



MINISTÈRE DE LA DÉFENSE

# METHODOLOGY FOR STATISTICAL EVALUATION OF ATMOSPHERIC DISPERSION MODELS IN A RISK ASSESSMENT CONTEXT

Bertrand Sapolin<sup>1</sup>, Gilles Bergametti<sup>2</sup>, Philippe Bouteilloux<sup>1</sup>, Alain Dutot<sup>2</sup>

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Atmospheric Dispersion Modelling for Regulatory Purposes*



DIRECTION GÉNÉRALE DE L'ARMEMENT

<sup>1</sup> DGA Maîtrise NRBC, Vert-le-Petit, France

<sup>2</sup> Laboratoire Interuniversitaire des Systèmes  
Atmosphériques (LISA), Créteil, France



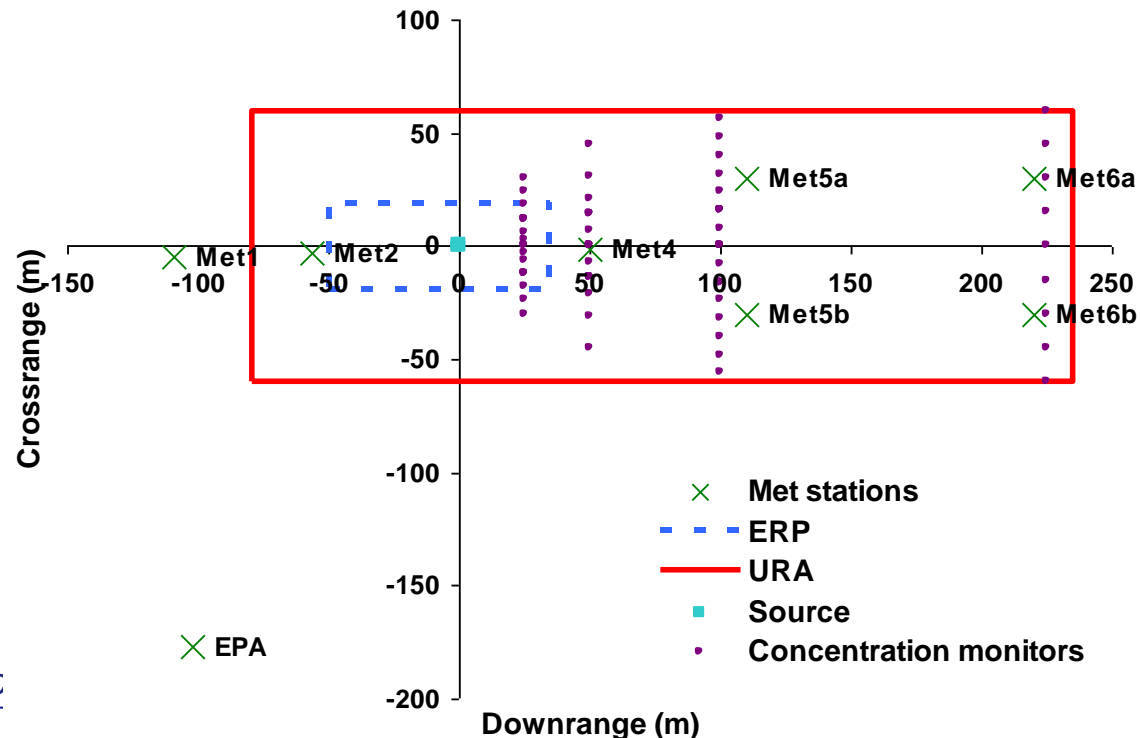
# Background

- Chemical, Biological, Radiological (CBR) risk assessment
  - Evaluate potential consequences of accidental or deliberate releases of toxic substances into the atmosphere
  - Use transport and dispersion models
  - Output: predicted effect on the population
- Scenarios
  - Short term releases
  - Non-stationary transport and diffusion
  - Acute inhalation toxicity
- Focus of the study:
  - Statistical evaluation against experimental data
    - Kit Fox: representative of risk assessment scenarios interesting the French MoD
    - Model: HPAC
  - Chemical risk assessment



# Experimental data: Kit Fox

- US DoE Nevada Test Site
- Flat desert area artificially roughened
  - URA (Uniform Roughness Array):  $z_0 \sim 0.02\text{m}$
  - ERP (Equivalent Roughness Pattern):  $z_0 \sim 0.2\text{m}$
- 52 dense gas  $\text{CO}_2$  releases
  - ERP&URA: 13 instantaneous, 6 continuous
  - URA alone: 21 instantaneous, 12 continuous
- 77 concentration samplers
  - 4 downwind distances: 25, 50, 100, 225m
  - Time resolution: 1s
- Met data
  - Local met stations
  - Time resolution: 1-10s
  - Neutral to stable conditions



# Dispersion model

- HPAC (US DTRA)
  - Dispersion: SCIPUFF (Lagrangian Puff Model)
  - Version 4.04 SP4
- Kit Fox simulations
  - URA/ERP: 42x42 grid cells
  - Modelling domain: 420x420m
  - Source term: stack release (stack height = 0m)
  - Met data: all stations and vertical levels, 20s averaging time
  - Concentration output time step: 1s
- Note
  - Same configuration for the 52 trials (no “case by case adjustment”)
  - The purpose is not to evaluate model performance but rather use the evaluation results to investigate new methodologies for model evaluation



# Comparison HPAC / Kit Fox with the MVK

- Model Validation Kit (MVK) protocol: arc max concentrations
- Example of results (FAC2 with 95% confidence intervals)

		Instantaneous concentration	20s moving average concentration
Block results	ERP puff	63.5 [49-76.4]	50 [35.8-64.2]
	ERP continuous	54.2 [32.8-74.4]	45.8 [22.1-63.4]
	URA puff	65.5 [54.3-75.5]	66.7 [55.5-76.6]
	URA continuous	45.8 [29.5-58.8]	41.7 [27.6-56.8]
Overall results		<b>59.2 [52.1-65.9]</b>	<b>54.3 [46.8-60.8]</b>

- MVK protocol:
  - Arc max value not appropriate => risk assessment more interested in values on the borders of toxic clouds
  - Concentration cannot be directly related to toxic effect

=> Need for a risk oriented evaluation methodology



# Guidelines for a risk oriented evaluation methodology



# Effect-related variables (1/3)

- Acute inhalation toxicity is a non linear function of concentration ( $C$ ) and time ( $t$ )

- Dosage:

$$d \mathbf{C} = \int_0^t \mathbf{C} d\xi$$

- Toxic load  $TL$ :

$$TL \mathbf{C} = \int_0^t \mathbf{C}^n d\xi$$

- Exponent  $n$  depends on the toxic substance

- Toxicological law: a given effect on an individual is reached by a fixed value of toxic load:

$$TL(t) = k \quad (eq. 1)$$

- Variability of population response to a given  $TL$

- Level  $k$  has a statistical meaning
- Statistical distribution of population response is usually lognormal
- *eq. 1* can be extended to a Cumulative Distribution Function of the population response

$$\Phi(TL) = \frac{1}{2} \left[ 1 + \operatorname{erf} \left( \frac{a \cdot \ln(TL) + b}{\sqrt{2}} \right) \right] \quad a, b: \text{constants associated to the toxic agent}$$

**Fraction of the population suffering adverse effect as a function of toxic load**



# Effect-related variables (2/3)

## •Remarks

- Effect-related variables are built from concentration time series (observed / predicted)
- Model performance depends on the substance

## •Choice of substances

- Risk assessment: numerous substances covering a large toxicity range
- Impossible to test all of them => choose representative substances
  - Toxicity range cut into 4 classes: low, moderate, high & very high toxicity
  - Criterion: AEGL-3 thresholds, exposure time = 10min
  - 1 representative substance in each class

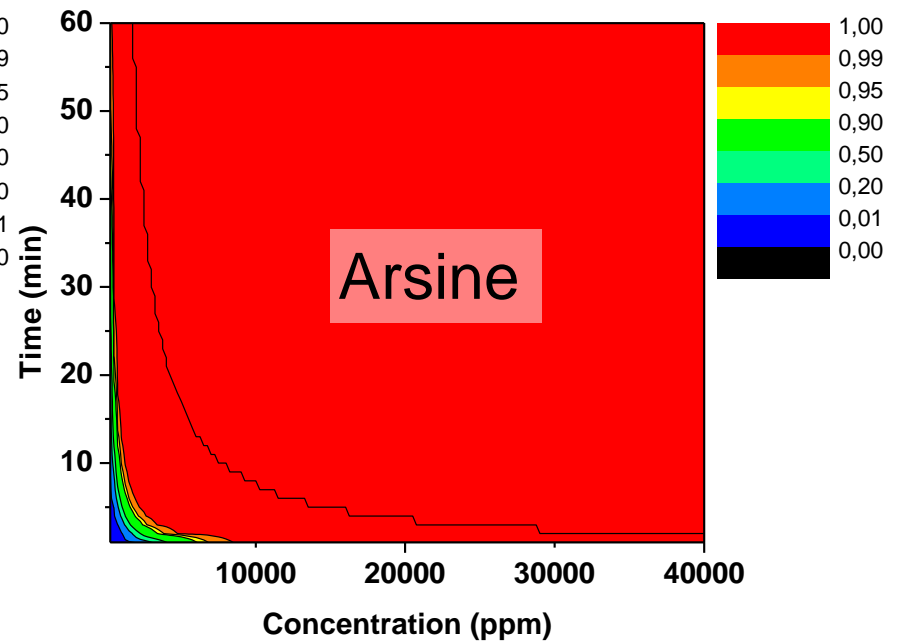
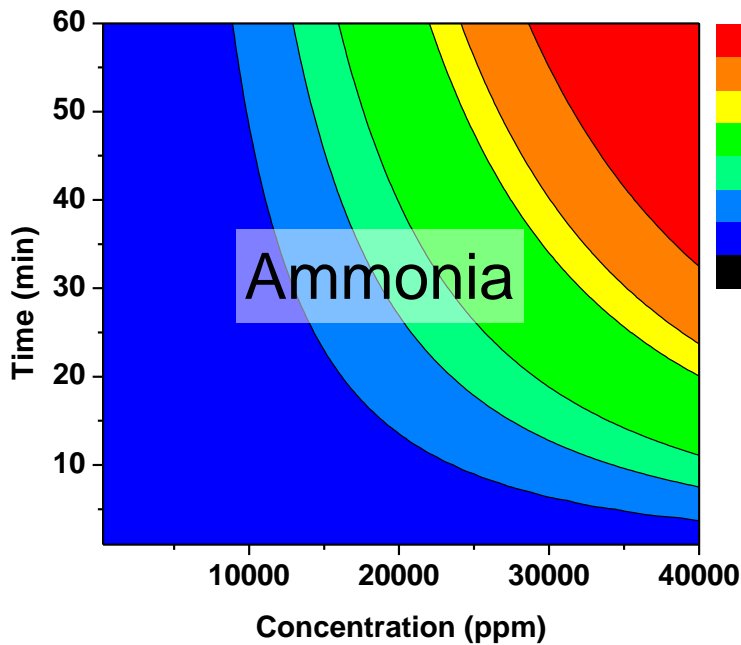
Classes			Benchmark agents			
Rank	Toxicity	AEGL-3 10 min range (mg/m <sup>3</sup> )	Agent name	Probit parameters ( <i>C</i> in ppm, <i>t</i> in min)		
				<i>a</i>	<i>b</i>	<i>n</i>
I	Low	AEGL-3>500	Ammonia NH <sub>3</sub>	2.17	-47.4	1.83
II	Moderate	50<AEGL-3<500	Hydrogen fluoride HF	2.63	-29.9	1
III	High	5<AEGL-3<50	Phosphine PH <sub>3</sub>	16.81	-120.89	0.5
IV	Very high	AEGL-3<5	Arsine AsH <sub>3</sub>	2.65	-26.08	1.18





# Effect-related variables (3/3)

- Compared toxicity
  - Class I: ammonia (“low” toxicity)
  - Class IV: arsine (very high toxicity)
- Fraction of fatalities as a function of concentration and exposure duration





# Comparisons based on effect-related variables

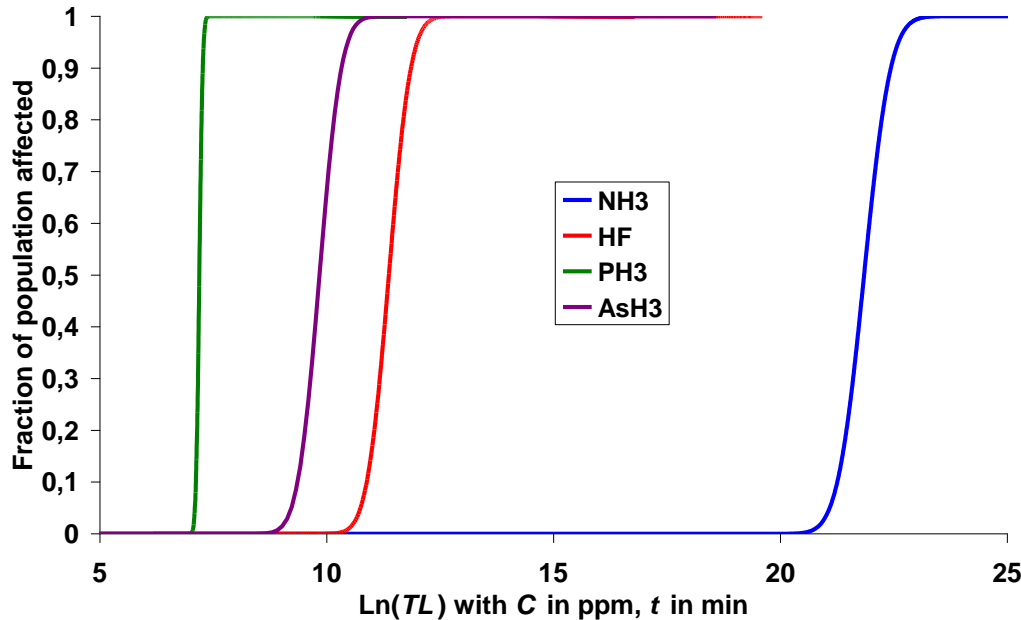
- Point to point comparisons
- Variables: dosage, toxic load
- Results (FAC2)

		$C_t$	$C^n_t$			
			$NH_3$	HF	$PH_3$	$AsH_3$
Block results	ERP puff	21.1[18.2-24]	13.8[11.4-16.4]	21.6[18.6-24.6]	33.9[30.4-37.4]	19.2[16.4-22.1]
	ERP cont.	22.9[18.7-27.1]	13.1[9.7-16.6]	23.3[19.2-27.8]	34.9[30.1-39.8]	22[17.8-26.2]
	URA puff	29.5[26.6-32.5]	18.3[15.8-21]	30.4[27.4-33.5]	55[51.4-58.3]	26.1[23.2-29]
	URA cont.	35.5[32-39.1]	20.4[17.4-23.4]	36[32.5-39.6]	61.2[57.3-64.7]	29.9[26.5-33.3]
Overall results		<b>27.8[26.1-29.5]</b>	<b>16.9[15.5-18.3]</b>	<b>28.4[26.7-30.1]</b>	<b>47.8[45.9-49.7]</b>	<b>24.6[23-26.2]</b>

- Poor performance
  - Point to point comparisons
  - $n > 1$  gives more weight to the uncertain variable => FAC2 decreases as  $n$  increases

# Suggested use of effect-related variables (1/3)

## Population response = $f(\text{toxic load})$



- Same pattern for all the substances
  - A plateau “nobody affected”
  - A plateau “everybody affected”
  - A narrow sloping part
- A same measure / prediction difference does not have the same impact whether the difference covers or not the sloping part of the response curve
- Large measure / prediction differences in the steady parts are unimportant

## TL95% / TL05%

Agent	$r = TL95\%/TL05\% = C95\%/C05\%$
NH <sub>3</sub>	<b>2.29</b>
HF	<b>3.48</b>
PH <sub>3</sub>	<b>1.47</b>
AsH <sub>3</sub>	<b>2.85</b>

- Population response increases only on a very narrow range of toxic load
- $r$  small  $\Rightarrow$  FAC2 inappropriate
- Non linear population response  $\Rightarrow$  criteria emphasizing amplitude of model errors are inappropriate (FB, NMSE...)



# Suggested use of effect-related variables (2/3)

## ● Suggestion

- **Compare fractions of population affected instead of toxic load**
- Choose an incidence level & count the monitors where this level is exceeded
- Event = the fixed incidence level is exceeded
- Contingency table

Event predicted? \ Event observed?	Yes	No	Total
Yes	A	D	A+D
No	C	B	C+B
Total	A+C	D+B	N = A+B+C+D

## ● Criteria

- False positive rate  $R_{fp} = \frac{D}{D+B}$
- False negative rate  $R_{fn} = \frac{C}{A+C}$
- Detection rate  $R_d = \frac{A}{A+C}$
- Good analysis rate  $R_{ga} = \frac{A+B}{N}$
- Bad analysis rate  $R_{ba} = \frac{C+D}{N}$

## ● Similarity with the Measures of Effectiveness (MOE, Warner, Platt et al 2001)

$$MOE1 = \frac{A_{ov}}{A_{ov} + C_{FN}A_{FN} + C_{FP}A_{FP}} = \frac{A}{A + C_{FN}C + C_{FP}D}$$



# Suggested use of effect-related variables (3/3)

- Results

- Detection rates > 70%
- False negative rates < 30%
- False positive rates < 20%
- Good analysis rates > 75%
- Bad analysis rates < 25%

Agent	$R_d$	$R_{fn}$	$R_{fp}$	$R_{ga}$	$R_{ba}$
NH <sub>3</sub>	n.s.	n.s.	n.s.	n.s.	n.s.
HF	82%	18%	6%	93%	7%
PH <sub>3</sub>	80%	20%	17%	98%	2%
AsH <sub>3</sub>	72%	28%	19%	79%	21%

*HPAC vs 52 Kit Fox trials – n.s.: not significant*

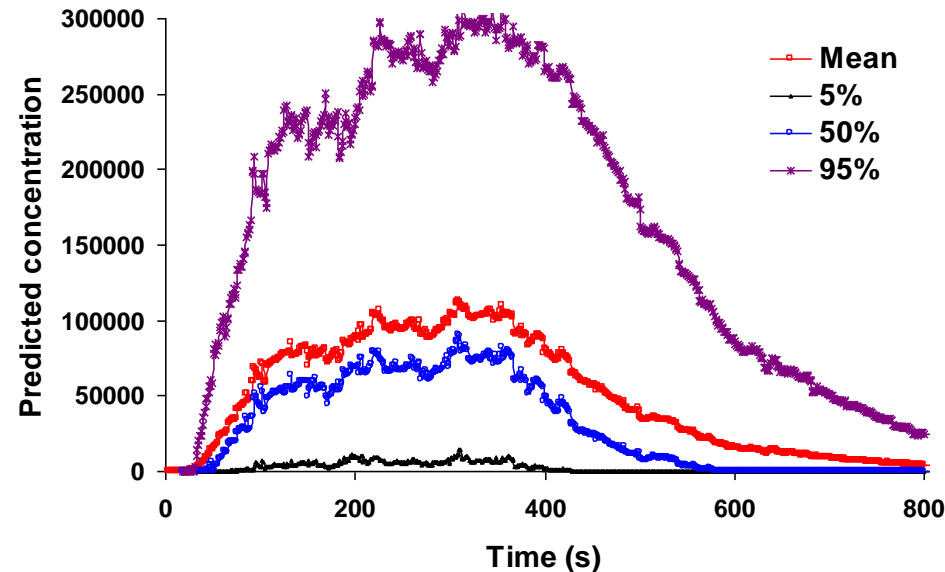
- Analysis

- Better results
- Suggested methodology
  - Focus on the end-user variable of interest (evaluation objective = risk assessment)
  - Measured / predicted toxic load differences without impact on the population response do not penalize the model



# Concentration fluctuations (1/3)

- The suggested methodology has been applied to ensemble average model results.
- The methodology could be extended to include inherent uncertainties
  - Model result  $\neq$  measure
  - Model result = ensemble average, measure = one realization of the ensemble => part of measure / prediction discrepancies may not be ascribed to the model
  - Need for a model able to predict inherent uncertainties
- SCIPUFF
  - Mean concentration + variance of fluctuation + integral timescale for concentration fluctuations (autocorrelation)
  - Theoretical distribution for concentration (clipped normal, left-shifted and clipped gamma...)
  - => uncertainties in the concentration time series



*SCIPUFF: time series of concentration distribution (left-shifted and clipped gamma model)*



# Concentration fluctuations (2/3)

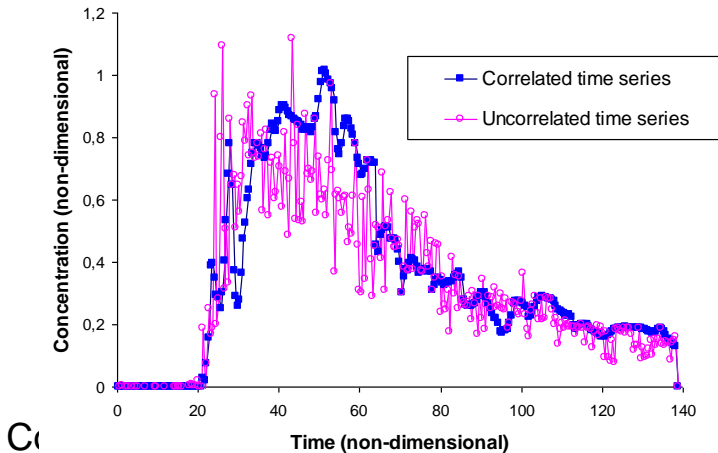
- Suggestion
  - 1) Use SCIPUFF to build modelled distributions of toxic load
  - 2) Compare the modelled distributions to measures
- How to build modelled toxic load distributions?
  - Generate many synthetic concentration time series from SCIPUFF results
  - For each time series, calculate toxic load
  - Build empirical toxic load distribution
- How to generate synthetic time series?
  - Sampling one concentration value at each time step produces uncorrelated time series
  - In reality, time series are correlated
  - Is it a conservative assumption to build toxic load distributions without considering time correlations?



# Concentration fluctuations (3/3)

## ● Wind tunnel experiments (Hall et al, 2000)

- Several repeats of instantaneous gas release
- Concentration time series measured at several locations
- At each location, measured time series (correlated) were used to calculate “natural” mean & variance of toxic load
- Time series were then artificially decorrelated and used to calculate “artificial” mean & variance of toxic load



	Correlated ("natural")	Uncorrelated ("artificial")
Mean	45.34 [43.04-47.63]	45.34 [44.9-45.78]
Standard deviation	$s_1 = 3.21$ [2.2-5.85]	$s_2 = 0.62$ [0.42-1.13]
<i>Null hypothesis <math>s_1=s_2</math> rejected at the 5% significance level</i>		

*Toxic load distribution (toxic load exponent =1), using correlated or uncorrelated time series*

## ● Conclusion

- Ignoring time series correlations amounts to
  - underestimating statistical variance of toxic load
  - underestimating upper percentiles of toxic load => not a conservative error
- => **Synthetic time series must include autocorrelations**





# Conclusion

- Risk-oriented methodology
  - Effect-related variables: toxic load + response distribution => fraction of population affected
  - Compare fraction of population instead of toxic load => release some useless constraints in model evaluation
  - Point to point comparisons
  - Contour thresholds
- Future work: extend the methodology to include inherent uncertainties
  - Develop a method to build statistical distribution of toxic load / population response
  - The methodology could be applied to probabilistic models (first & second moments of concentration distribution)