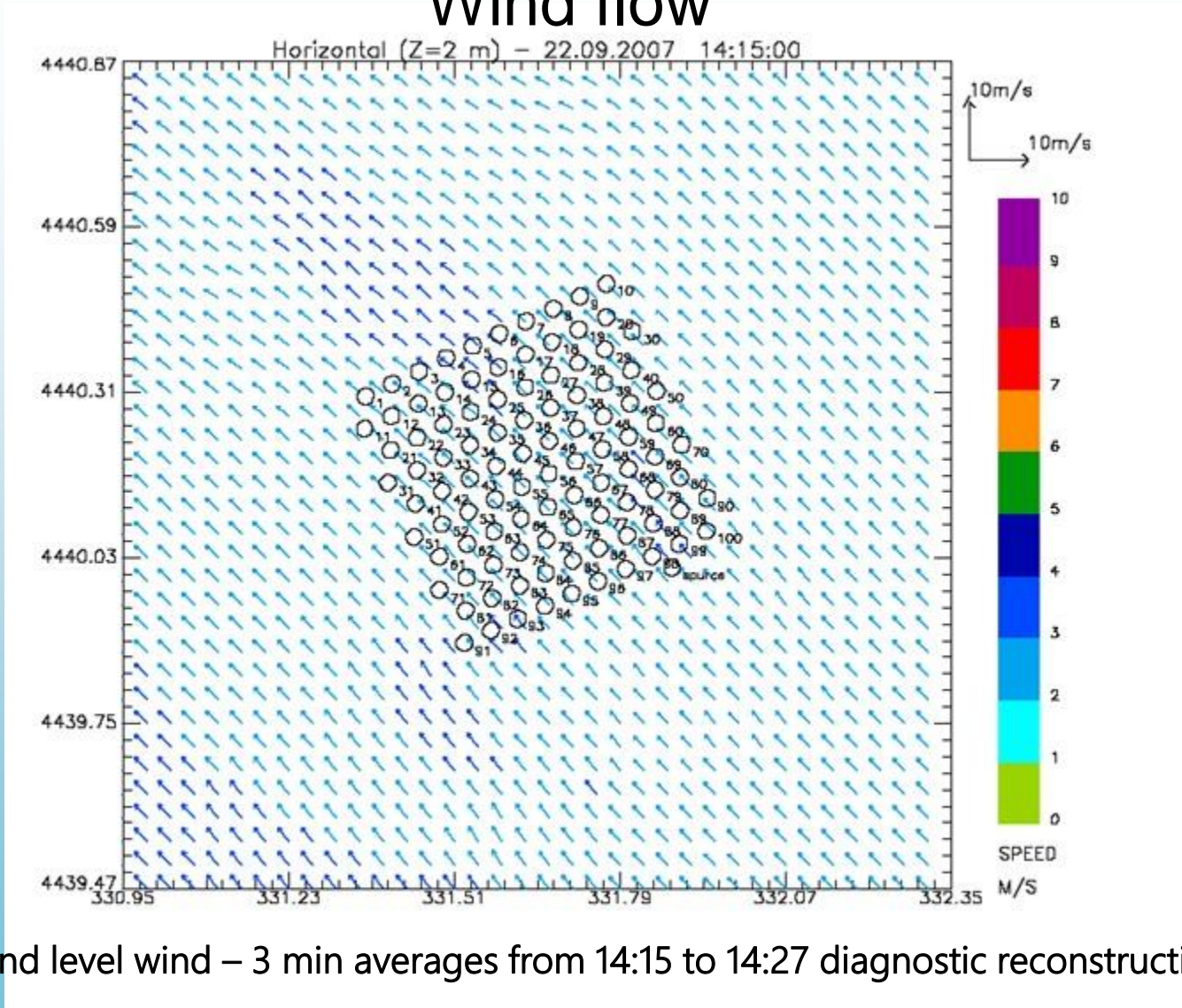
Experiment chosen Trial 54: steady wind from SE

Experiment duration: 12 minutes from 14:15 to 14:27 of 2009/09/22

Platt N., DeRiggi D (2012) Comparative investigation of Source Term Estimation algorithms using FUSION field trial 2007 data: linear regression analysis, IJEP, 48 (1-4), pp. 13-21

FFT07 – Trial 54

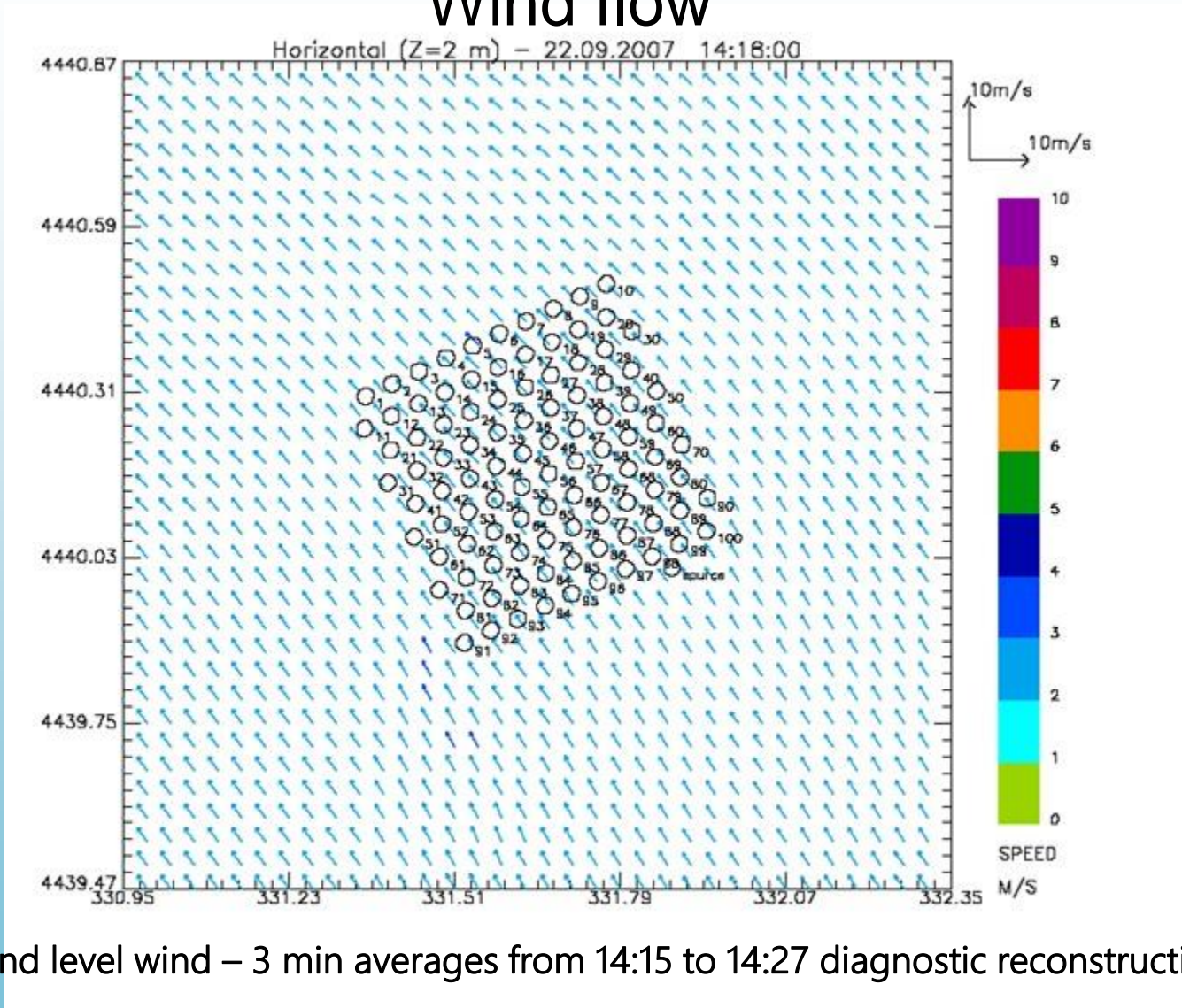
Wind flow



Ground level wind – 3 min averages from 14:15 to 14:27 diagnostic reconstruction

FFT07 – Trial 54

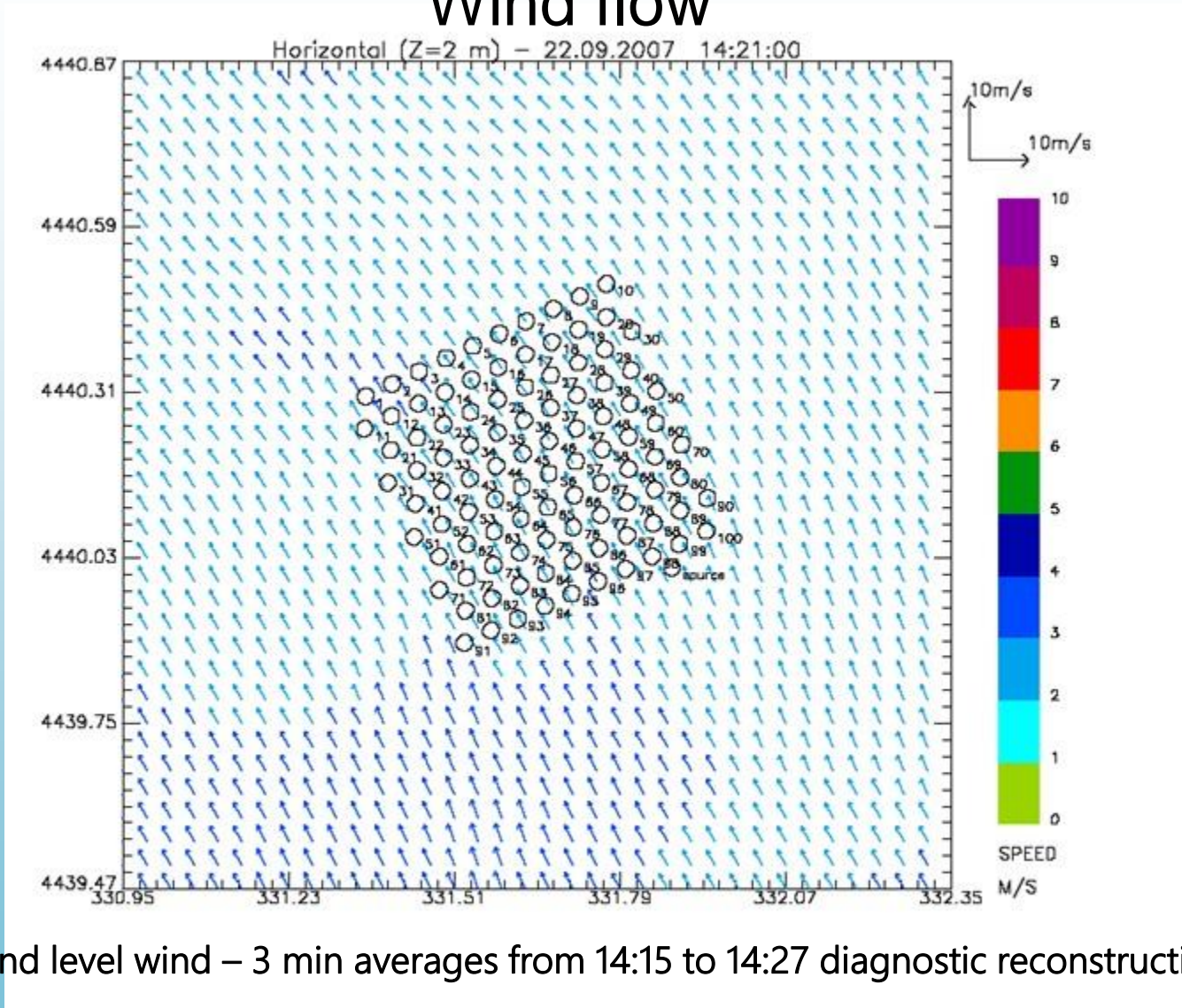
Wind flow



Ground level wind – 3 min averages from 14:15 to 14:27 diagnostic reconstruction

FFT07 – Trial 54

Wind flow

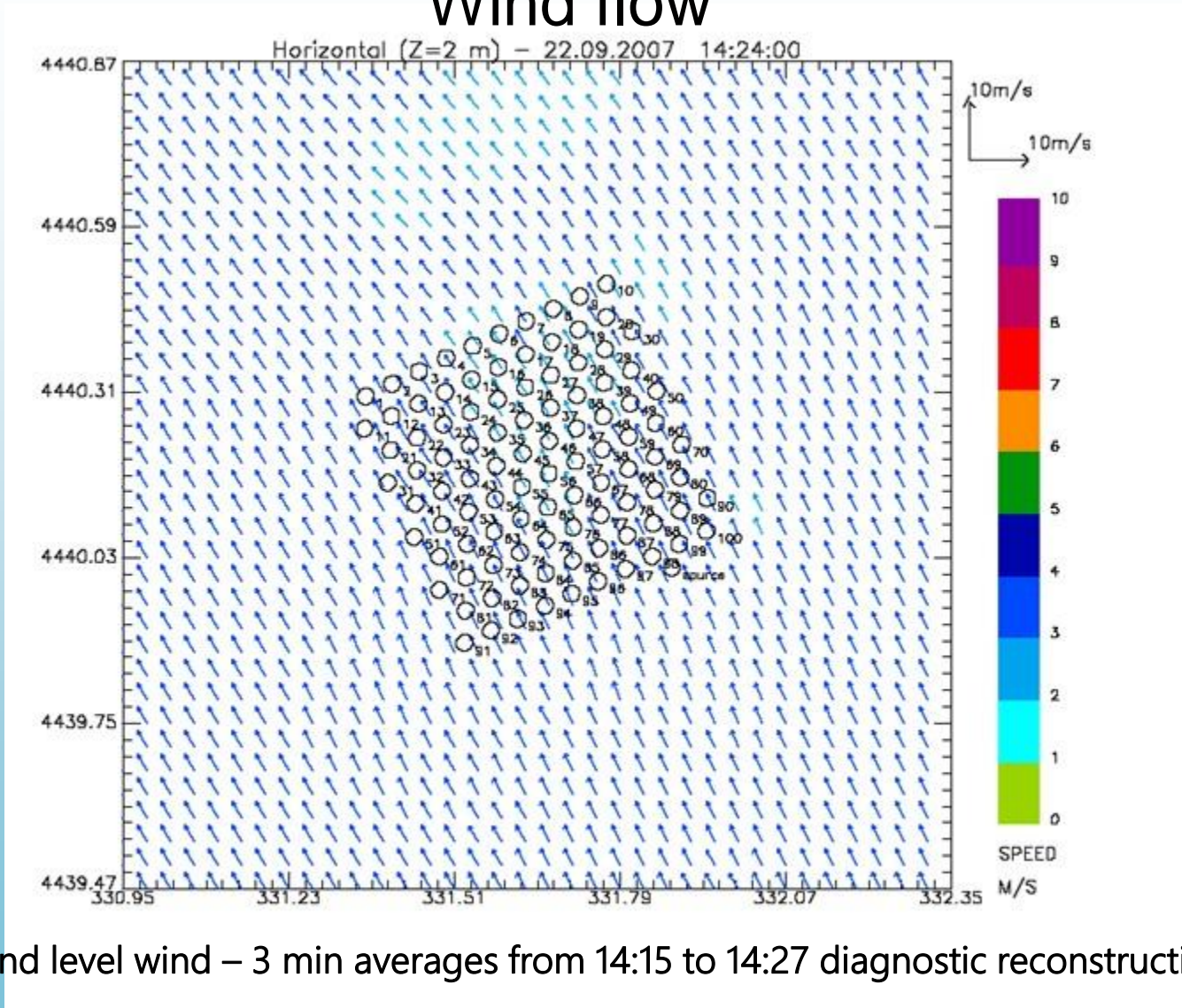


14:21

Ground level wind – 3 min averages from 14:15 to 14:27 diagnostic reconstruction

FFT07 – Trial 54

Wind flow

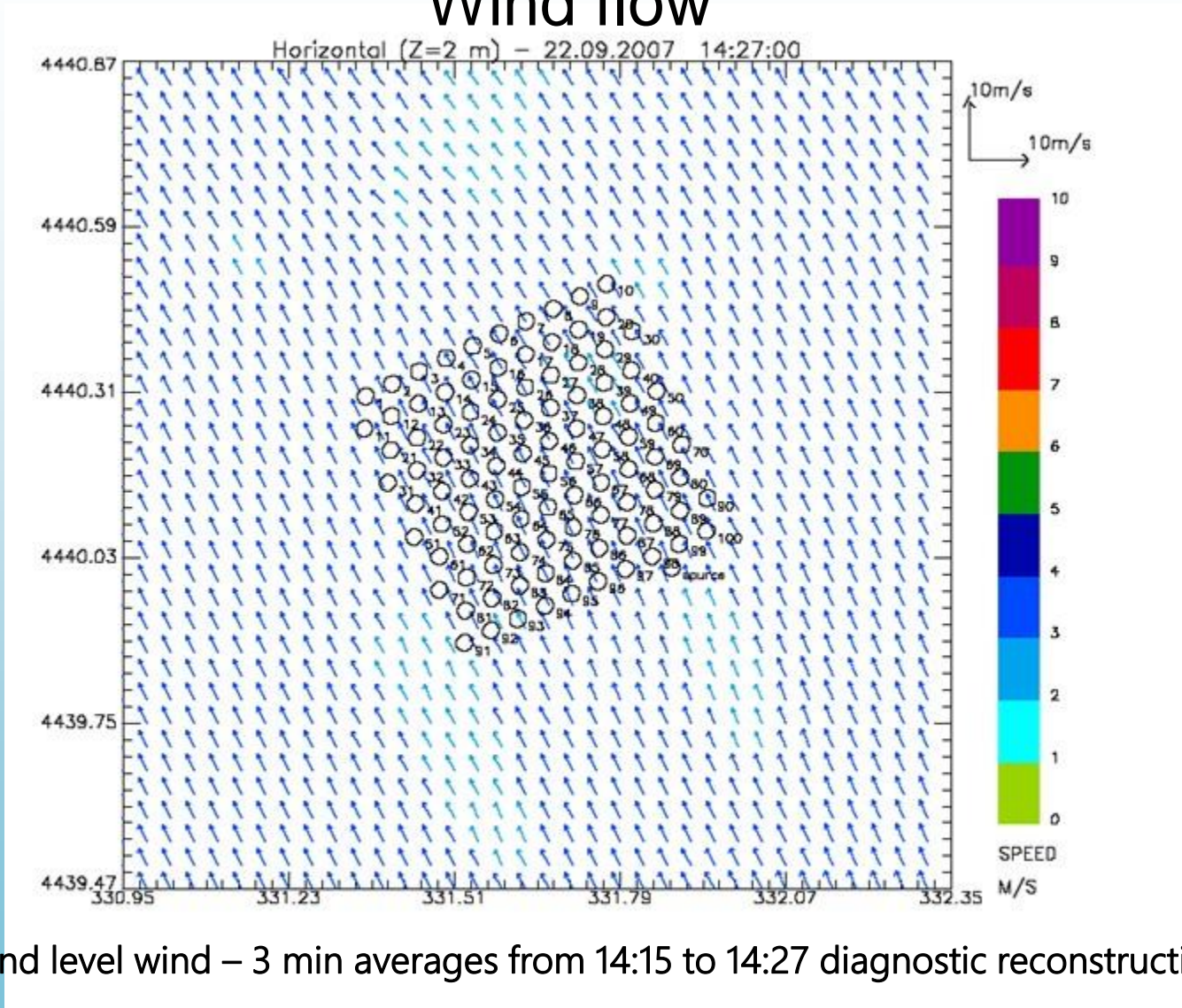


14:24

Ground level wind – 3 min averages from 14:15 to 14:27 diagnostic reconstruction

FFT07 – Trial 54

Wind flow

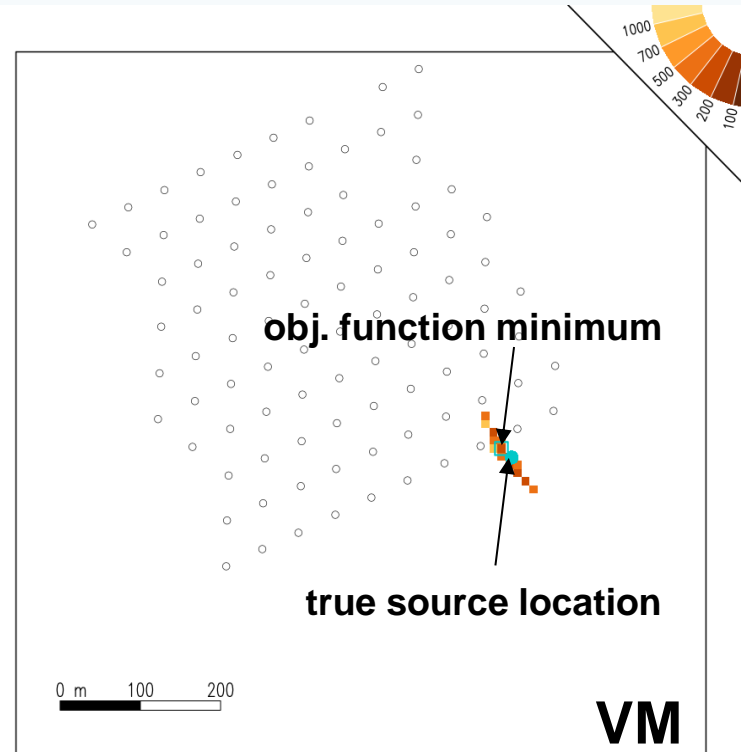
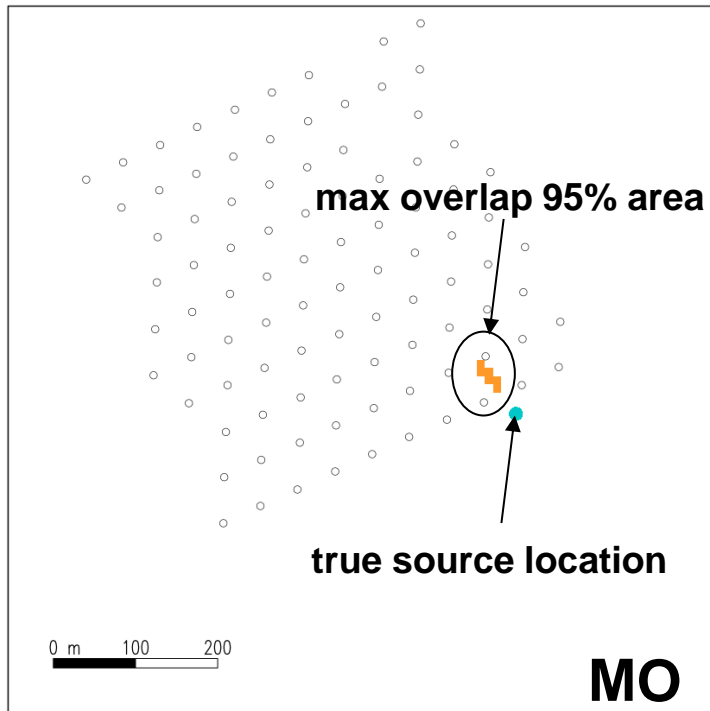


14:27

Ground level wind – 3 min averages from 14:15 to 14:27 diagnostic reconstruction

FFT07 – Trial 54

Source position - estimation

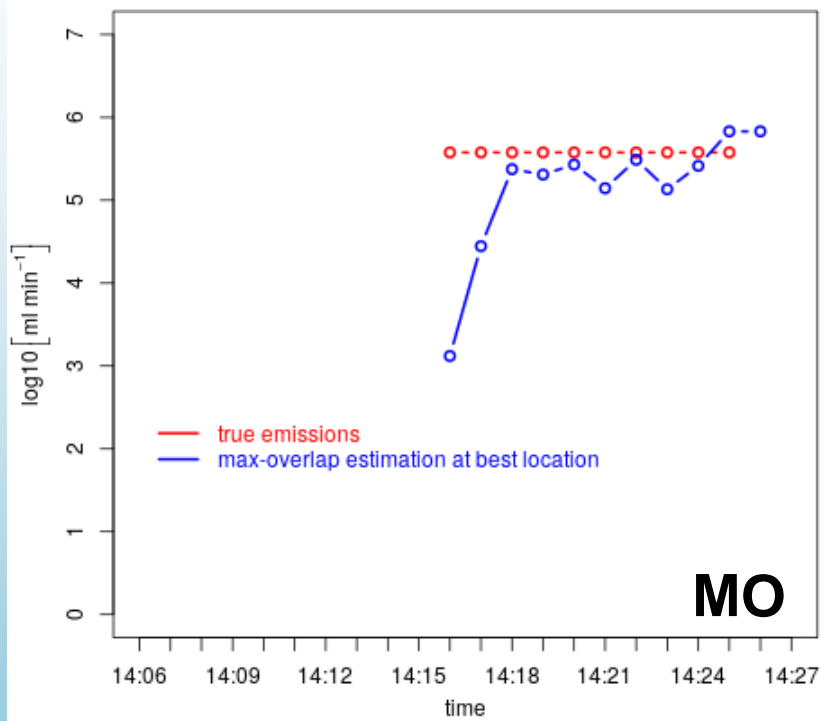


Plot of the objective function

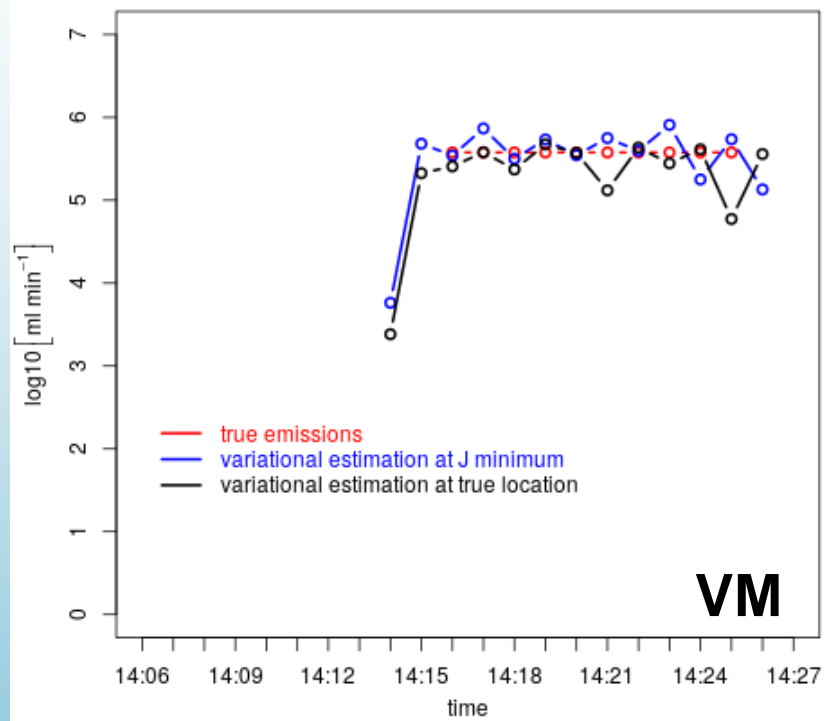
FFT07 – Trial 54

Emission flow estimation

T54 2007-09-22 - 100 stations - log10 of emissions



T54 2007-09-22 - 100 stations - log10 of emissions



Cumulated emissions:

MO estimation at best location: 2.940×10^6 ml

Cumulated emissions:

VM estimation at true location: 3.606×10^6 ml

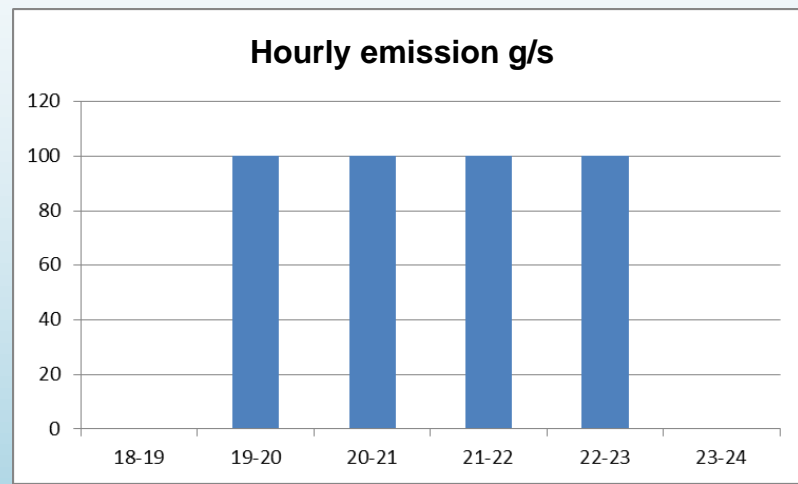
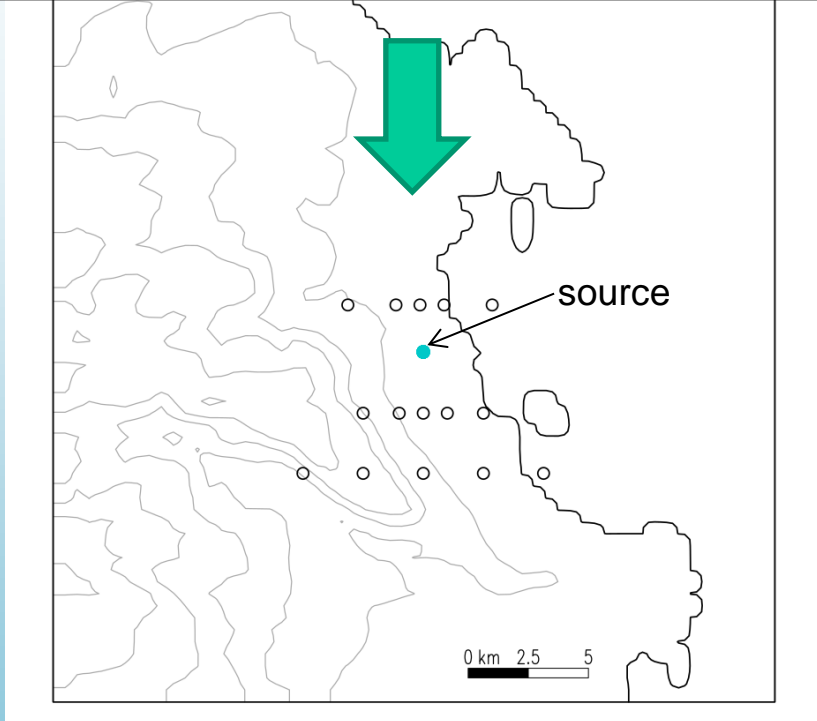
VM estimation in minimum of J: 5.405×10^6 ml

True emissions at true source: 3.775×10^6 ml

Synthetic case 1

Real domain 30x30 km² coastal industrial site, complex terrain

Stationary flow from North (19:00 – 24:00) 2 m/s



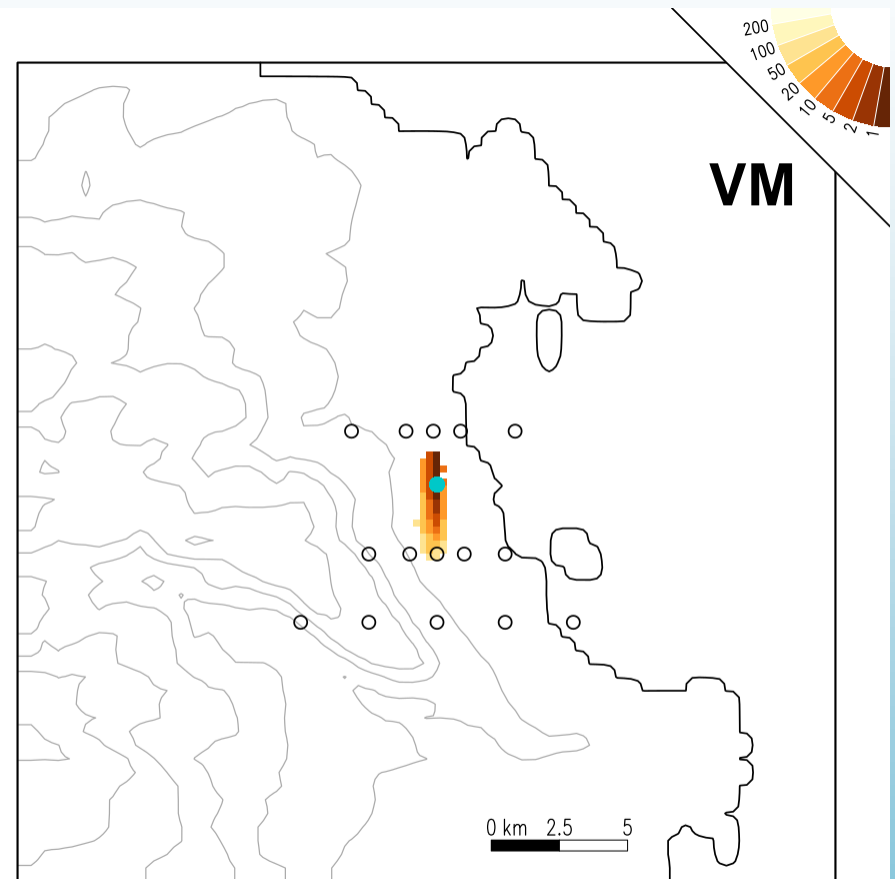
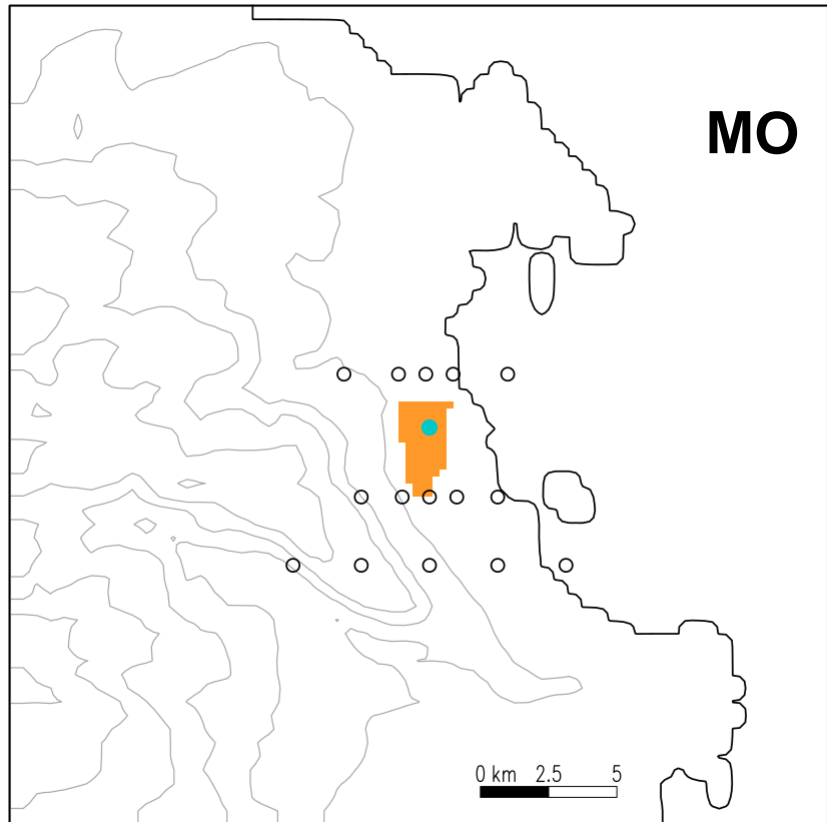
Stationary emission flow
100 g/s from 19:00 – 23:00

- 5 upwind samplers
- 5 downwind samplers 2 km to the source
- 5 downwind samplers 4 km to the source

Use of forward Spray to build concentrations at pseudo-samplers

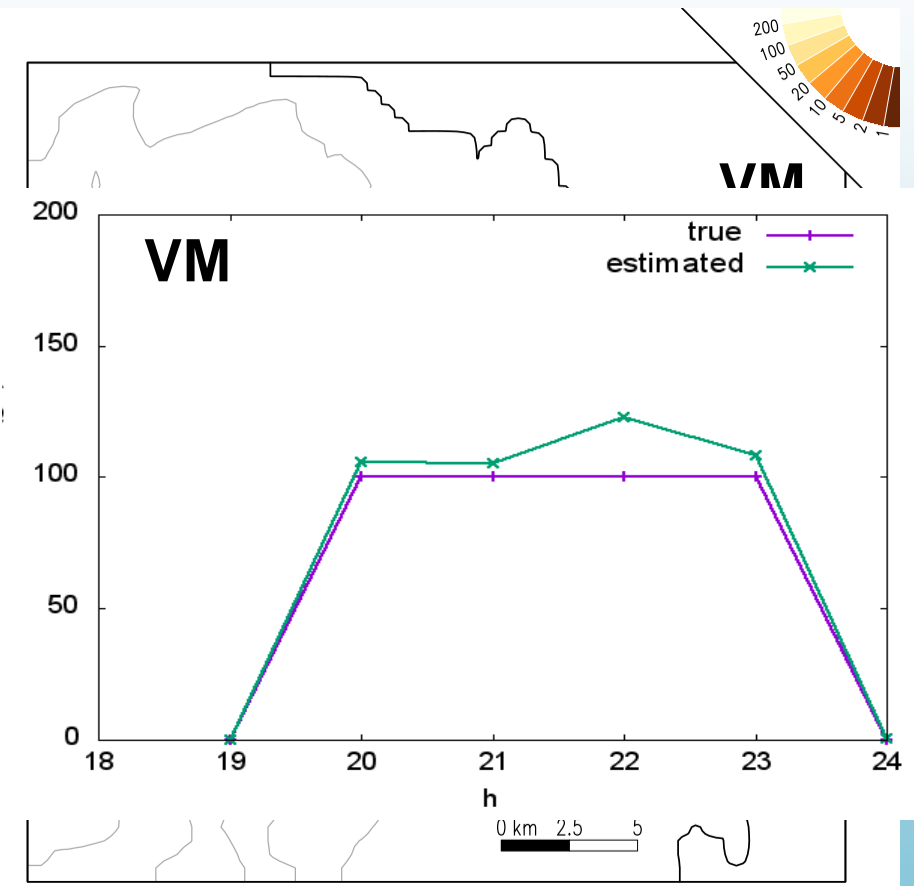
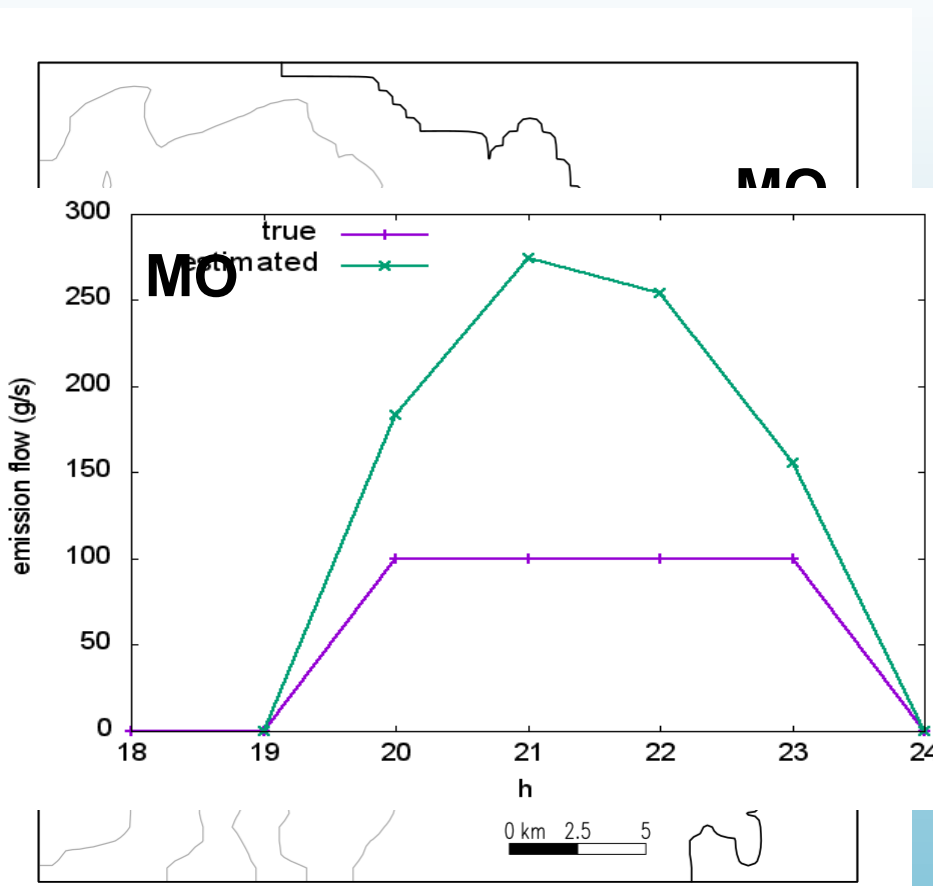
Synthetic case 1

Source position - estimation



Synthetic case 1

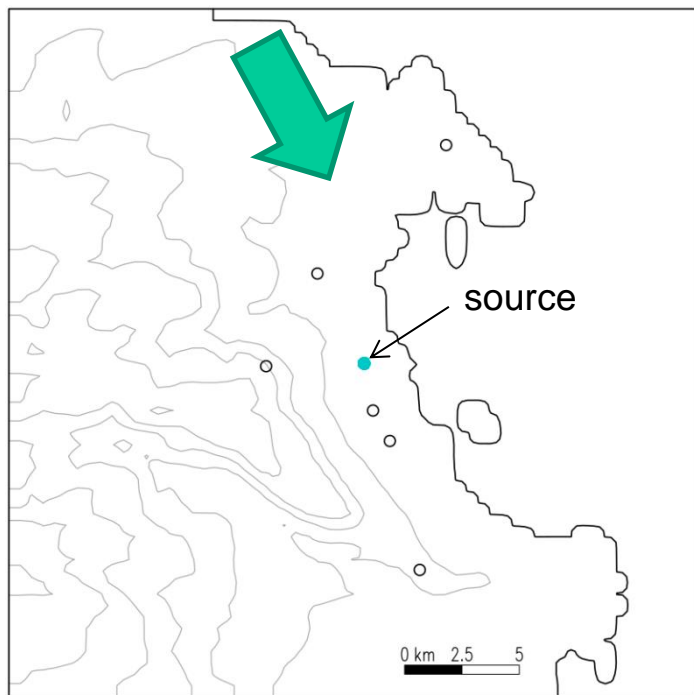
Emission flow



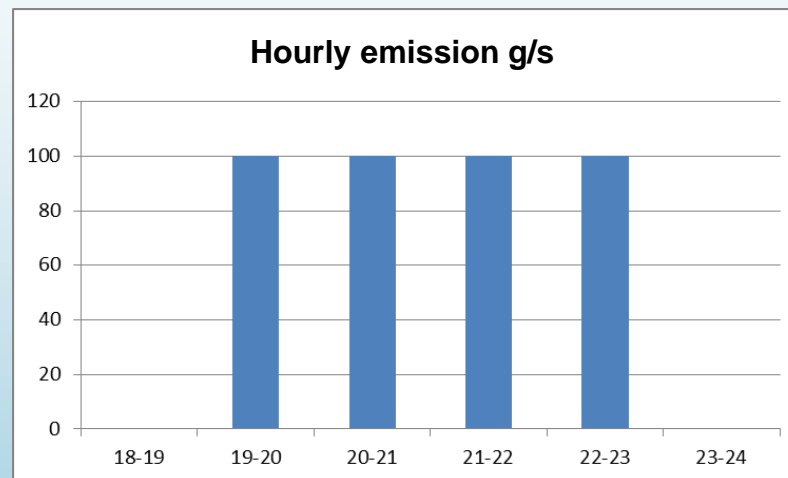
Synthetic case 2

Same domain as in case 1, but samplers as in the local existing network and realistic wind direction

Stationary flow from NW (19:00 – 24:00)



6 sparse samplers, mainly along the coast

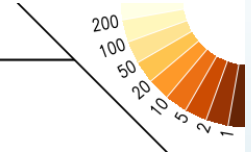
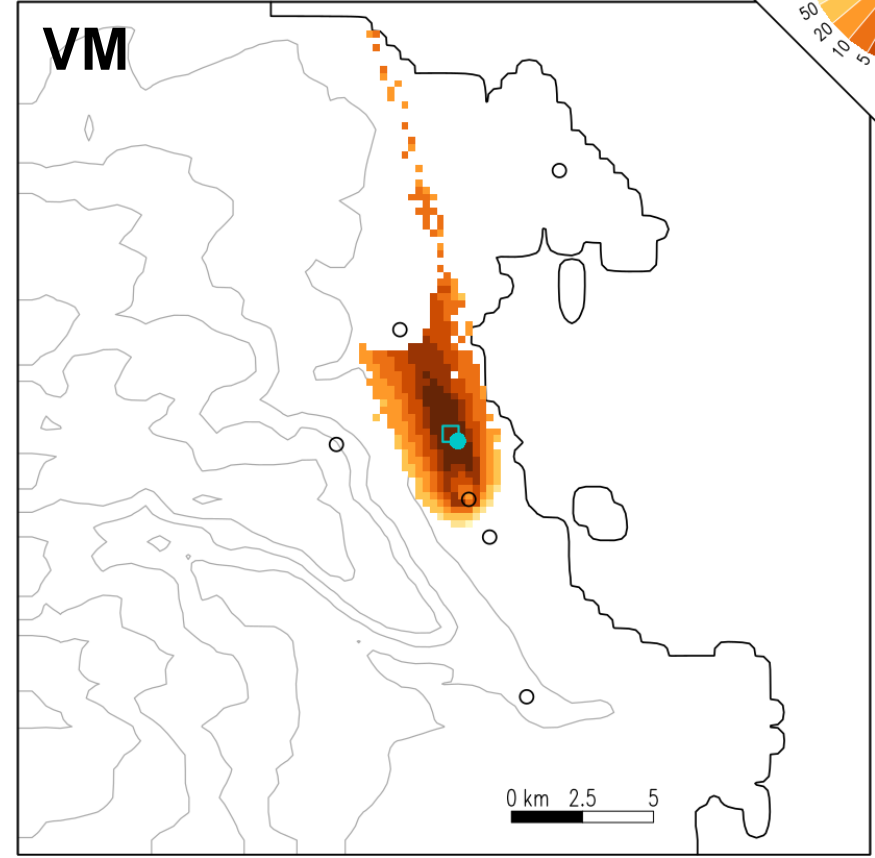
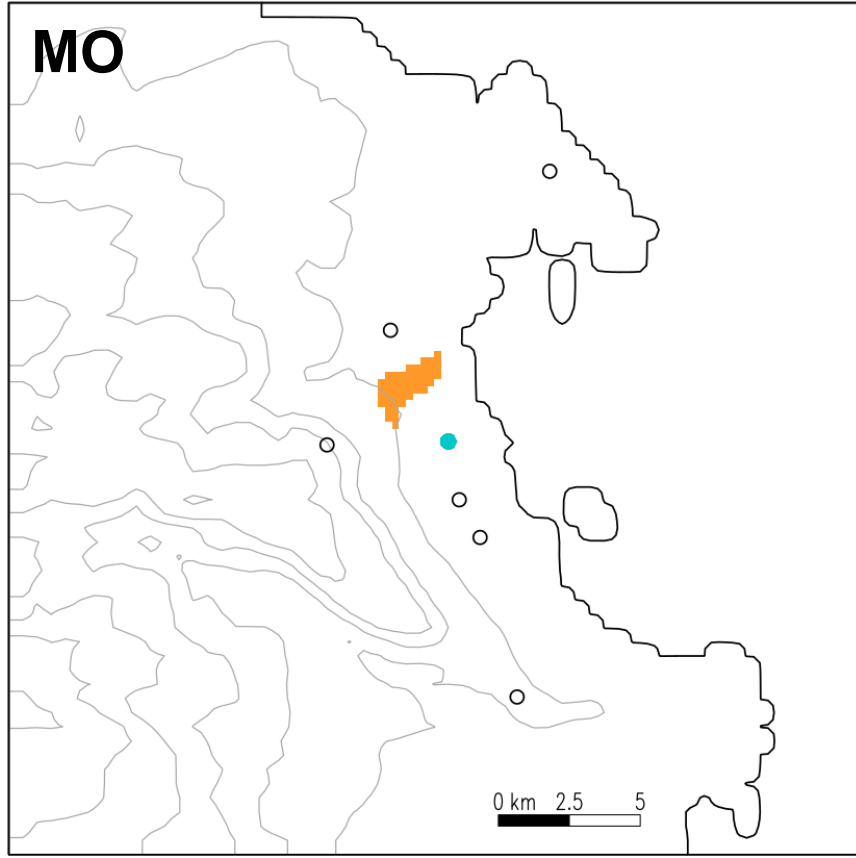


Stationary emission flow
100 g/s from 19:00 – 23:00

Use of forward Spray to build concentrations at pseudo-samplers

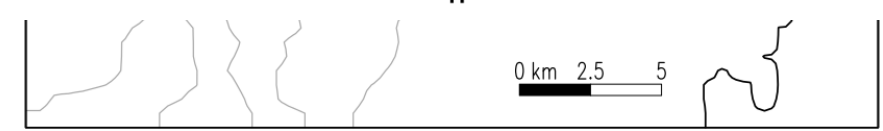
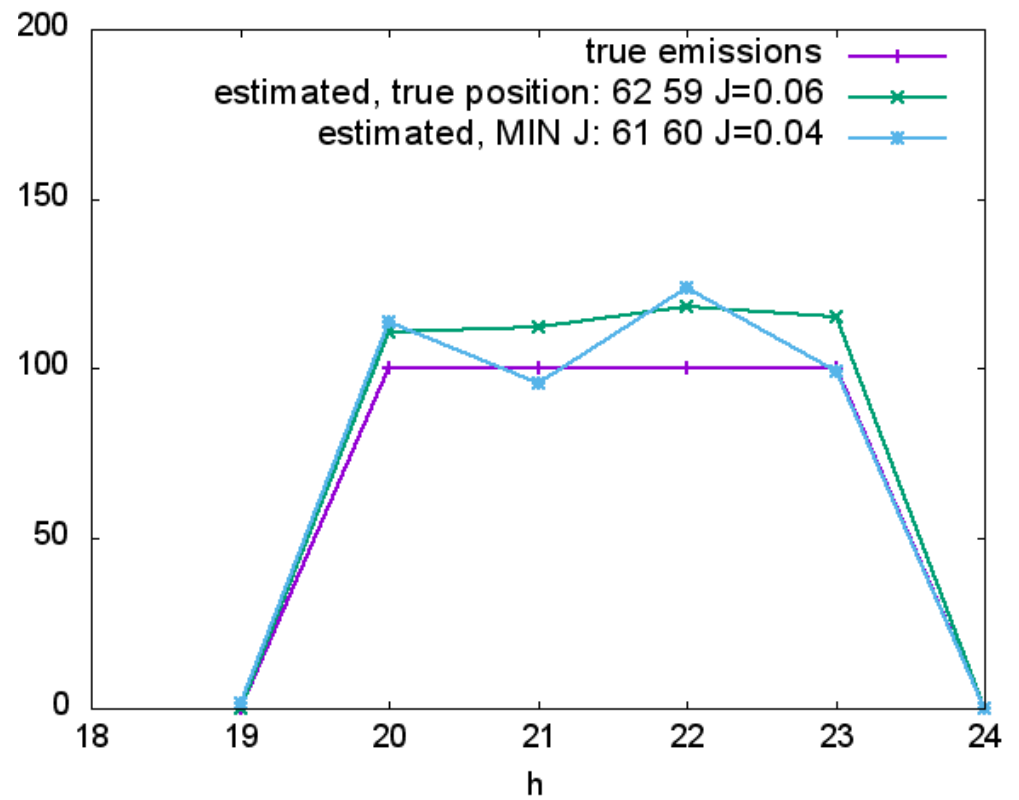
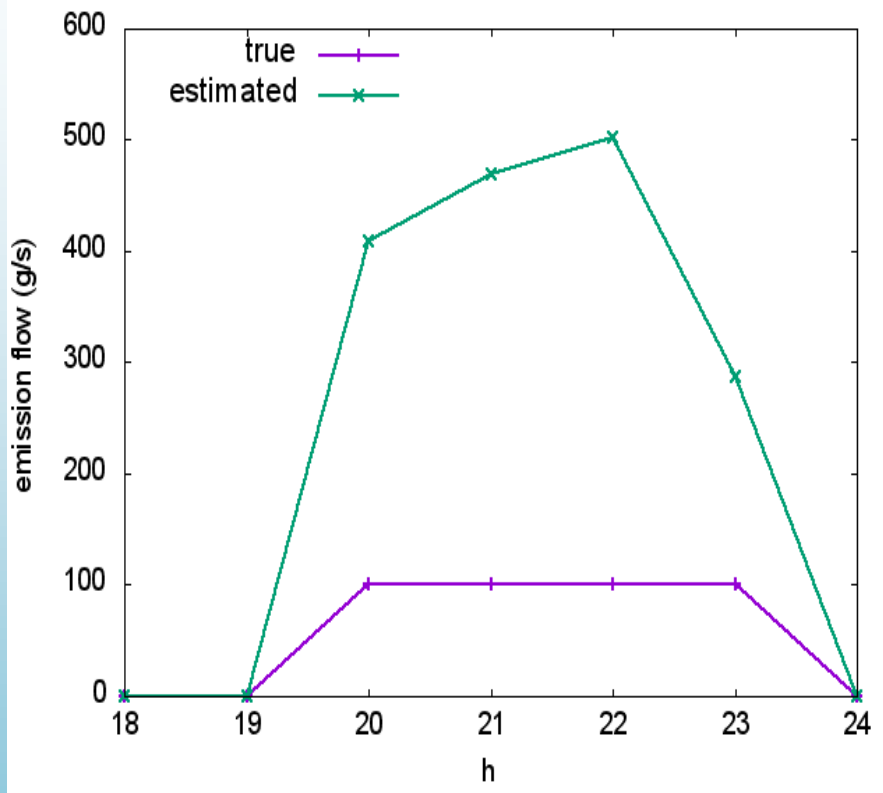
Synthetic case 2

Source position – estimation



Synthetic case 2

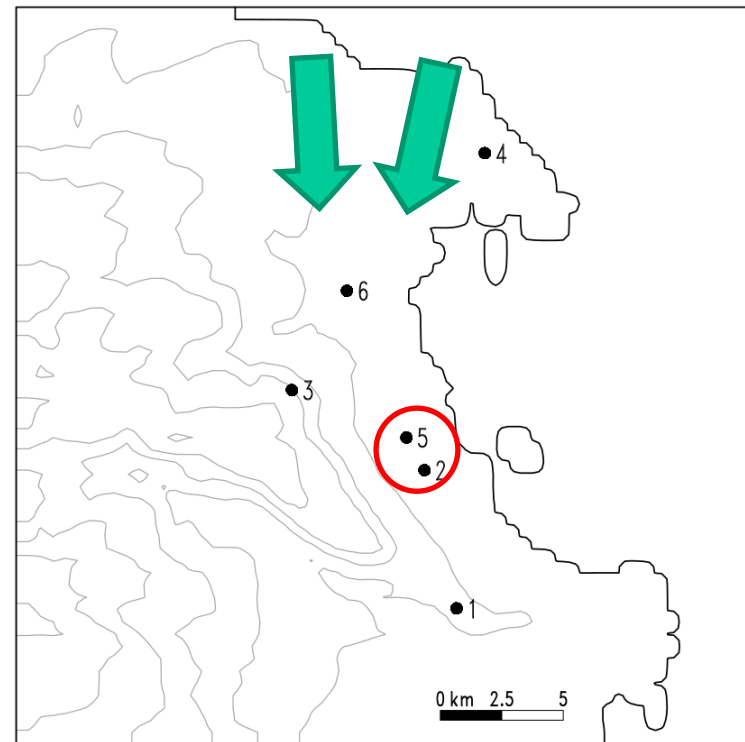
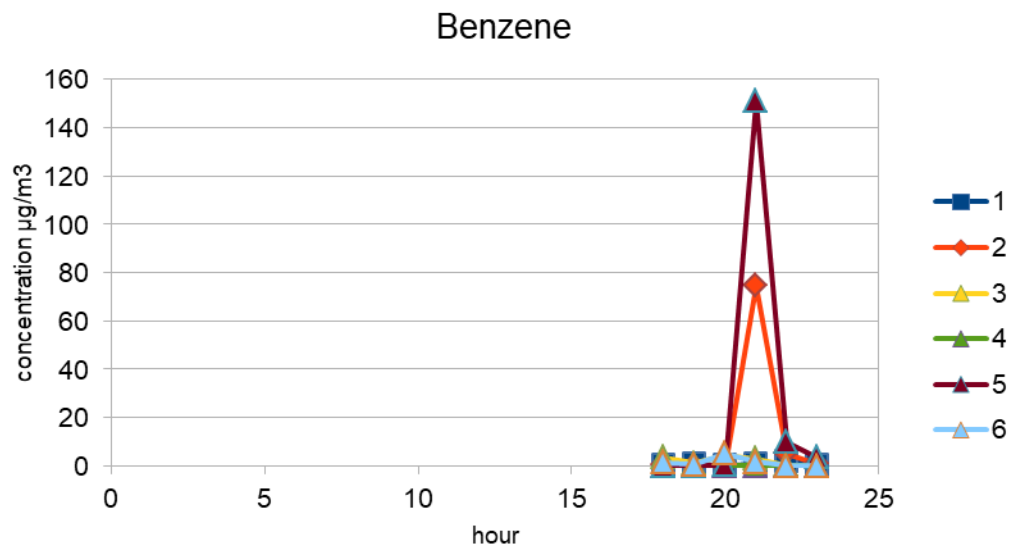
Source position – estimation



Real case

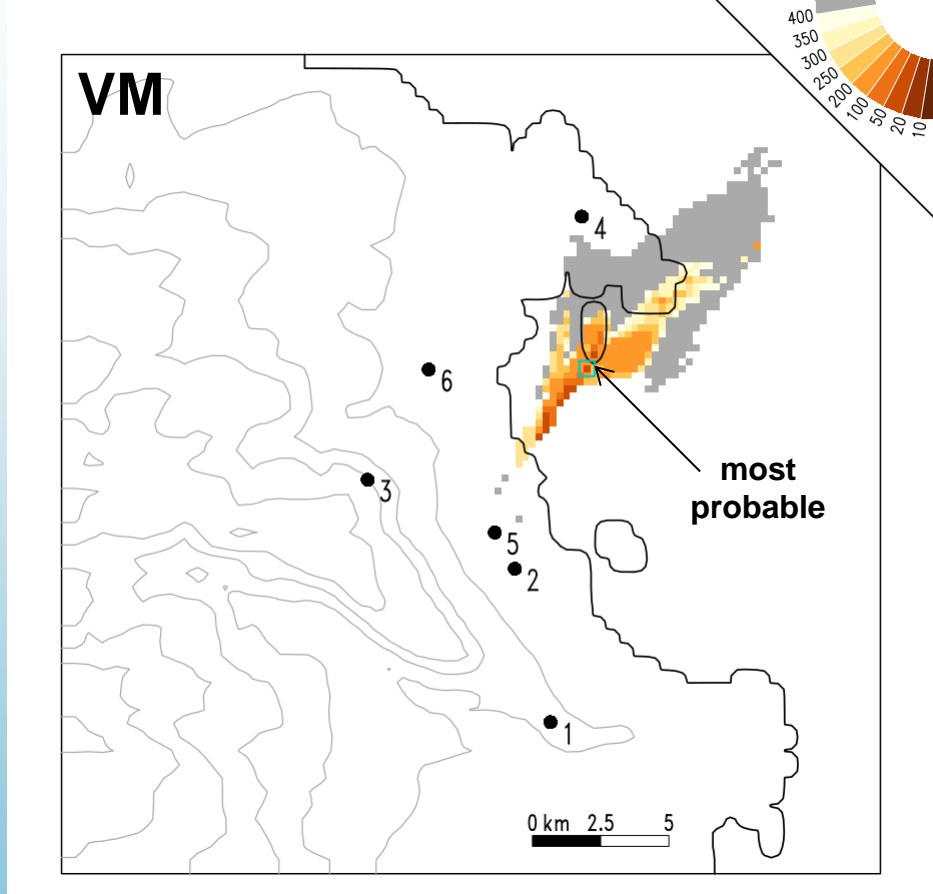
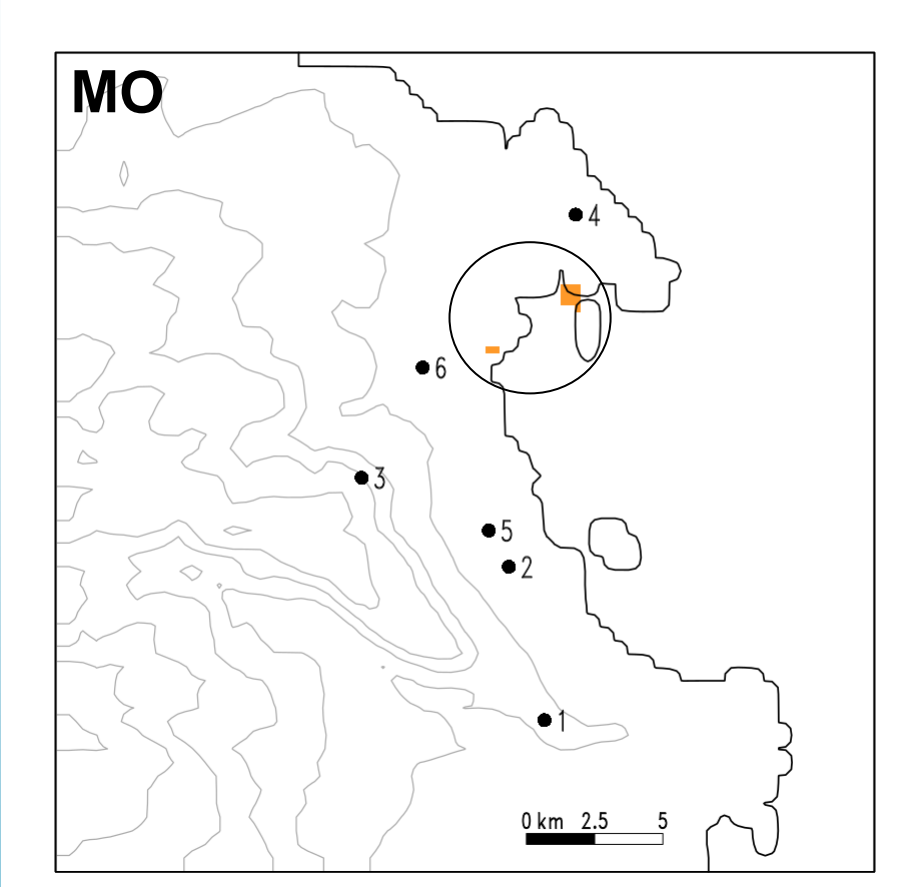
Benzene peak at 21:00

Weak wind (1-2 m/s) mainly from N and NNE

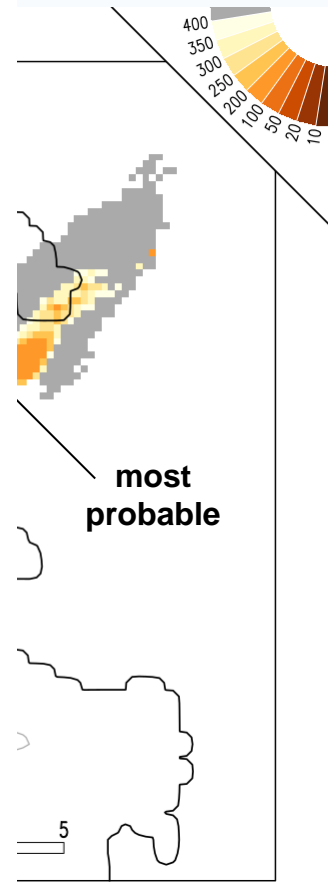
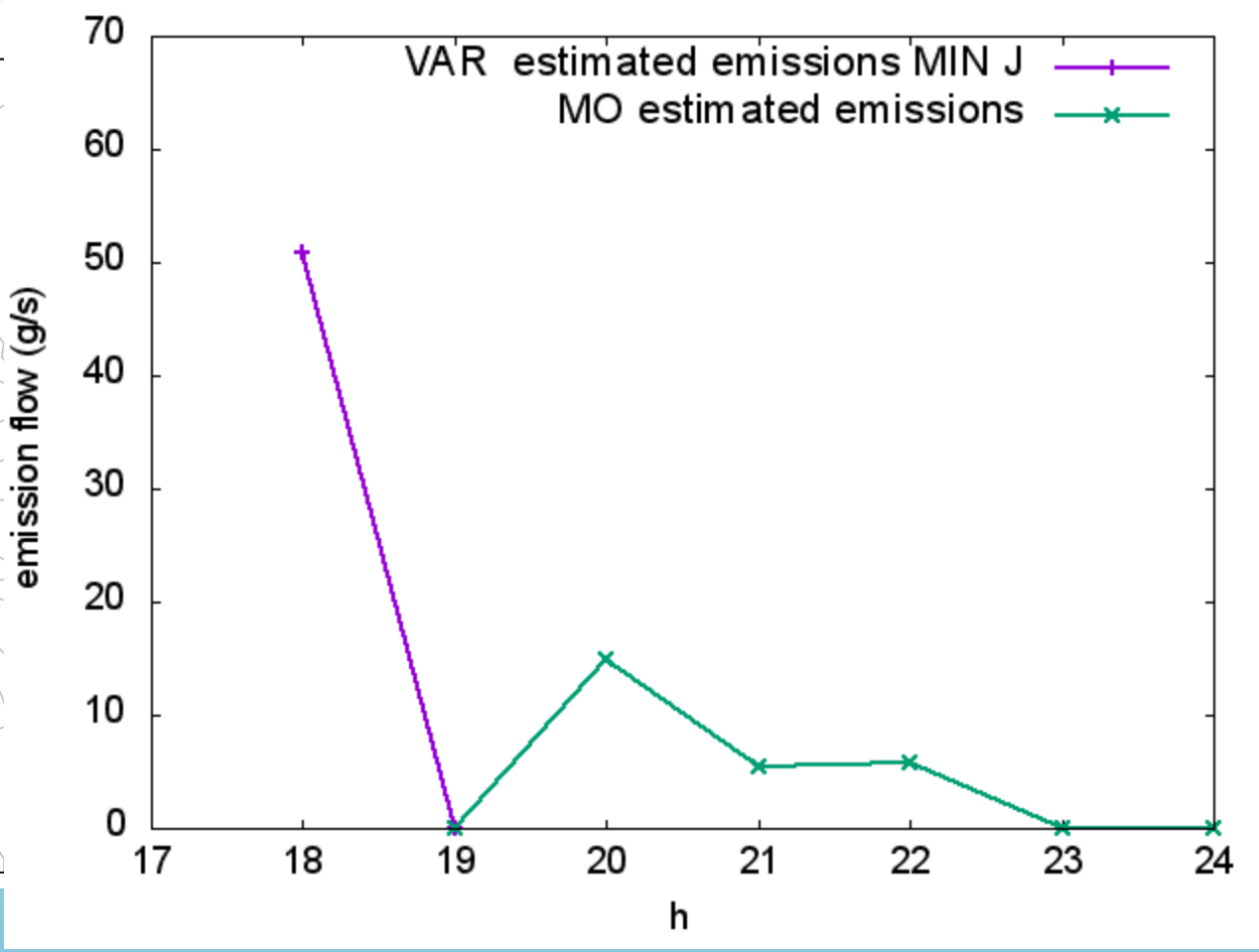
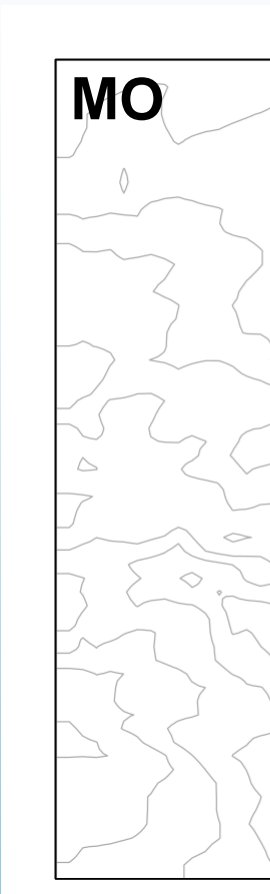


only two samplers
are substantially measuring the peak

Real case – source position



Real case – source position



- ◆ Two **Source Term Estimation (STE)** algorithms, based on **retroSPRAY** results have been tested
- ◆ Real and synthetic test cases and on real operational cases with different spatial and temporal time scales
- Critical point 1: definition of the **wind** field: advection and transport
- Critical point 2: **Station spatial distribution**, particularly with respect to main wind directions
- **ZERO observations** are useful to exclude impossible, or very unlikely, source locations, particularly if upwind to the source

When 1) **wind uncertainty** is **small** and 2) **observational information** is **sufficient**, both method locate the **source position** with acceptable accuracy

The **variational method** seems to provide a more accurate estimate of the source position and in particular of the emitted quantities, even if in an operational environment, for a rapid response, the **maximum overlap** method gives reasonable results