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# **Effect of Unstable Thermal Stratification on the Atmospheric Boundary Layer above Urban Street Canyons by Large-Eddy Simulation**

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**Parallel Session 8**

**Urban Scale and Street Canyon Modelling: Meteorology and Air Quality**



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# Introduction

- For high-Reynolds-number (Re) flows above idealized homogeneous surface, the wind profile can be described by the law of the wall (Spalding 1962)

- Wall units ( $u^+$ ,  $z^+$ ) were suggested to normalize the velocity ( $u$ ) and wall distance ( $z$ ) as

$$u^+ = \frac{u}{u_*} \quad z^+ = z \frac{u_*}{\nu}$$

- Near the wall, three characteristic layers of the wind profiles are suggested
  - Laminar sublayer,
  - Buffer layer, and
  - Log-law region

- In the laminar sublayer (approximately  $z^+ < 5$ ), the velocity is directly proportional to the wall distance as

$$u^+ = z^+$$

- In the log-law region (approximately  $z^+ > 30$ ),

$$u^+ = A_u \ln(z^+) + B_u$$

- $A_u$  and  $B_u$  are constants
- In the buffer region, the velocity profile exhibits a behavior between those in the laminar sublayer and the log-law region

- Similarly, the temperature profile can be approximated by the logarithmic form as

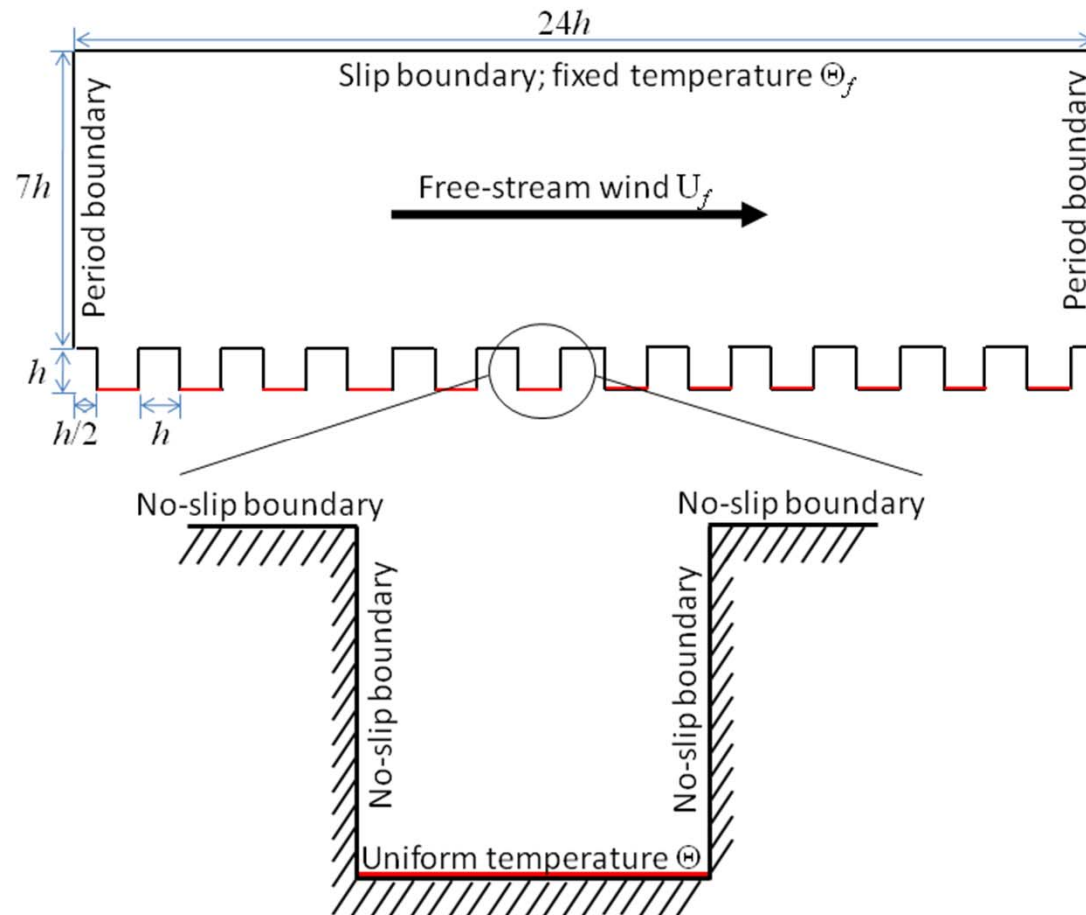
$$\theta^+ = A_\theta \ln(z^+) + B_\theta$$

- where  $\theta^+$  ( $=\theta/\theta_*$ ) is the temperature in wall unit with  $\theta_* = (\partial\theta/\partial z|_{\text{wall}}/u_*)$  the friction temperature, and  $A_\theta$  and  $B_\theta$  are constants
- In this study, we investigate how the log profiles of wind and temperature above urban street canyon change with unstable thermal stratifications

# Methodology

- Large-eddy simulation (LES) using open-source CFD code OpenFOAM (OpenFOAM 2011)
- One-equation subgrid-scale (SGS) model (Schuman 1975)

- The domain dimensions are  $24h \times 5h \times 8h$ . Twelve identical street canyons are considered in order to capture the large-scale turbulence over the buildings in the urban atmospheric boundary layer.

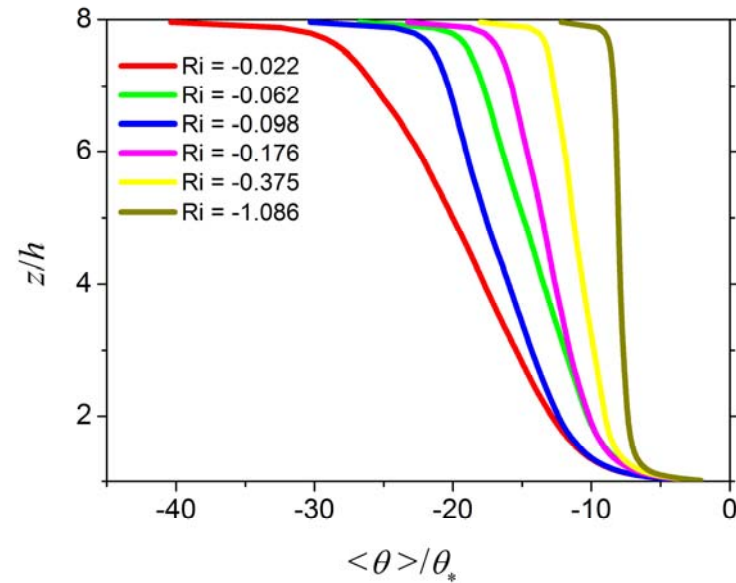
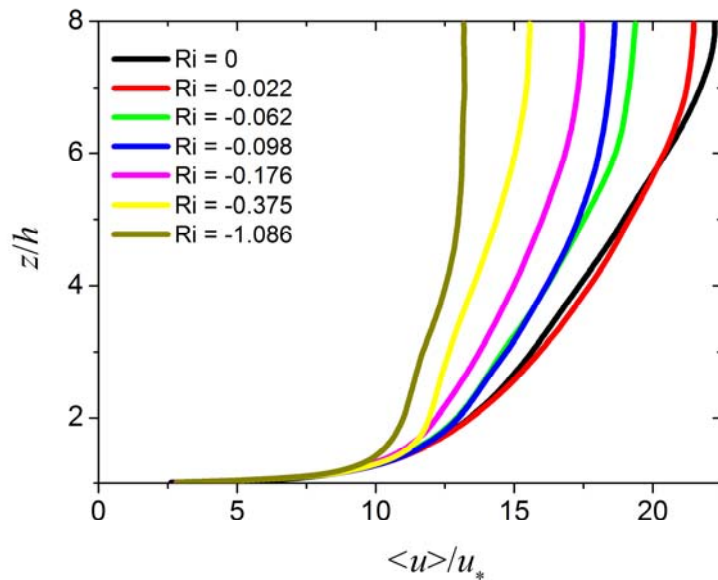


- $Re (= U_f h / \nu)$  is about 10,000
- Richardson number
  - $Ri (= \alpha g L (\Theta - \Theta_f) / U_f^2)$  is equal to 0, -0.022, -0.062, -0.098, 0.176, -0.375, and -1.086
- LES domain is discretized into 2.4 million of brick elements with grid spacing  $1.4 \times 10^{-2} h$  and  $4 \times 10^{-1} h$  at the bottom and top boundaries, respectively
- After  $200h/U_f$  of transient calculation, the results are ensemble averaged (denoted by  $\langle \bullet \rangle$ ) using another  $200h/U_f$  of LES data at time interval  $0.1h/U_f$
- Detailed model validation and comparison were reported in Cheng and Liu (2011a) and (b).

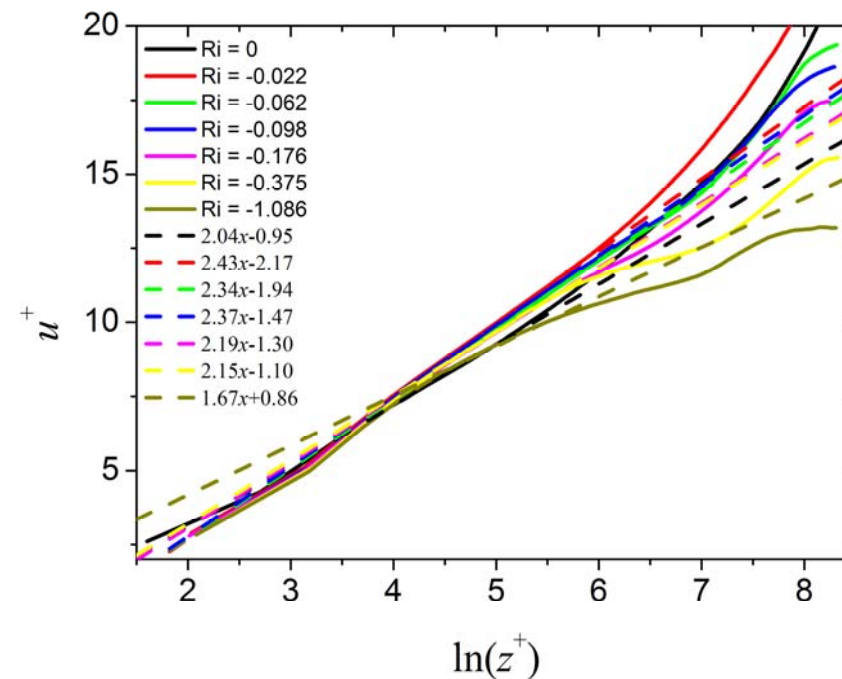


# Results and Discussion

- Substantially modifications in the vertical profiles of wind and temperature above the street canyons at different Ri are observed

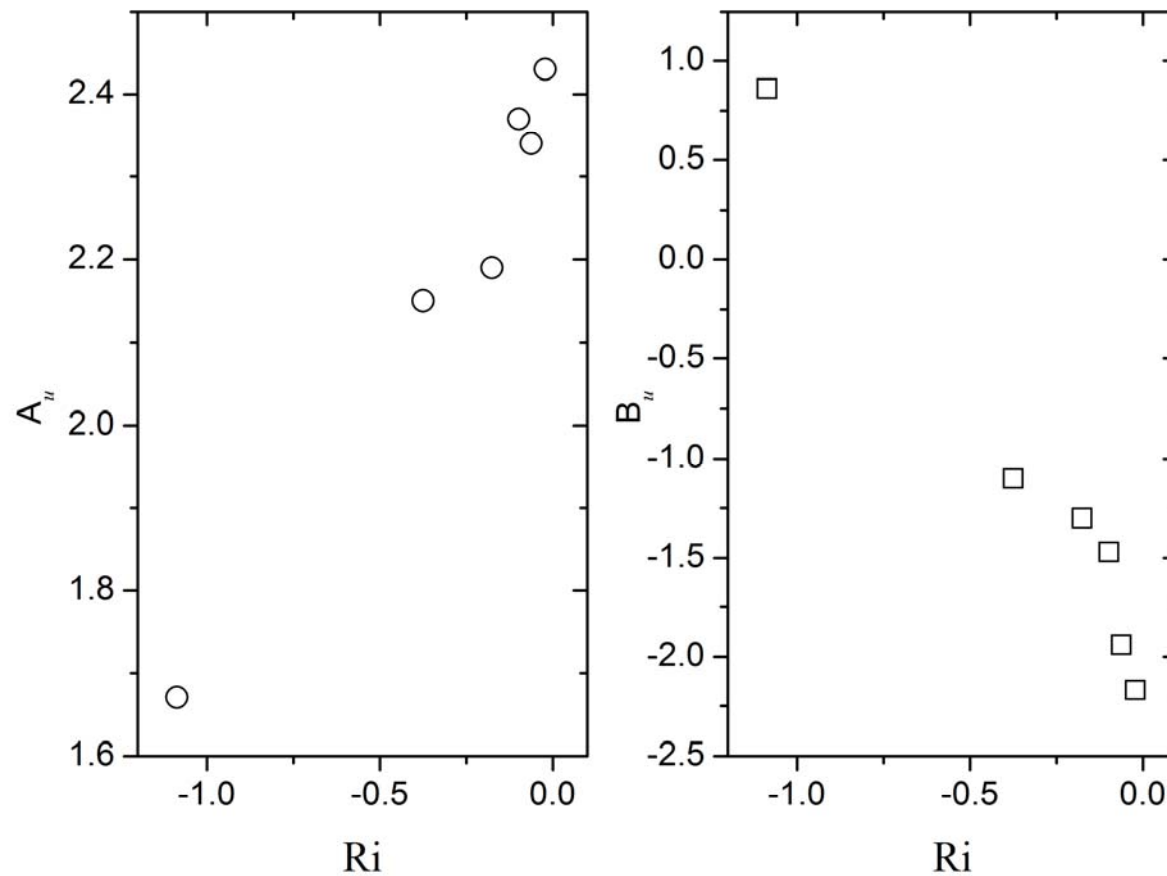


- Velocity in wall unit ( $u^+$ ) against  $z^+$  at different Ri
- Boundary layer is in fact developed over the street canyons therefore vertical displacement height of  $h$  is employed
- The slope of the curves in general decreases with decreasing Ri. The profiles fall onto a straight line at  $50 < z^+ < 300$ , which correspond to the logarithmic profile

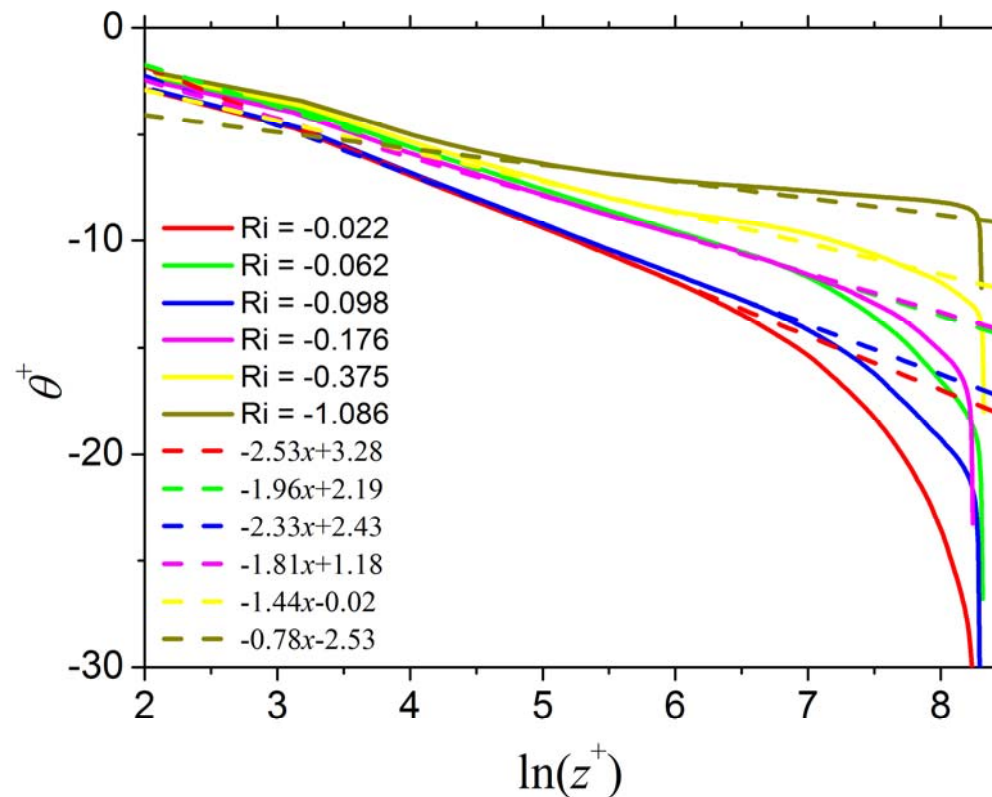


- As  $Ri$  increases from -1 to 0,  $A_u$  increases from 1.7 to 2.4 while  $B_u$  decreases from 0.7 to -2.2.

$$u^+ = A_u \ln(z^+) + B_u$$

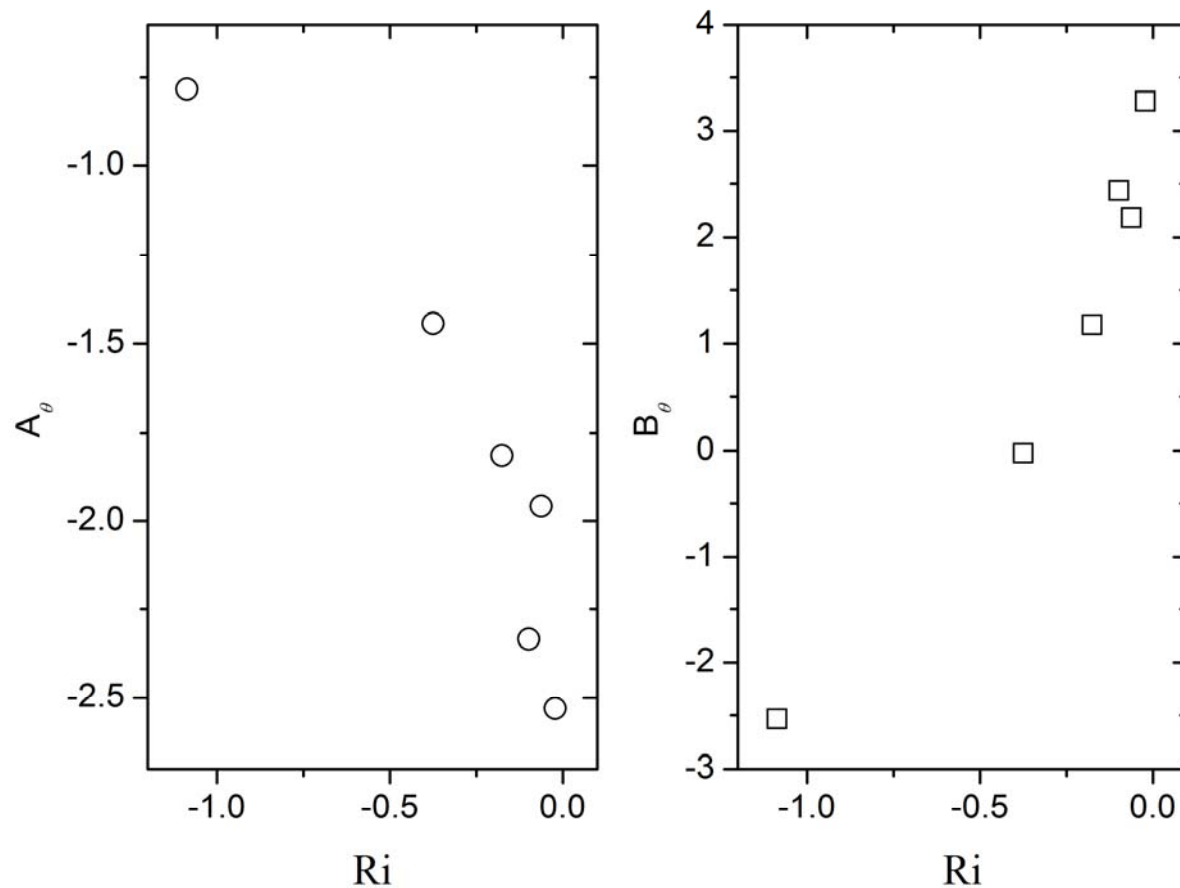


- Temperature ( $\theta^+$ ) against  $\ln(z^+)$
- The slope of the curves increases with decreasing Ri that become less negative
- Good least-square fittings are obtained in the range about  $150 < z^+ < 300$



- Moving toward neutral stratification for increasing Ri from -1 to 0, the values of  $A_\theta$  decrease from -0.8 to -2.5 while the values of  $B_\theta$  increase from -2.5 to 3.

$$\theta^+ = A_\theta \ln(z^+) + B_\theta$$



# Conclusion

- Seven sets of LES are performed to investigate the effect of unstable thermal stratifications on the behaviours of wind and temperature above idealized 2D urban street canyons
- The wind and temperature profiles in unstable stratification can be described by logarithmic profiles in which the slope and  $y$ -intercept are functions of thermal stratification
- As  $Ri$  decreases from 0 to -1 (more unstable),  $A_u$  and  $B_\theta$  decrease while  $A_\theta$  and  $B_u$  increase
- Changes in  $A_u$  and  $A_\theta$  are due to the enhanced momentum exchange and heat transfer in the turbulent boundary layer

# References

- W. C., Cheng and C.-H., Liu, 2011a: Large-eddy simulation of flow and pollutant transports in and above two-dimensional idealized street canyons. *Boundary-Layer Meteorol.*, **129**, 411-437.
- W. C., Cheng and C.-H., Liu, 2011b: Large-eddy simulation of turbulent transports in urban street canyons in different thermal stabilities. *J. Wind. Eng. Ind. Aerodyn.*, **99**, 434-442.
- OpenFOAM 2011: <http://www.opencfd.co.uk/openfoam/>.
- U., Schumann 1975: Subgrid scale model for finite difference simulations of turbulent flows in plane channels and annuli. *J. Comput. Phys.*, **18**: 376-404.
- D. B., Spalding 1962: A new analytical expression for the drag of a flat plane valid for both the turbulent and laminar regimes. *Int. J. Heat Mass Transf.*, **5**, 1133-1138.