

# Comparison of results from dispersion models for regulatory purposes based on Gaussian and Lagrangian algorithms: an evaluating literature study

9<sup>th</sup> International Conference on Harmonisation within  
Atmospheric Dispersion Modelling for Regulatory Purposes

Garmisch-Partenkirchen, 01. - 04.06. 2004

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# German Federal Office for Radiation Protection

(Bundesamt für Strahlenschutz, BfS)

## Tasks

- radiation protection
- safety in nuclear engineering
- transportation and safekeeping of nuclear fuel
- radioactive waste disposal

# The BfS sites

Rendsburg

Bonn

Hanau

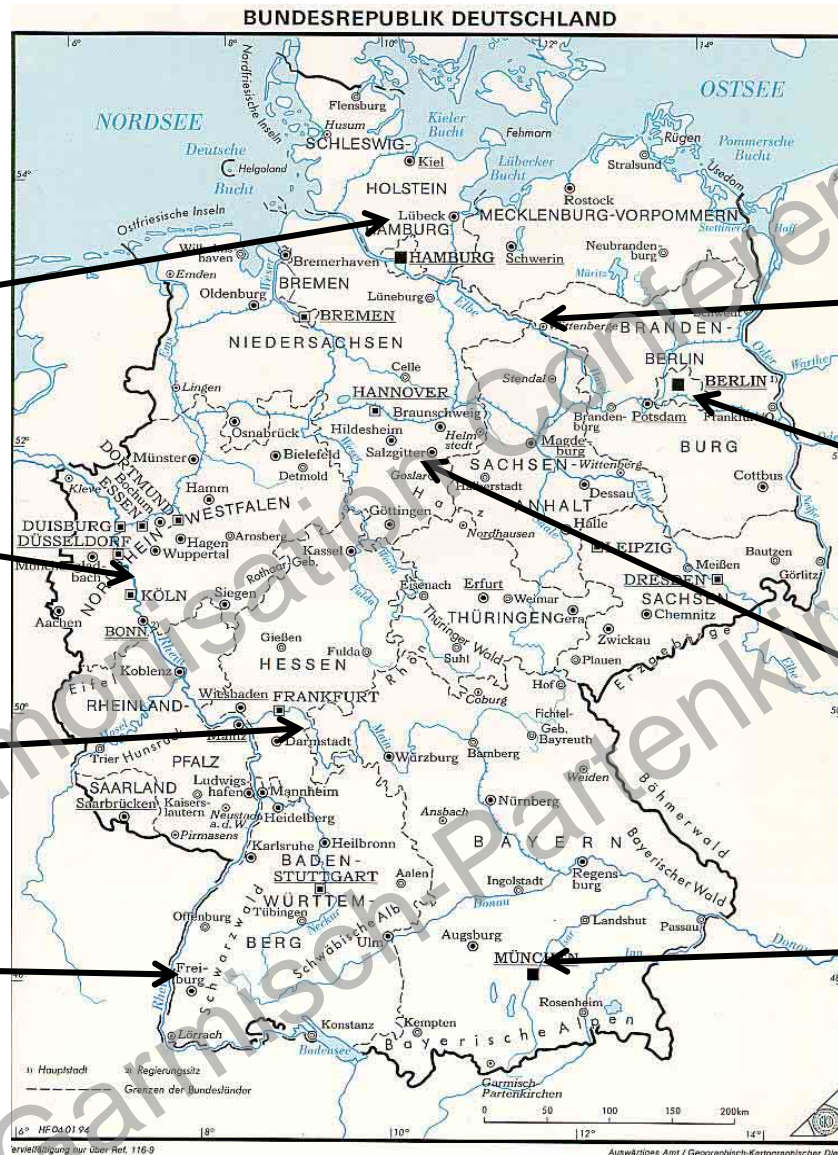
Freiburg

Gorleben

Berlin

Salzgitter

Neuherberg,  
Munch



BfS has responsibility  
for

nuclear power plants  
in the  
Federal Republic  
of Germany

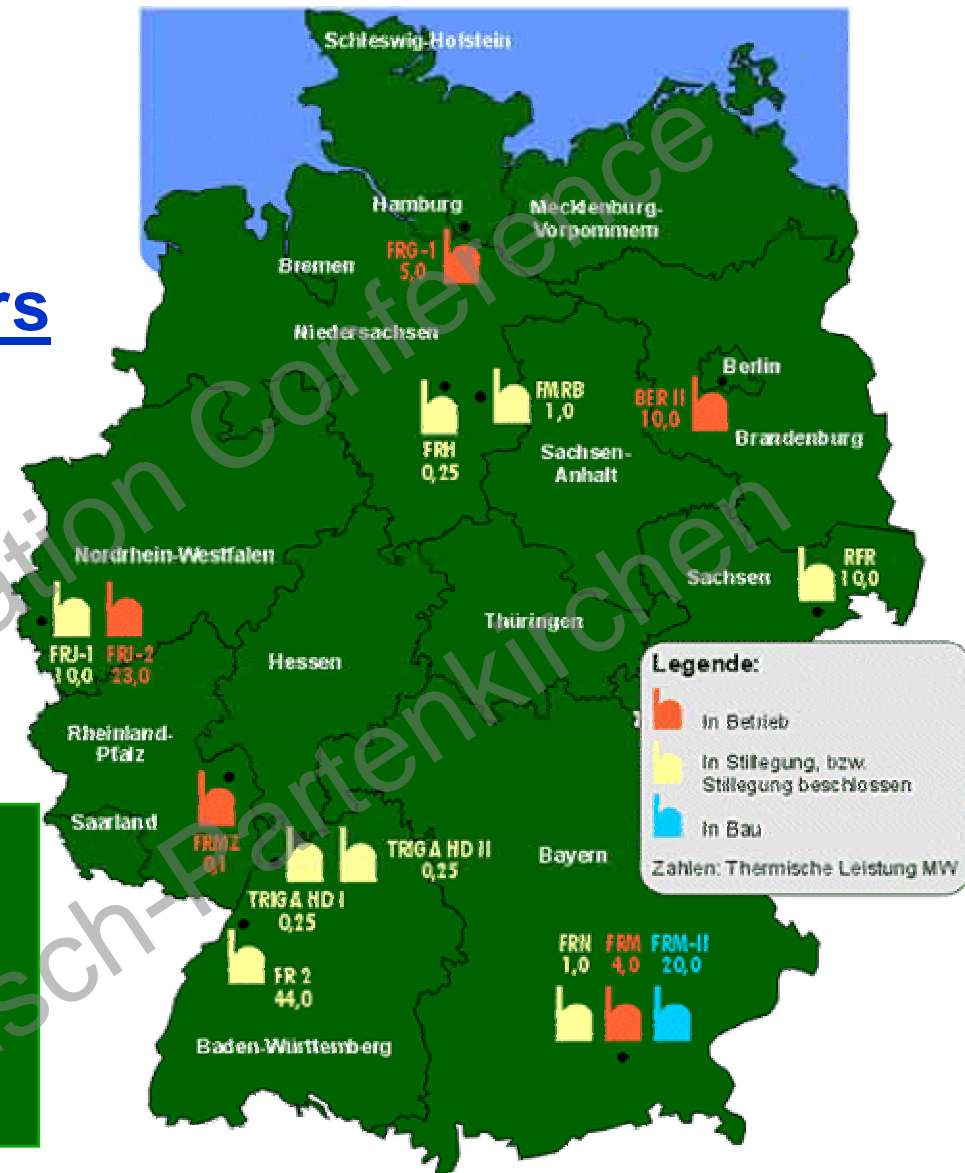
- reactor in operation
- reactor shut down or shut down is decided



# BfS has responsibility for

## nuclear research reactors in the Federal Republic of Germany

- reactor in operation
- reactor shut down or shut down is decided
- reactor under construction





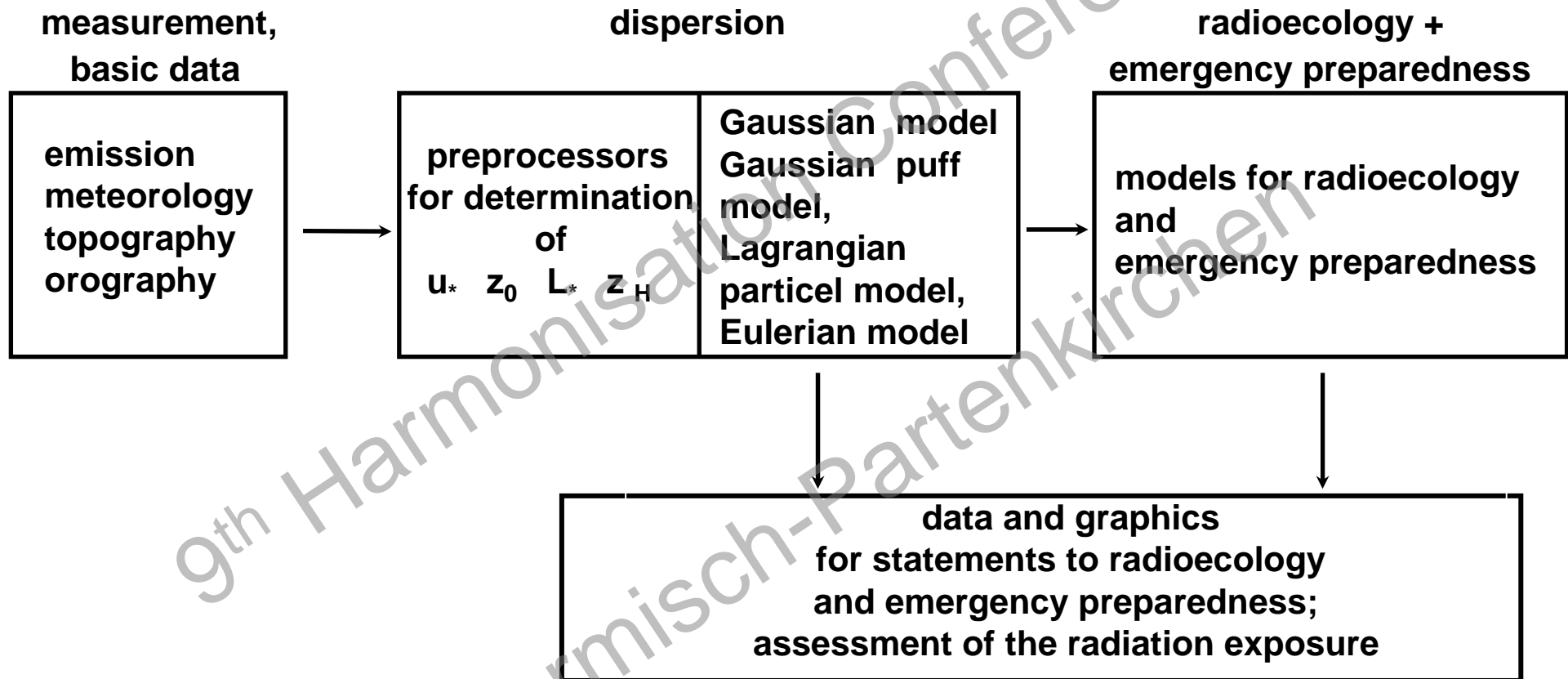
**BfS has responsibility  
for**

**supply and disposal of  
nuclear material  
in the  
Federal Republic  
of Germany**

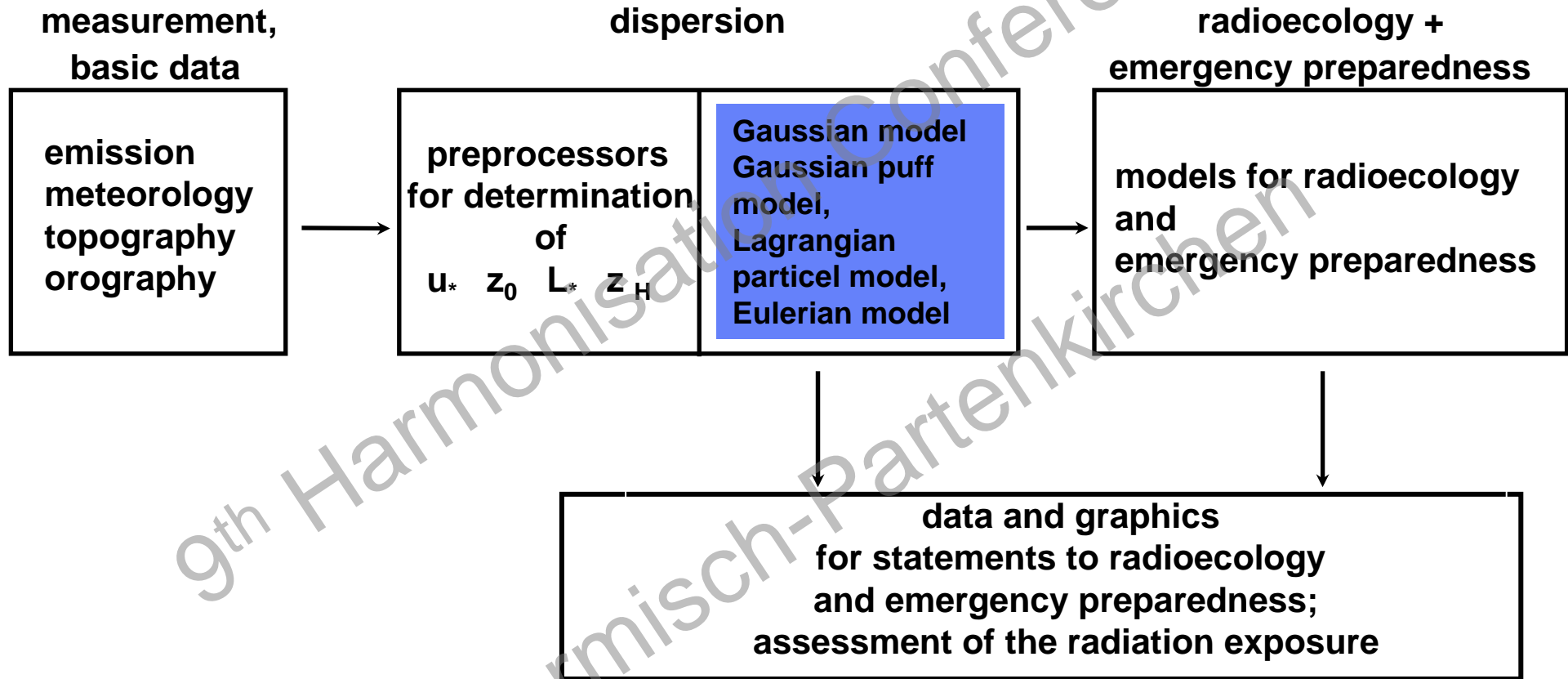
- **facility in operation**
- **facility shut down or  
shut down is in progress**



# Computational procedures for radiation exposure after emission in the atmosphere



# Computational procedures for radiation exposure after emission in the atmosphere





# Computational procedures for radiation exposure in Germany

## legal procedures

- **AVV** (Technical guideline for computation of radiation exposure during normal operation)
- **SBG** (Technical guideline for computation of radiation exposure during emergencies)
- **expert systems (e.g. RODOS, ...)**

# Gaussian model in German legal procedures

## Gaussian dispersion of concentration

(total reflection from surface)

$$\bar{c}(x, y, z) = \frac{Q_0}{2\pi \cdot u_x \cdot \sigma_y \sigma_z} \exp\left[-\frac{y^2}{2\sigma_y^2}\right] \cdot \left\{ \exp\left[-\frac{(z-H)^2}{2\sigma_z^2}\right] + \exp\left[-\frac{(z+H)^2}{2\sigma_z^2}\right] \right\}$$

$\bar{c}$ : concentration

$Q_0$ : source strength

$\sigma_y, \sigma_z$ : dispersion parameters (variance of Gaussian distribution), measured or derived from  $\sigma_{v,w}$

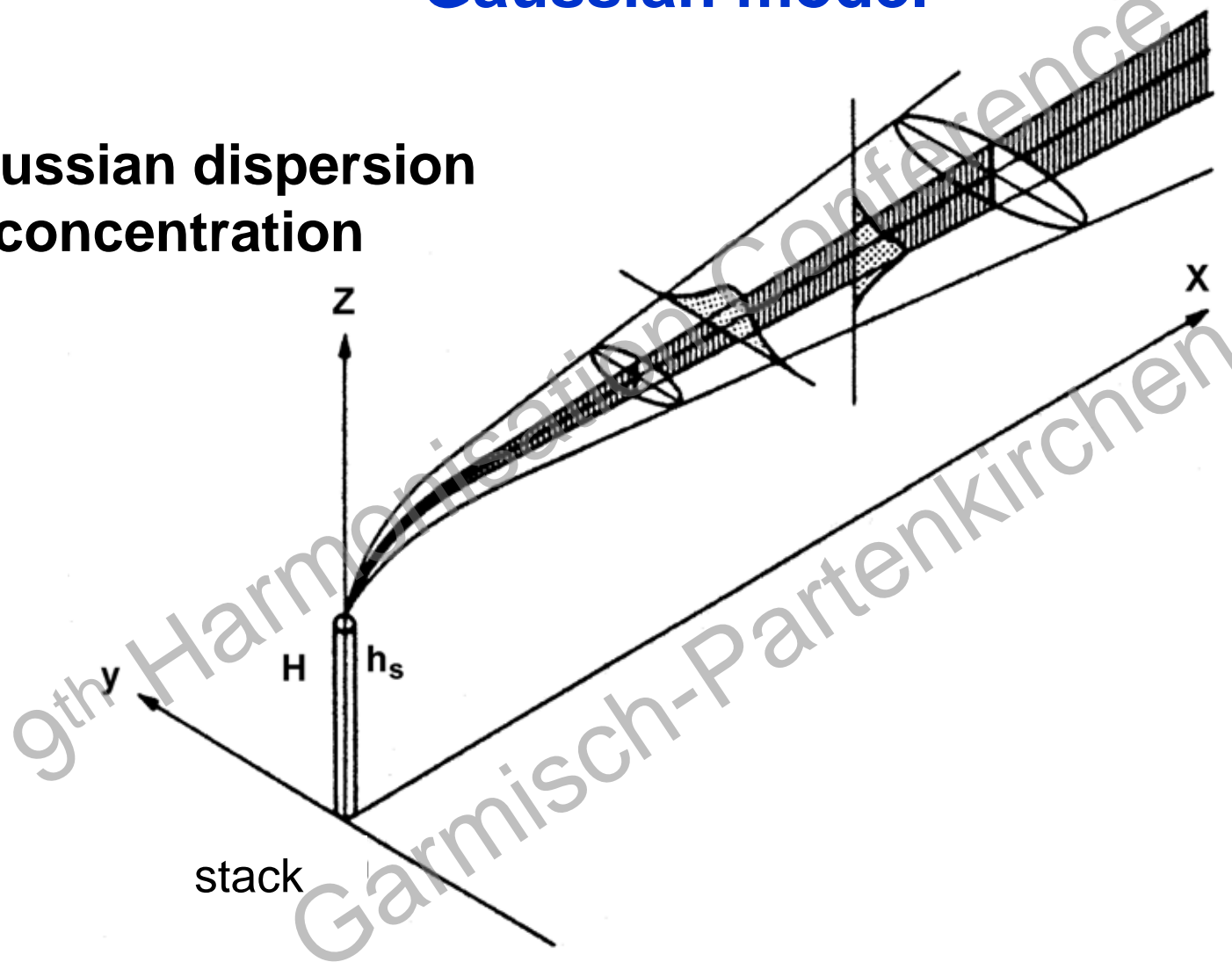
$u_x$ : medium transportation velocity

$H$ : height of plume axis (effective emission height)

$x, y, z$ : Cartesian coordinates of emission point, with  $y$  and  $z$  orthogonal to wind direction

# Gaussian model

## Gaussian dispersion of concentration



**real dispersion conditions**

**differ a lot from Gaussian model assumptions**



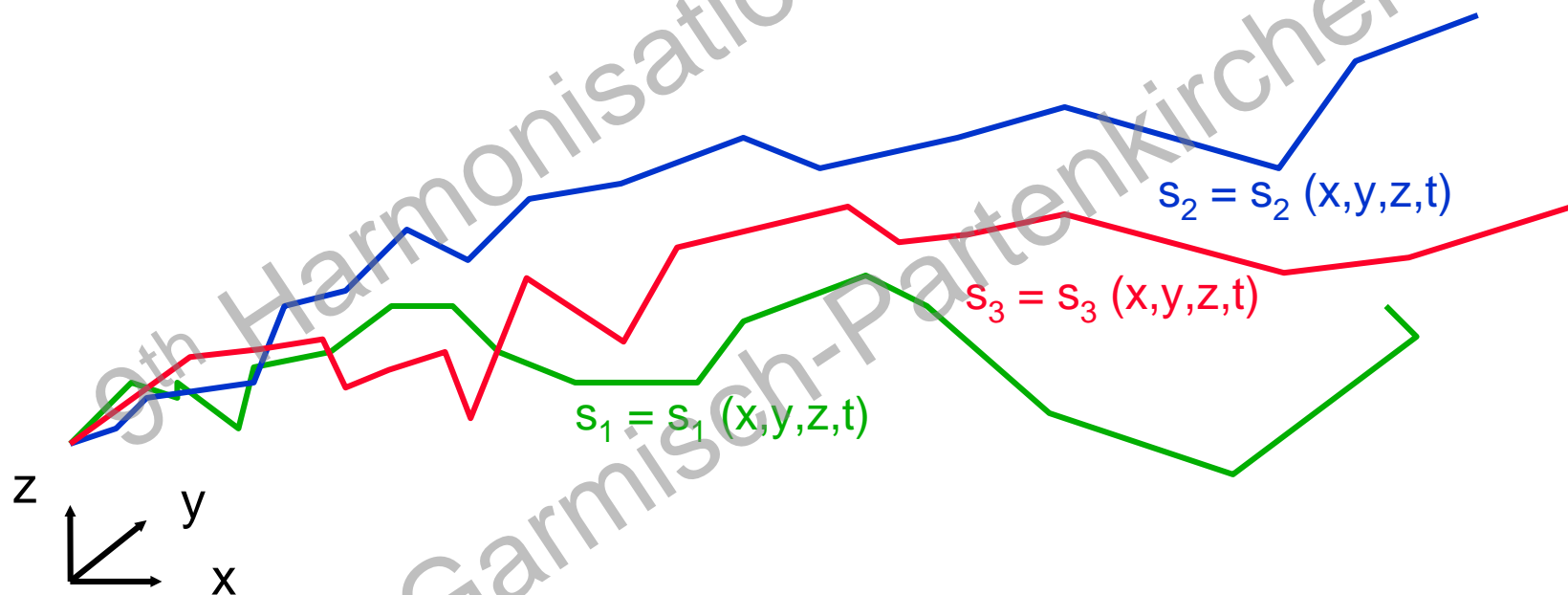
# Gaussian model

generally not considered:

- windprofile
- height dependance of windvector (Ekman-spiral)
- windshear
- local / regional windsystems
- short term / explosive releases
- inhomogeneous surface roughness
- low inversions
- inhomogeneous / instationary turbulence
- low wind speed (high pressure area)

# Possible alternative: Lagrangian model

particle model, consideration of (different) particle trajectories





# Lagrangian model, basic procedures

$$X_{n+1} = X_n + \Delta t \cdot (\bar{u}_n + u_n' + \hat{u}_n)$$

- **mean wind velocity**  
advection (large scale processes)
- **turbulent wind velocity**  
„directed“ turbulence ( ~ Lagrangian correlation time)  
+ stochastic turbulence
- **additional wind velocity**  
description of external processes (e.g. sedimentation,  
inhomogeneous turbulence)

# Lagrangian model

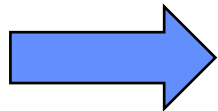
advantage / disadvantage

advantage

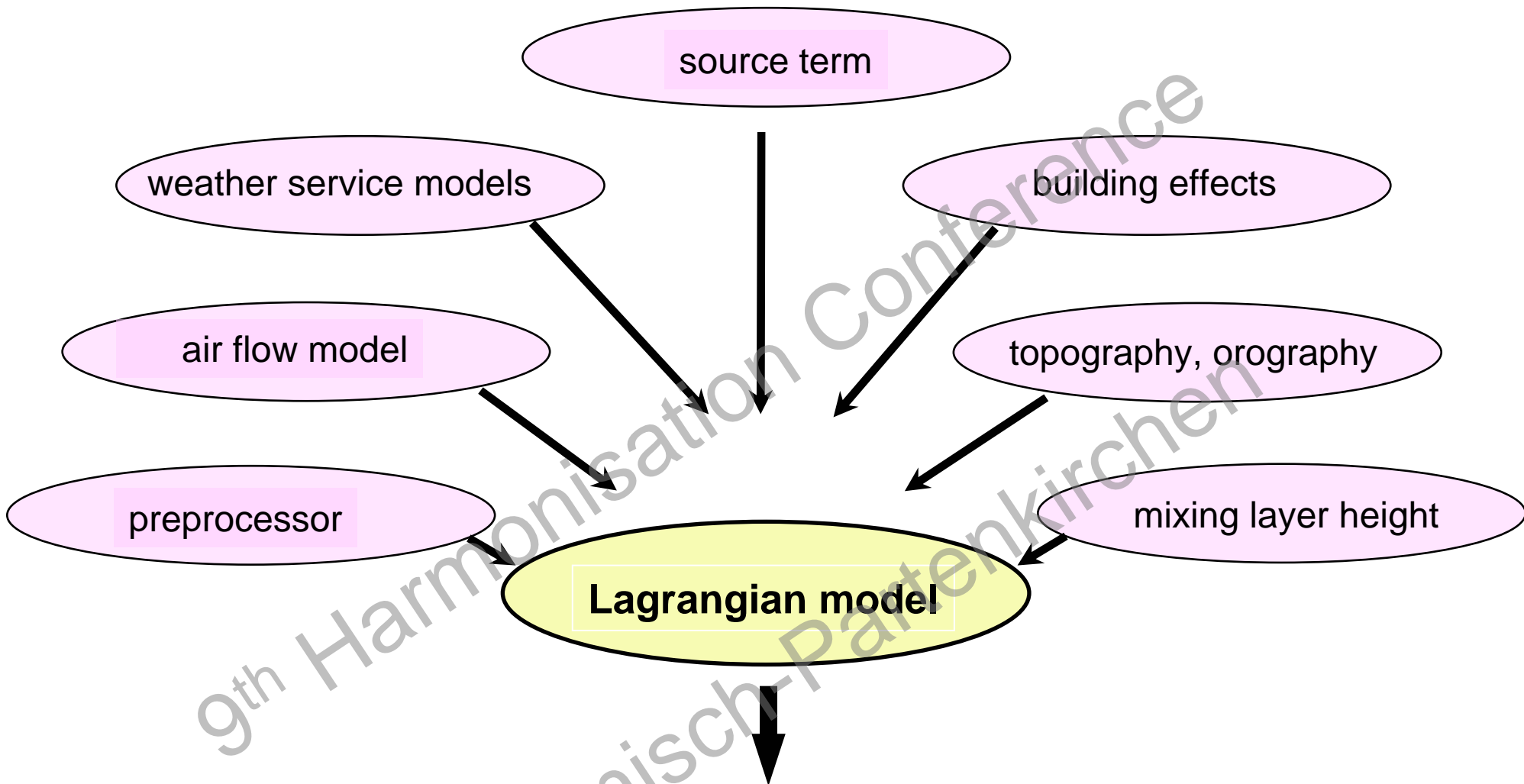
- several meteorological and physical effects can be considered more intensively

disadvantage

- additional parameters necessary resp. available (  $L_*$ ,  $u_*$ ,  $z_0$ ,  $d$ ,  $T$ , turb. heat flux, turb. flux for momentum)
- air flow model necessary
- additional measurement data



**But : SODAR, diagn. / prognostic models**



**results close to reality**  
**EURATOM Guidelines 96/29 !**

**Gaussian model**  
**GM**



**Lagrangian model**  
**LPM**



**Comparative considerations**  
**(literature study)**

# Comparative considerations (literature study)

[Glaab, 1986]

**comparison of**

**German Clear Air**

**Regulation(TA Luft )**

**with**

**Lagrangian model**

- flat terrain
- source distance up to 5000 m
- point sources in different heights

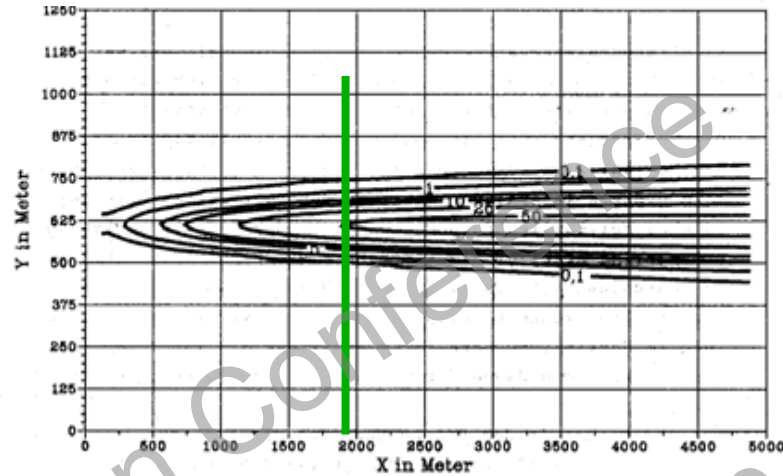
# Comparative consideration

[Glaab, 1986]

isolines of  
surface concentrations  
[ $\mu\text{g}/\text{m}^3$ ]

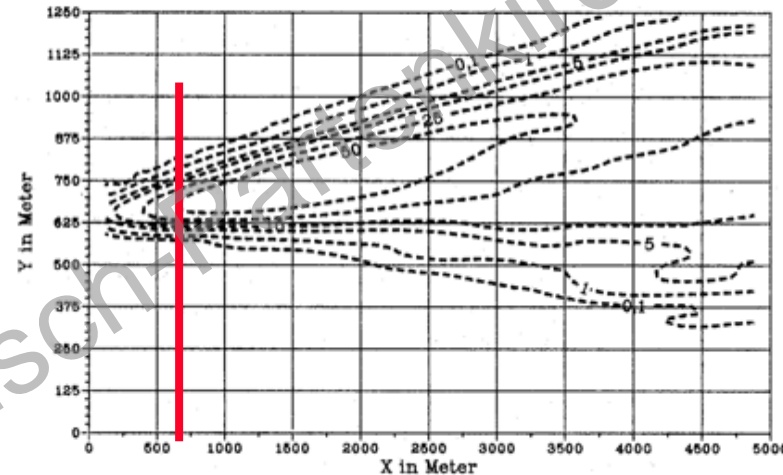
e.g. distance of  
isoline  $50 \mu\text{g}/\text{m}^3$   
from source

source height 21 m



Gauß

figure 13a<sub>1</sub> : surface concentrations in  $\mu\text{g}/\text{m}^3$  (dispersion class I, Gaussian method)



Lagrange

figure 13a<sub>2</sub> : surface concentrations in  $\mu\text{g}/\text{m}^3$  (dispersion class I, particle model)



# Comparative consideration

[Glaab, 1986]

profiles along axis with  
max. surface  
concentrations

[ $\mu\text{g}/\text{m}^3$ ]

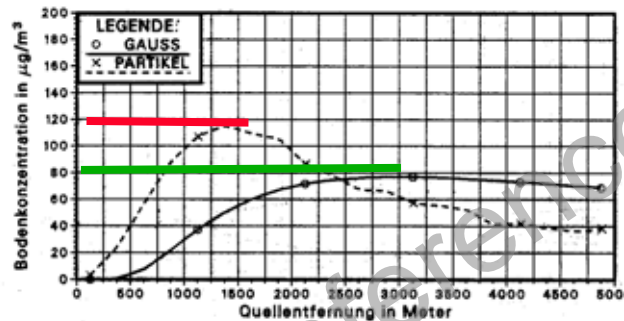


figure 14a : profiles along the axis of maximal surface concentration as a function of source distance (dispersion class I) → F

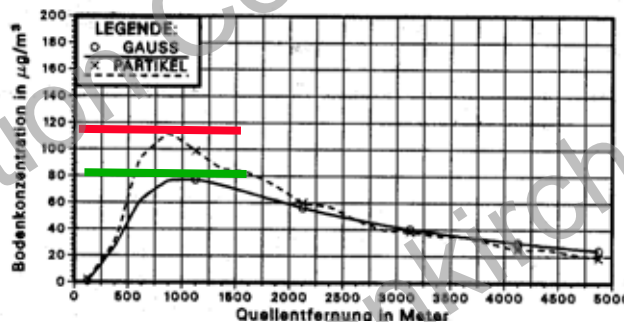


figure 14b : profiles along the axis of maximal surface concentration as a function of source distance (dispersion class II) → E

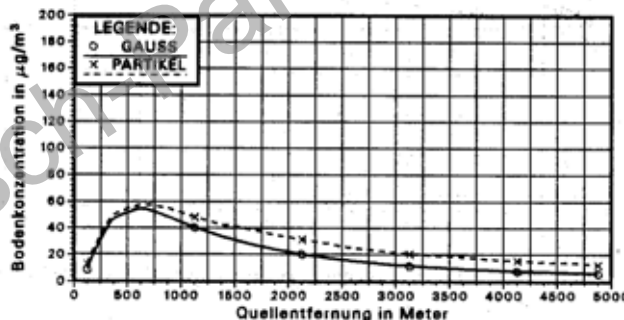


figure 14c : profiles along the axis of maximal surface concentration as a function of source distance (dispersion class III<sub>1</sub>) → D

stability

I F

II E

III<sub>1</sub> D

# Comparative considerations

[Glaab, 1986]

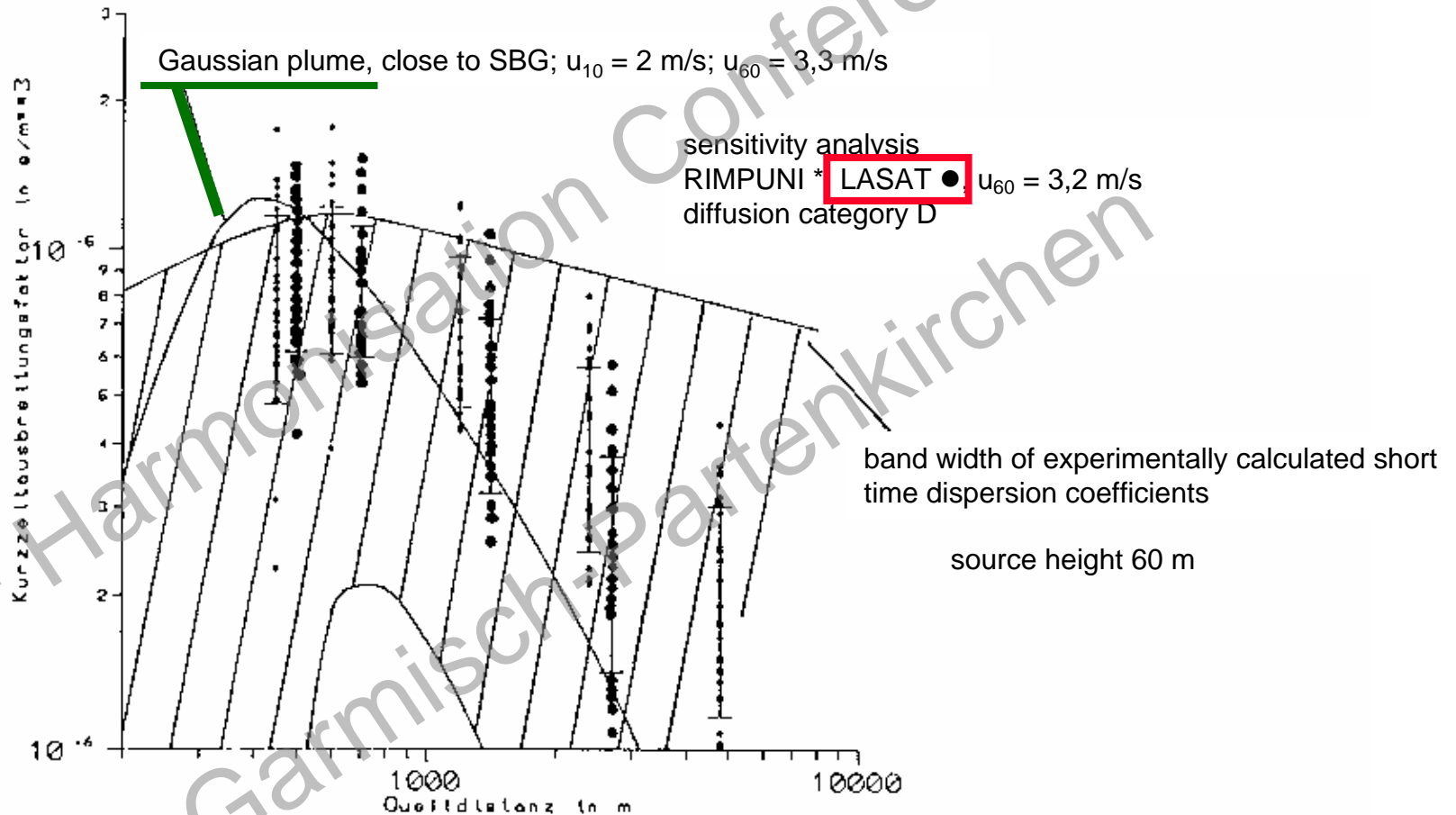
**general conclusions:  
the Lagrangian model computes in**

- **stable case**  
position of high concentrations closer to source,  
significant higher ground surface concentrations
- **unstable case**  
lower concentrations close to source  
higher values in greater distance
- **greater differences when sources are close to surface**

# Comparative considerations (literature study)

[Martens et al 1993]

## short time dispersion coefficient under the plume axis



# Comparative considerations (literature study)

[Martens et al 1993]

## results:

- all models are practical to describe average conditions
- average parameters of boundary layer ( like in GM ) are not suited for consideration of individual cases
- parameters of boundary layer ( $u_*$ ,  $L$ ,  $z_0$ ,  $m_H$ ) like in LPM describe better the situation of stability than categories of diffusion

# Comparative consideration Gaussian and Lagrangian model

[Janicke, 2001 a]

## comparison of

- **GuidelineTA Luft (AUSTAL 86 based on GM) with**
- **advanced model system**  
**Lagrangian particle model LASAT**

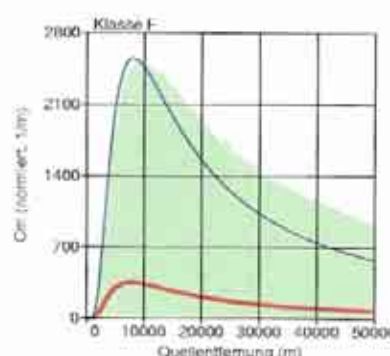
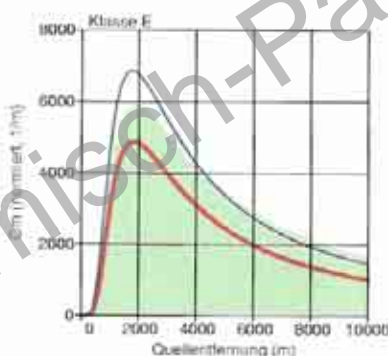
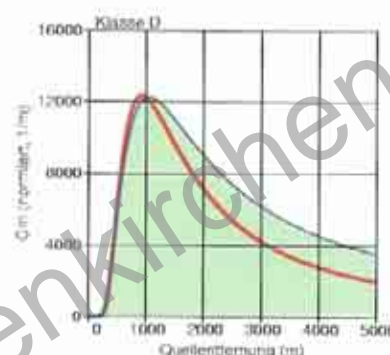
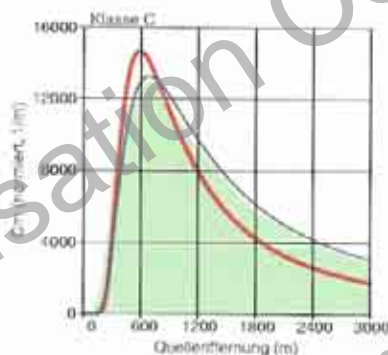
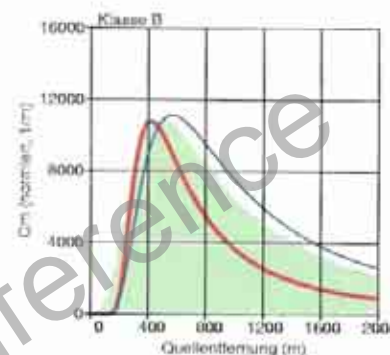
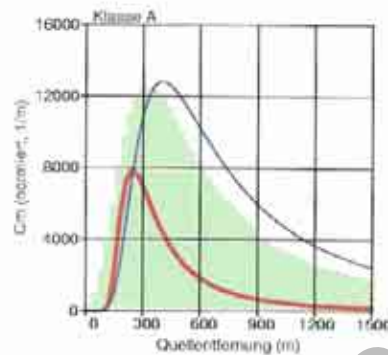
# Comparative consideration




## GM - LPM

[Janicke, 2001 a]

normalized  
maximum concentration

source height 100 m



-  Gauß
-  Lagrange
-  here not considered



# Comparative consideration

[Janicke, 2001 a]

## results:

- it is possible to reproduce GFM results with LPM
- single situation: don't use Gaussian model
- longterm computations: Gaussian model is good for plain terrain and lifted sources

# Comparative consideration

[Janicke, 2001 b]

## Gaussian model (AUSTAL 86) and Lagrangian model (AUSTAL 2000)

**basis:**

**statistic of stability class**

**1951 - 1969**

**source heights**

**100 m, (50 m) and 25 m**

**roughness lengths**

**1.5 m, 1.0 m and 0.5 m**

# Comparative consideration

[Janicke, 2001 b]

AUSTAL86

J \ I	14	15	16	17	18	19	20	21	22
22	14	17	22	30	36	34	30	28	26
21	14	17	22	30	39	37	34	32	29
20	16	18	21	26	33	34	37	35	28
19	20	22	22	15	10	21	32	30	26
18	23	26	27	11	0	8	25	27	24
17	20	23	24	20	10	16	23	24	22
16	17	20	23	25	26	23	22	20	18
15	16	18	21	23	25	22	20	18	16
14	15	16	18	20	21	19	17	15	14

AUSTAL2000,  $z_0 = 1.5$  m

J \ I	1	2	3	4	5	6	7	8	9
9	9	13	17	23	30	29	25	23	20
8	11	16	19	28	37	36	31	31	25
7	13	16	17	22	33	32	34	35	25
6	18	21	19	15	16	24	31	29	21
5	20	25	26	15	3	14	23	26	20
4	16	20	21	20	15	15	20	22	18
3	14	18	21	22	24	21	19	18	15
2	13	17	19	21	23	21	18	16	13
1	10	14	15	16	18	16	14	13	10



source height 100 m

AUSTAL2000,  $z_0 = 1.0$  m

J \ I	1	2	3	4	5	6	7	8	9
9	10	12	16	22	29	29	24	23	20
8	10	13	17	24	33	32	28	29	26
7	13	14	15	18	28	27	30	30	23
6	16	19	17	13	14	19	26	26	21
5	20	24	22	14	2	10	20	23	19
4	15	19	19	17	13	13	18	20	17
3	13	17	20	20	21	18	18	17	14
2	13	17	18	20	21	19	17	15	12
1	10	13	14	16	17	16	14	12	9

AUSTAL2000,  $z_0 = 0.5$  m

J \ I	1	2	3	4	5	6	7	8	9
9	10	12	16	20	27	25	21	20	20
8	10	12	15	20	26	26	22	25	25
7	11	13	12	15	21	21	24	26	21
6	16	17	14	10	11	14	19	21	18
5	19	21	21	13	1	9	16	19	19
4	16	17	17	16	11	11	14	17	16
3	12	15	17	18	18	16	15	14	14
2	12	15	16	17	18	17	15	14	12
1	10	14	14	16	17	15	13	11	10



# Comparative consideration

[Janicke, 2001 b]

source height 25 m

AUSTAL86

J \ I	0	1	2	3	4	5	6	7	8
8	22	27	35	47	55	49	39	33	29
7	24	30	40	58	75	63	50	42	34
6	29	34	44	70	110	87	68	49	35
5	37	45	54	75	146	128	79	48	34
4	43	55	77	102	0	102	70	46	33
3	38	46	58	81	93	75	54	39	29
2	31	39	49	59	65	53	41	31	24
1	29	35	40	43	45	39	32	26	21
0	26	29	31	33	34	31	26	22	19

AUSTAL2000,  $z_0 = 1.5$  m

J \ I	1	2	3	4	5	6	7	8	9
9	22	41	51	72	90	74	53	45	33
8	35	57	79	121	154	117	90	76	46
7	40	67	97	161	247	172	132	90	48
6	60	98	130	204	408	273	159	91	48
5	73	129	200	305	332	265	145	88	47
4	57	98	144	229	260	182	111	76	41
3	44	81	122	148	160	121	88	57	34
2	44	71	86	92	104	87	65	48	30
1	38	43	51	52	60	47	39	34	20

AUSTAL2000,  $z_0 = 1.0$  m

J \ I	1	2	3	4	5	6	7	8	9
9	31	43	55	76	94	82	56	47	36
8	37	56	73	110	143	115	87	78	56
7	44	63	87	132	196	146	121	93	53
6	61	88	103	131	242	206	139	87	50
5	80	118	161	175	75	167	122	85	50
4	60	89	113	148	157	126	97	71	46
3	50	77	106	116	124	100	75	55	36
2	45	73	79	84	89	75	63	49	29
1	41	48	51	55	61	53	44	35	28

AUSTAL2000,  $z_0 = 0.5$  m

J \ I	1	2	3	4	5	6	7	8	9
9	28	36	44	61	76	70	55	46	39
8	30	36	49	73	102	86	66	63	52
7	32	42	50	79	124	98	89	73	48
6	48	56	57	61	105	116	92	60	44
5	52	73	85	76	14	76	77	59	42
4	40	52	61	75	68	63	62	51	40
3	32	48	61	67	73	60	52	41	30
2	34	47	50	51	57	50	45	37	30
1	33	38	38	44	42	38	34	31	27

9th Harmonisation Conference  
Garmisch-Partenkirchen

# Comparative consideration

[Janicke, 2001 b]

## results:

- at source height 100 m: relative good similarity
- differences between GM and LPM increase with smaller source height
- single situations: partial considerable differences ( $z_0$  !)

# Comparative consideration

[Thehos et al, 1994]

## Gaussian model (TA Luft) and air flow / Lagrangian model FITNAH / LPDM

basis:

statistic

1944 single situations / 150 Cluster

source heights

75 m (computed with raised plume)

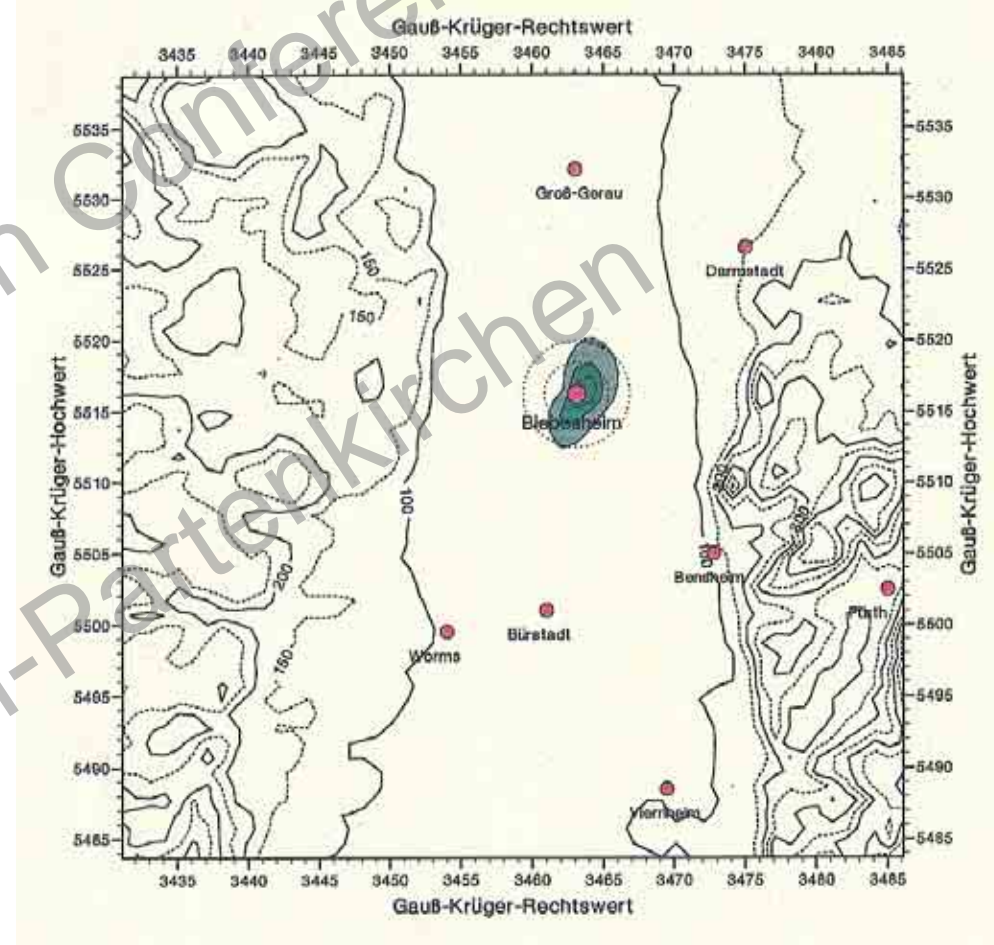
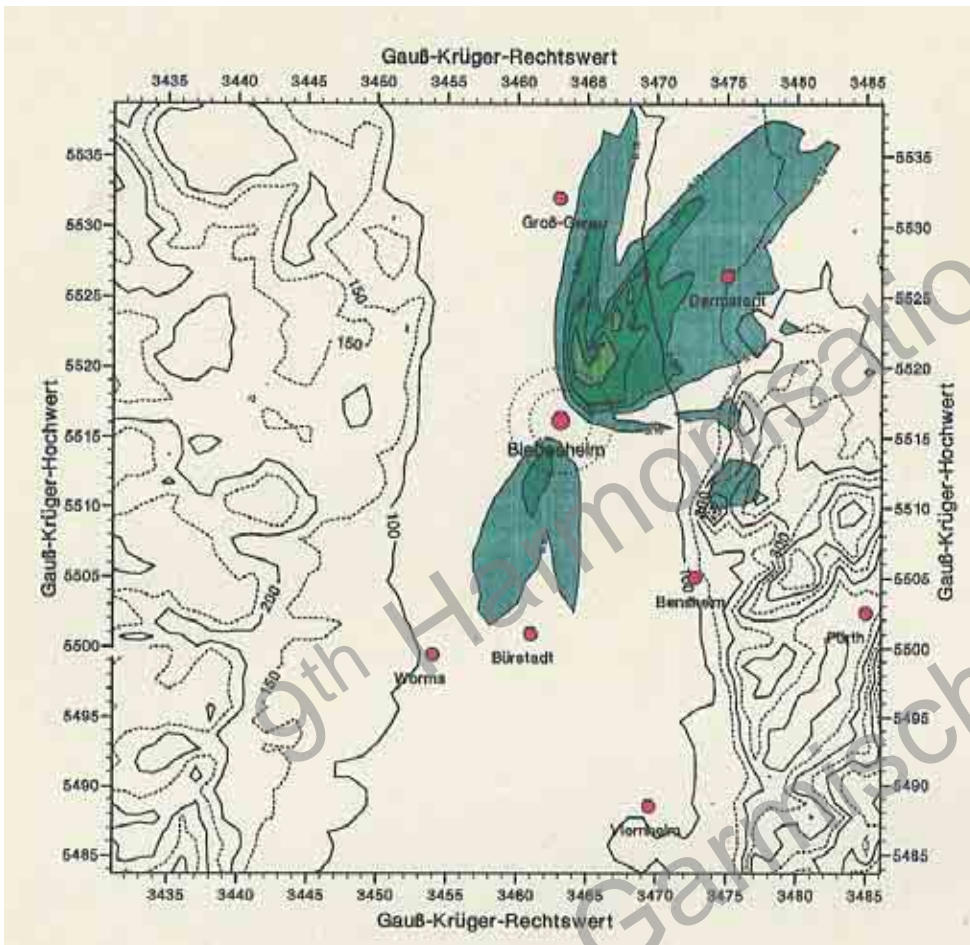
areas

Biebesheim, Kassel (cities in Germany)



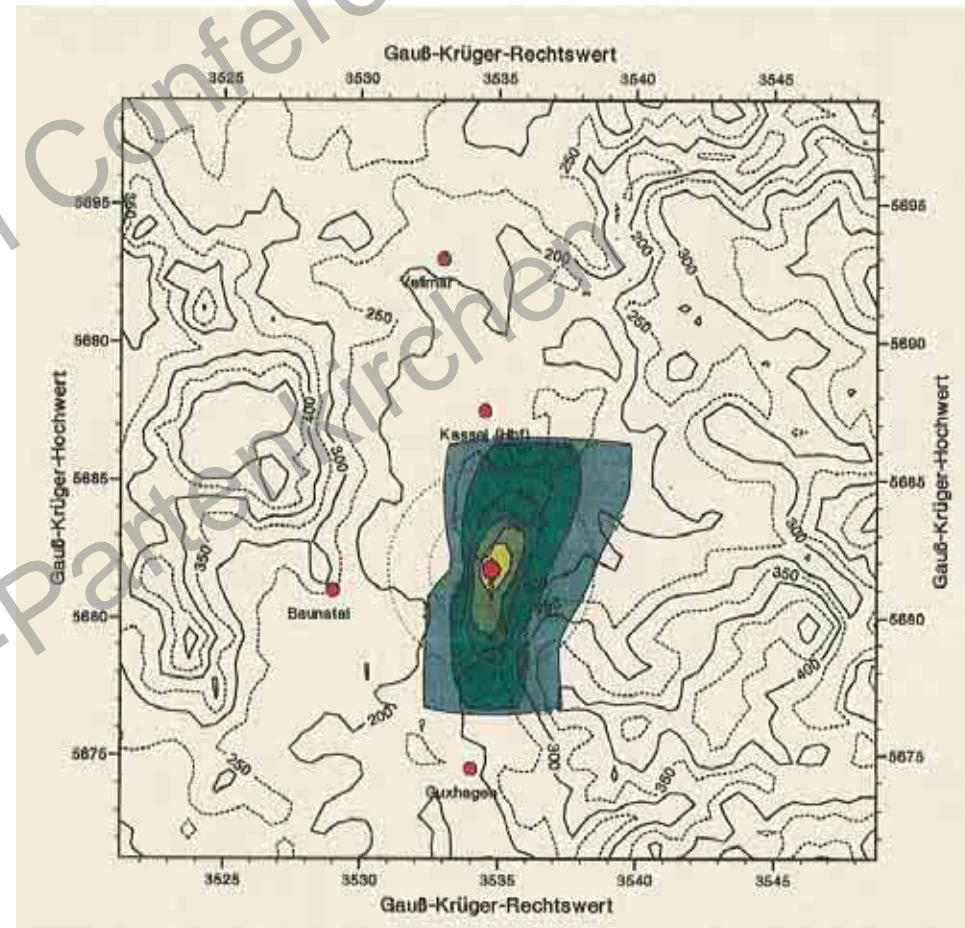
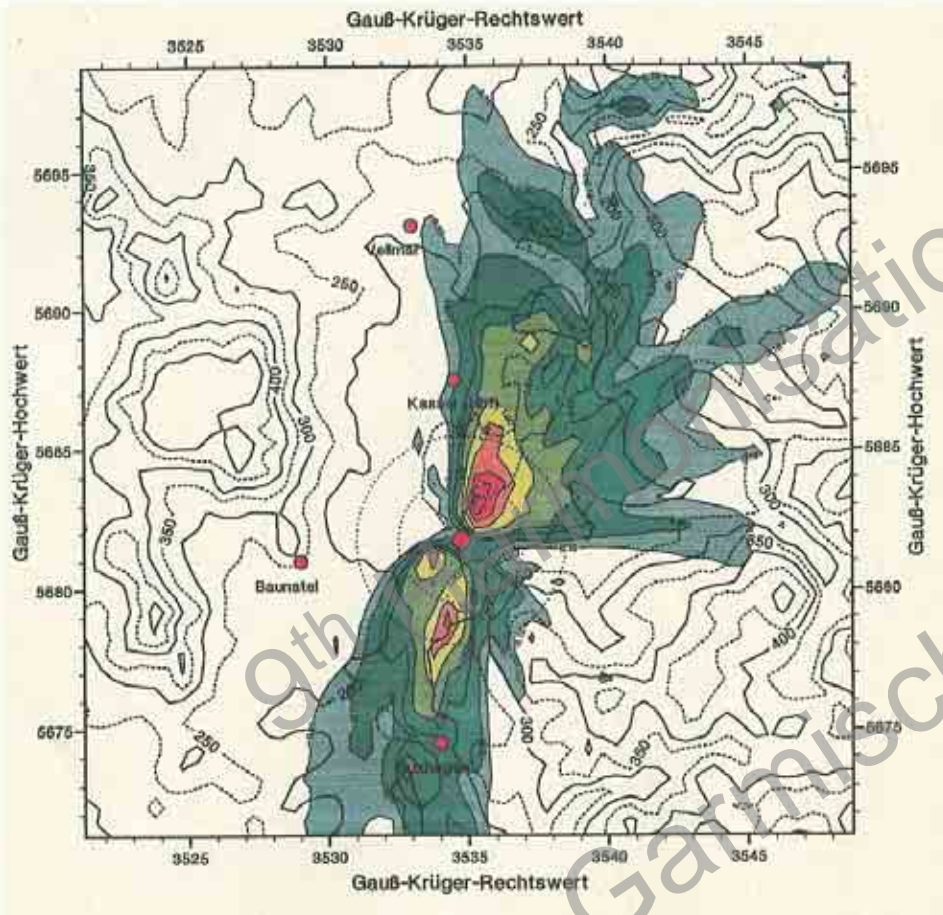
# Comparative consideration [Thehos et al, 1994]

direct comparison homogeneous orography



# Comparative consideration [Thehos et al, 1994]

direct comparison structured orography





# Comparative consideration [Thehos et al, 1994]

## results:

- **plain:** height of maximum complies good;  
position of maximum at LPM farther
- **not plain:** great differences

# Summary of the literature study

- **Gaussian models have partially severe constraints that can not be solved generally**
- **Gaussian models show especially deficits in situations with**
  - **instationarity (windfield, source)**
  - **orography**
  - **sources with low height**
- **Lagrangian models have greater significance because of their stronger physical contents**
- **Lagrangian models have been introduced in dispersion calculations in Germany for conventional pollutants**

# Summary

**recommendation:**

**further examination of the  
introduction of Lagrangian models  
in regulation guidelines for radioactive pollutants  
in Germany**

