

The MUST model evaluation exercise: Statistical analysis of modelling results

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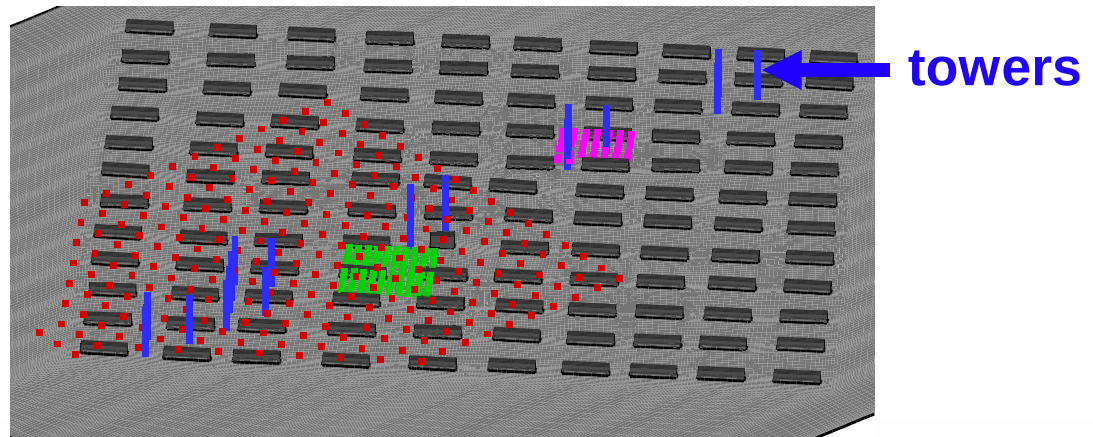
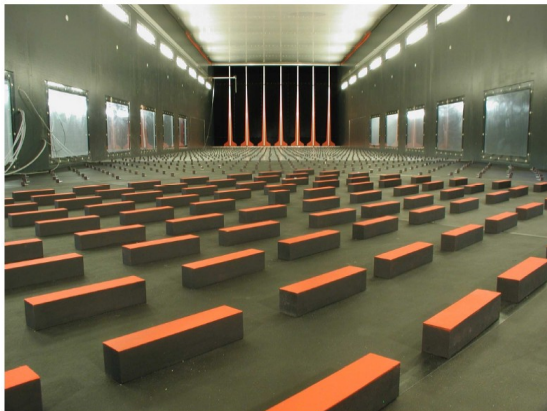
HARMO 12

***12th International Conference on Harmonisation within
Atmospheric Dispersion Modelling for Regulatory Purposes***

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- **Introduction**
- **Definition of hit rate**
- **Resulting metrics for the flow field at towers**
- **Definition of BOOT metrics for concentrations**
- **Resulting metrics for concentrations**
- **Definition of mean metrics for concentrations**
- **Resulting mean metrics for concentrations**
- **Conclusions**

- **COST 732 protocol for model evaluation – validation part**
 - qualitative data analysis
 - quantitative data analysis with metrics
- **Metrics for validation**
 - hit rate and BOOT metrics
 - point by point comparison (paired in space; statistically steady results)
 - available for **app. 30 CFD model runs** (in principle)
 - => Statistics of metrics from individual model results (N-version testing)
- **MUST wind tunnel case with -45° approach flow**



- **Hit rate**

$$q = \frac{1}{N} \sum_{n=1}^N i_n \quad i_n = \begin{cases} 1 & \text{if } |(O_n - P_n)/O_n| \leq \Delta_r \text{ or } |O_n - P_n| \leq \Delta_a \\ 0 & \text{otherwise} \end{cases}$$

with N: number of measurement positions

O_n : observation at position n

P_n : prediction at position n

$\Delta_r = 0.25$ (allowed **relative** difference)

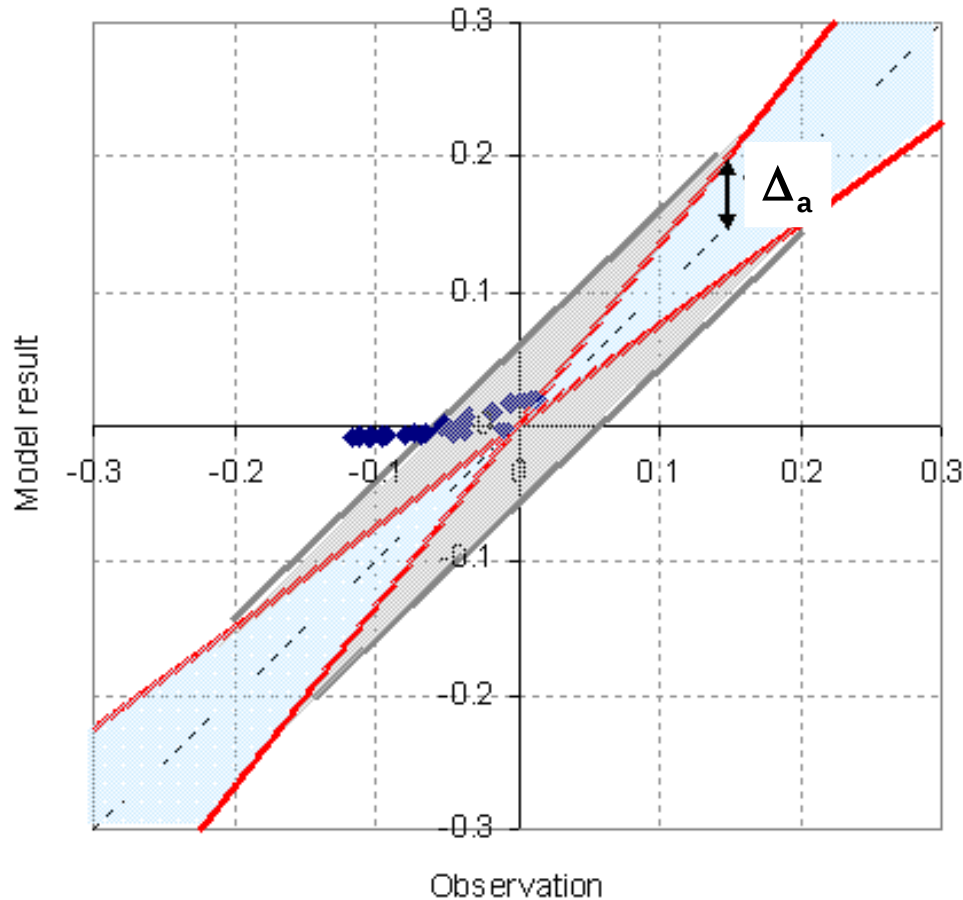
Δ_a (allowed **absolute** difference)

equal to measurement uncertainty

	U/U_{ref}	W/U_{ref}	k/U_{ref}^2
Δ_a	0.008	0.007	0.005

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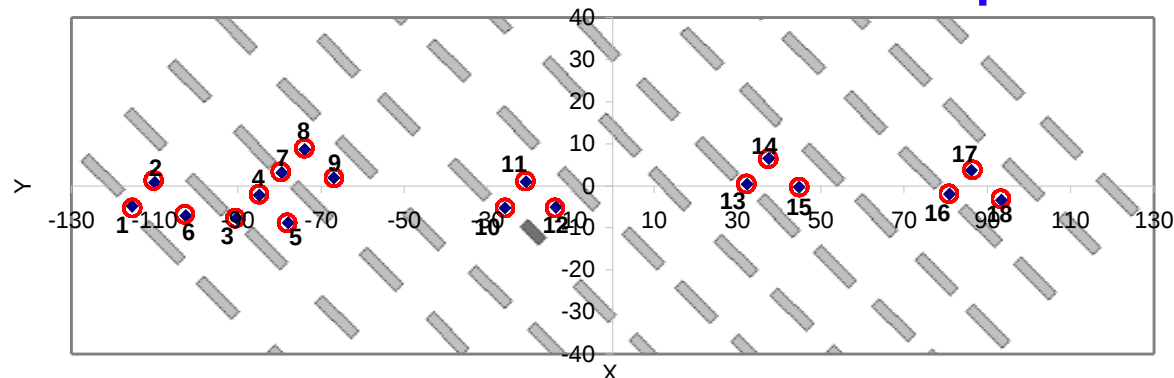
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Δ_a (allowed **absolute** difference)

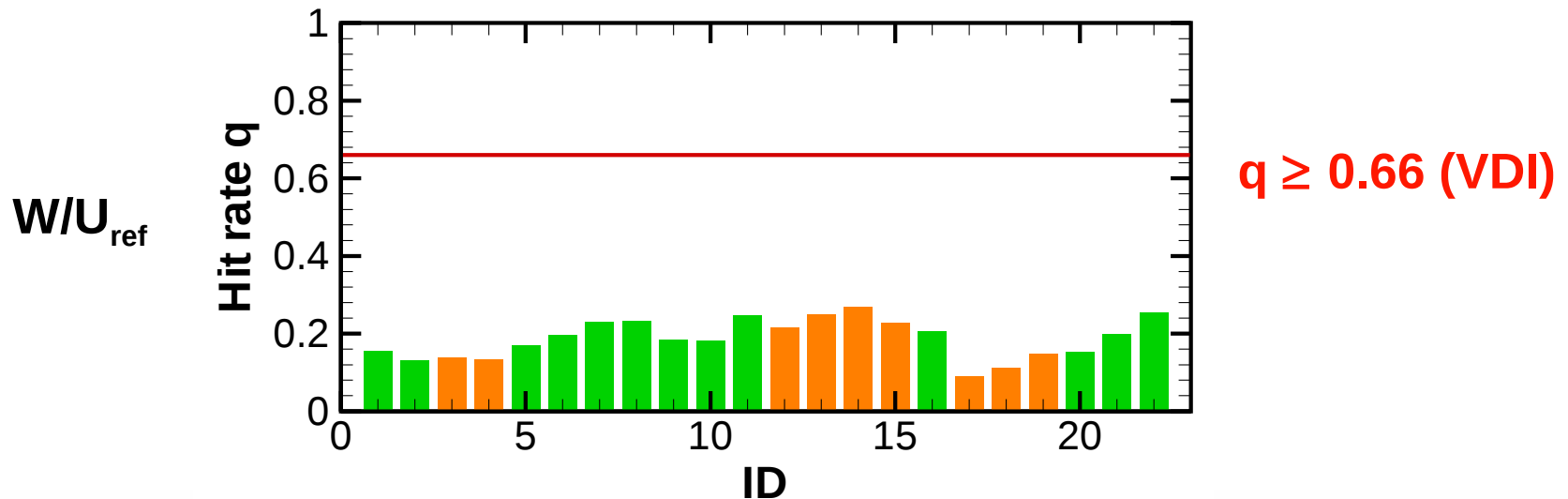
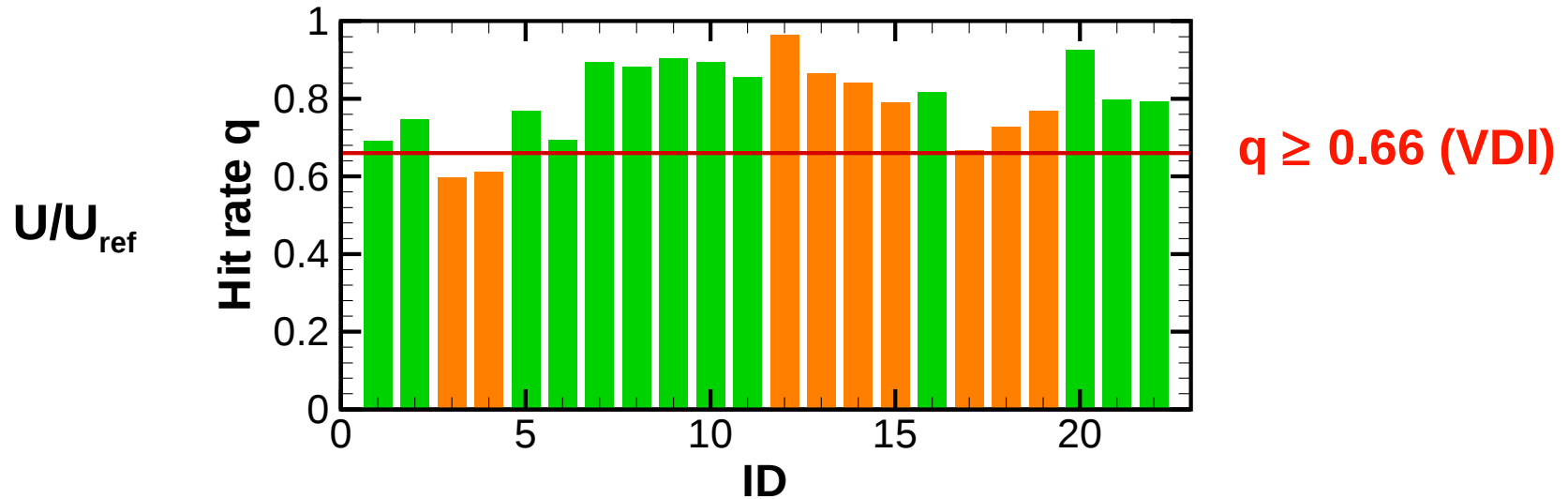
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	U/U_{ref}	W/U_{ref}	k/U_{ref}^2
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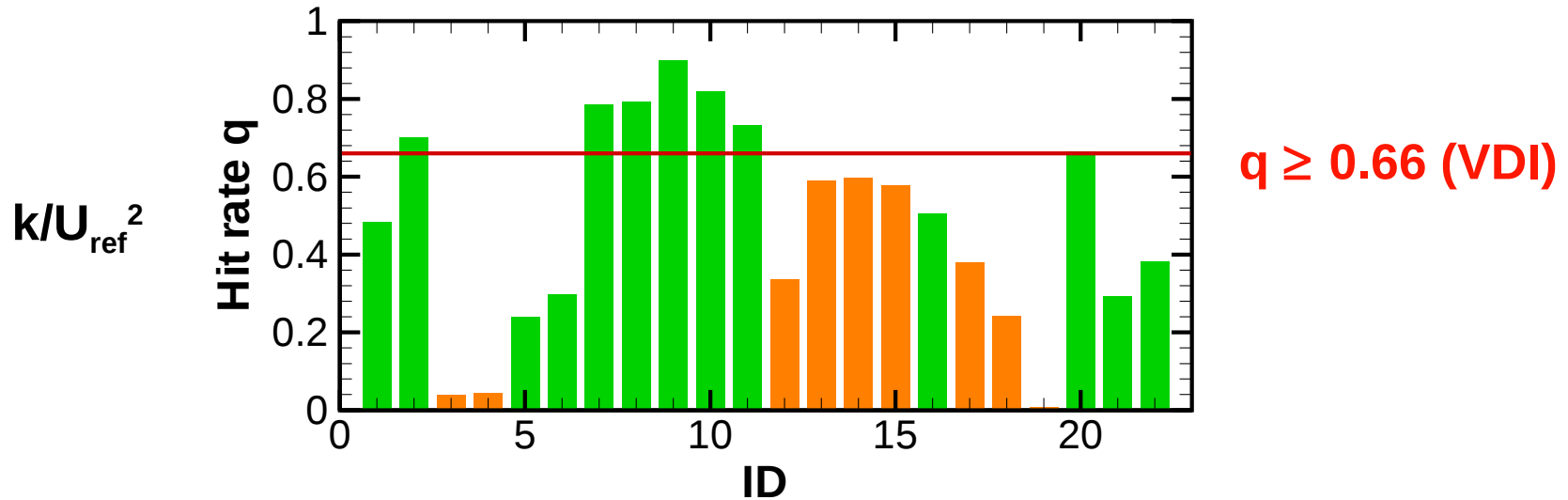
=> evaluated at 497 tower measurement positions



- Hit rate for mean velocities (at 497 tower measurement positions)



- Hit rate for turbulent kinetic energy (at towers)



difference in definition

$$\left(k/U_{ref}^2\right)_o = 0.5 \cdot \left[\left(U_{rms}/U_{ref}\right)_o^2 + 2 \cdot \left(W_{rms}/U_{ref}\right)_o^2\right]$$

$$\left(k/U_{ref}^2\right)_p = 0.5 \cdot \left[\left(U_{rms}/U_{ref}\right)_p^2 + \left(V_{rms}/U_{ref}\right)_p^2 + \left(W_{rms}/U_{ref}\right)_p^2\right]$$

has only a very small influence on the hit rate

- **Normalised concentration** $C^* = C \cdot U_{ref} \cdot H^2 / Q_{source}$
- **BOOT metrics** $FAC2 = \text{fraction of data with } 0.5 \leq C_p^* / C_o^* \leq 2$

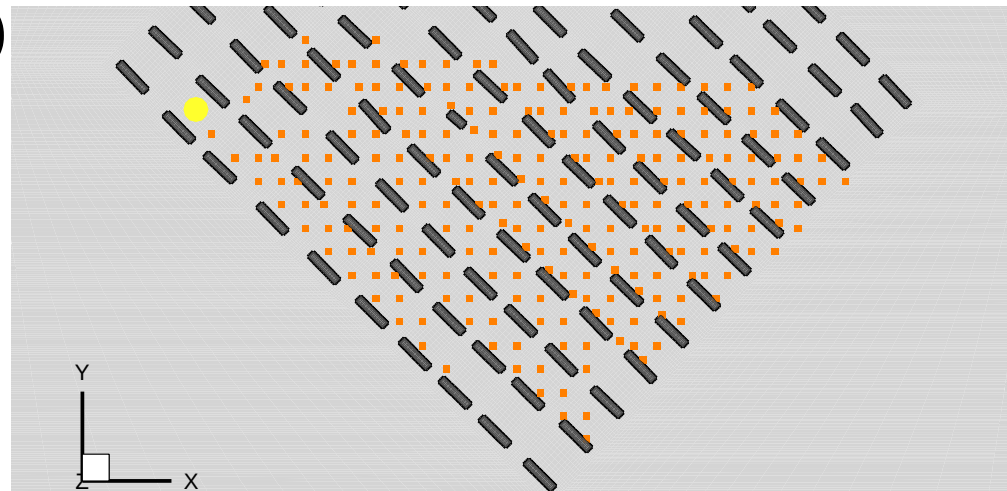
$$FB = 2 \left(\langle C_o^* \rangle - \langle C_p^* \rangle \right) / \left(\langle C_o^* \rangle + \langle C_p^* \rangle \right) \quad NMSE = \left\langle \left(C_o^* - C_p^* \right)^2 \right\rangle / \left(\langle C_o^* \rangle \cdot \langle C_p^* \rangle \right)$$

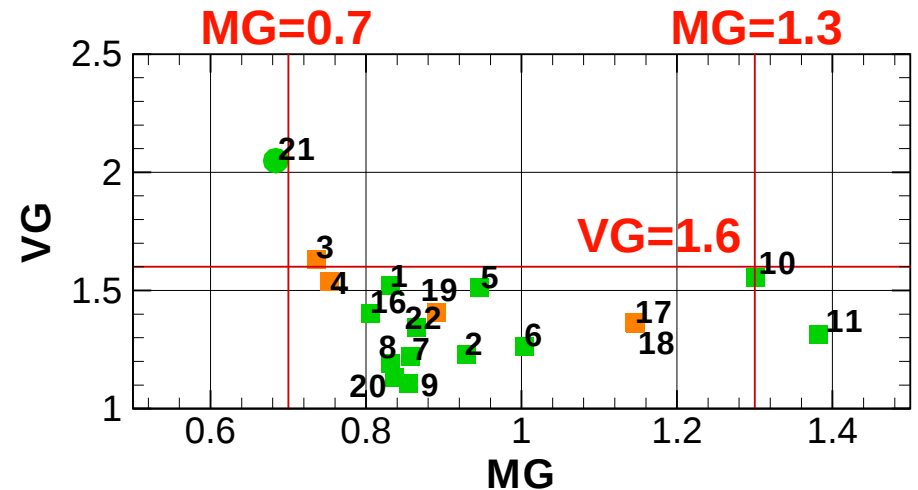
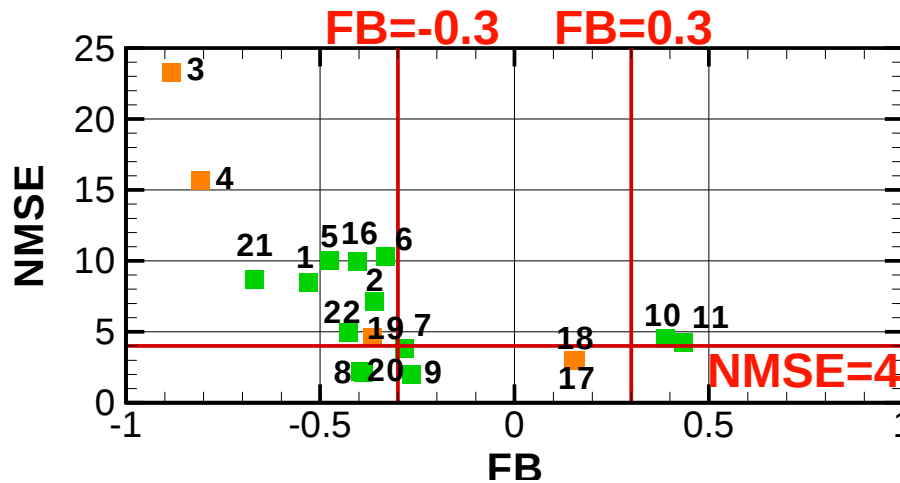
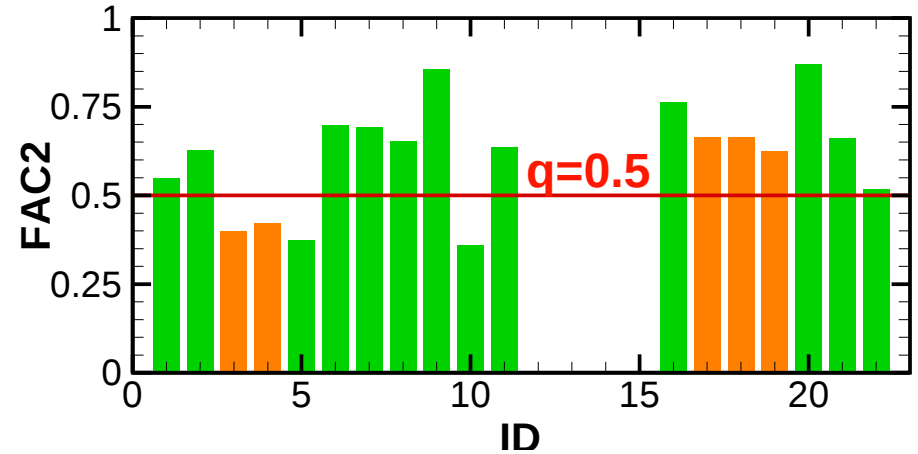
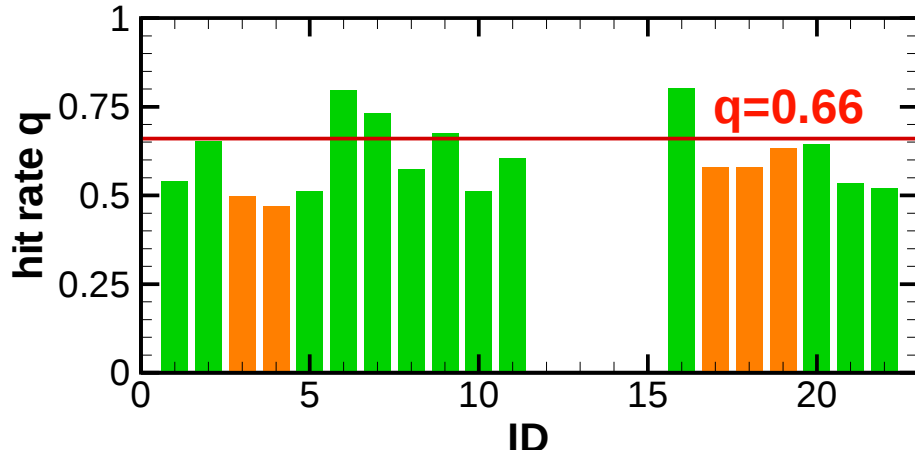
$$MG = \exp \left(\langle \ln C_o^* \rangle - \langle \ln C_p^* \rangle \right) \quad VG = \exp \left[\left\langle \left(\ln C_o^* - \ln C_p^* \right)^2 \right\rangle \right]$$

for MG and VG threshold $\Delta_a = 0.003$ (measurement uncertainty)

- **Measurement positions (256)**

$$z = H/2$$





- **Metrics from mean results at measurement positions (M=13)**

$$\overline{C_p^*} = 1/M \sum_{j=1}^M C_{p,j}^* \quad \tilde{C}_p^* = \text{median}[C_{p,j}^*]_{j=1,M}$$

$$\Rightarrow \text{e.g. } \bar{q} \equiv q(\overline{C_p^*}), \quad \tilde{q} \equiv q(\tilde{C}_p^*)$$

- **Mean metrics from individual metrics of the models (M=13)**

metrics of model run j: X_j

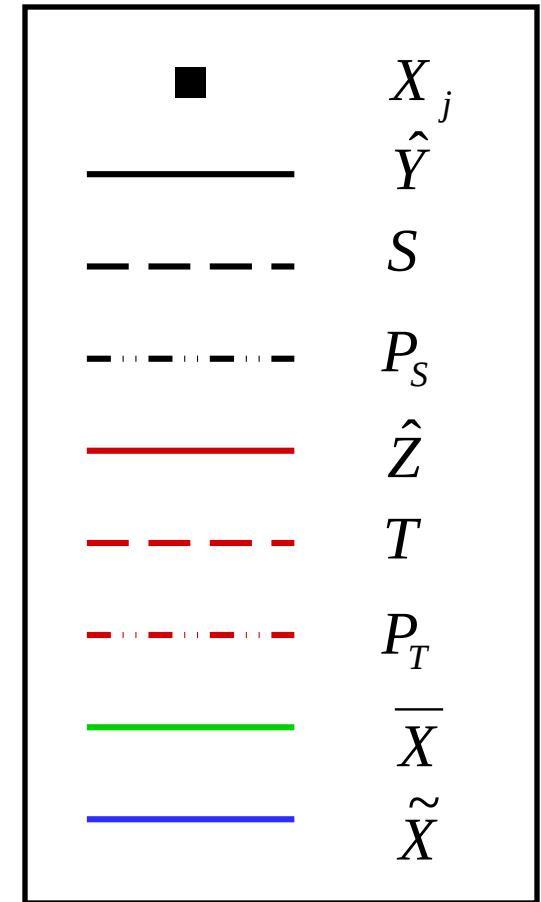
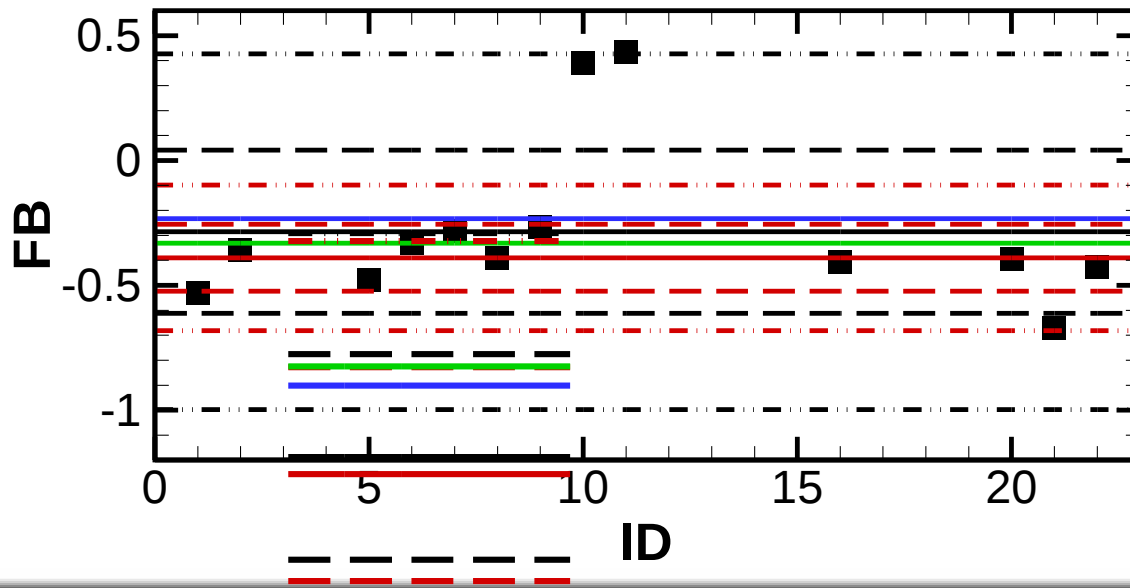
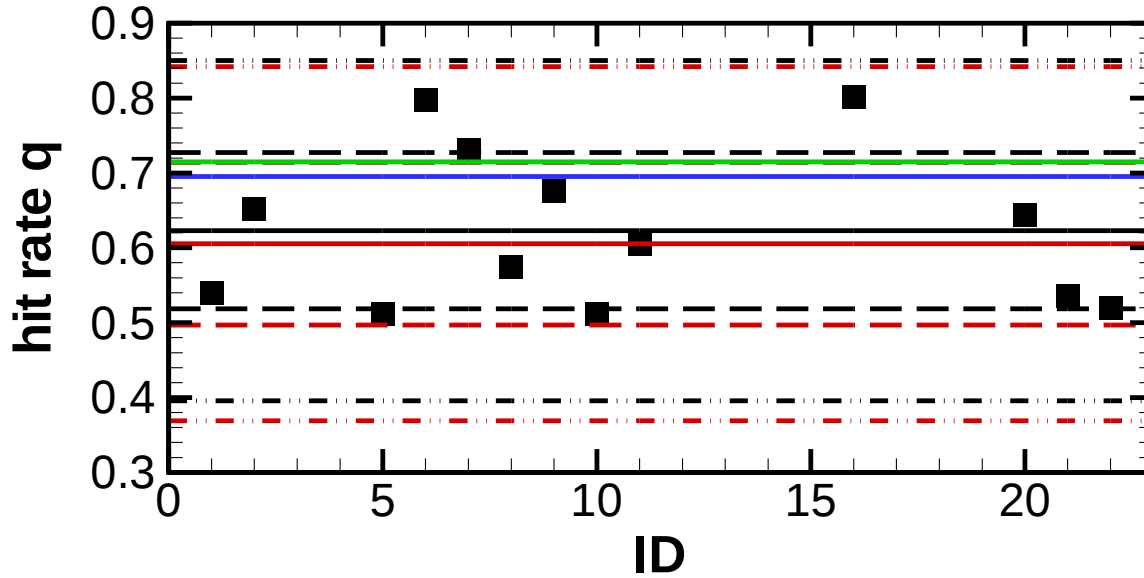
$$\text{mean metrics} \quad \hat{Y} = 1/M \sum_{j=1}^M X_j \quad \hat{Z} = \text{median}[X_j]_{j=1,M}$$

standard deviations

$$S = \left[1/(M-1) \sum_{j=1}^M (X_j - \hat{Y})^2 \right]^{1/2} \quad T = 1/0.6745 \sqrt{M/(M-1)} \text{median}(|X_j - \hat{Z}|)$$

confidence intervals (95%, based on student t distribution)

$$P_S = 2.179S \quad P_T = 2.179T$$



Validation metrics for the MUST -45° case

- concise indication of model performance
- hit rate for flow low for velocity components with small magnitude
- state of the art achievable for all concentration metrics
- further analysis of the statistics of metrics (N-version testing) necessary

- Metrics from mean results at measurement positions (M=13)

averages $\overline{C_p^*} = 1/M \sum_{j=1}^M C_{p,j}^*$ $\tilde{C}_p^* = \text{median}[C_{p,j}^*]_{j=1,M}$

standard deviations

$$\overline{\sigma_p} = \left[\frac{1}{M-1} \sum_{j=1}^M (C_{p,j}^* - \overline{C_p^*})^2 \right]^{1/2} \quad \tilde{\sigma}_p = 1/0.6745 \sqrt{M/(M-1)} \text{median}(|C_{p,j}^* - \tilde{C}_p^*|)$$

