



CENTRE EUROPÉEN DE RECHERCHE ET DE FORMATION AVANCÉE EN **CALCUL SCIENTIFIQUE**



COMPOUND PARAMETRIC METAMODELLING OF LARGE-EDDY SIMULATIONS FOR MICROSCALE ATMOSPHERIC DISPERSION

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Microscale air pollutant atmospheric dispersion

Scientific challenges for microscale flow dynamics and plume dispersion

Microscale

- Evolution in a complex geometry (*urban canopy*)
- Highly dependent to near-source behaviour

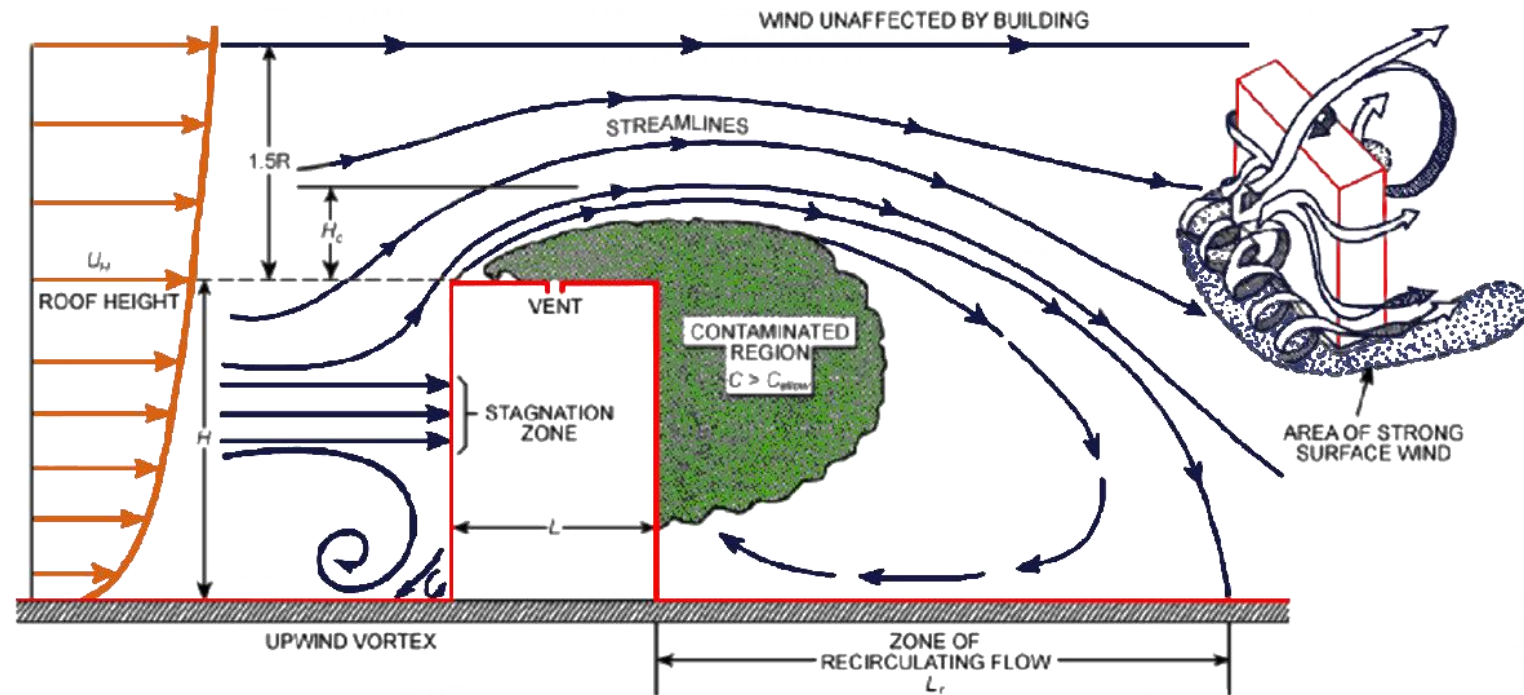
Meso to microscale

- Multiscale problem (*large-scale wind forcing, turbulence, boundary layers*)

Need for a stochastic approach...

Uncertainties are not accounted for by CFD models

- Mean wind and fluctuations
- Emission source location, type of pollutant, etc.

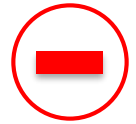


Tominaga and Stathopoulos (2013)

Large-eddy-simulations (LES)



- Can well represent complex flow features in canopies/behind obstacles
- Explicitly represent most of the eddies



- Very costly (60 000 hCPU for MUST¹ trial)
- Ensemble/uncertainties



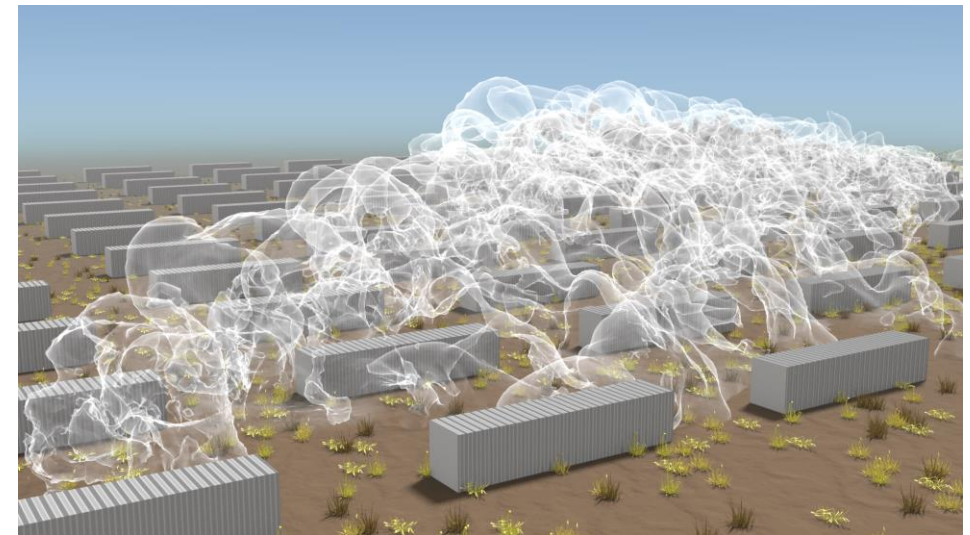
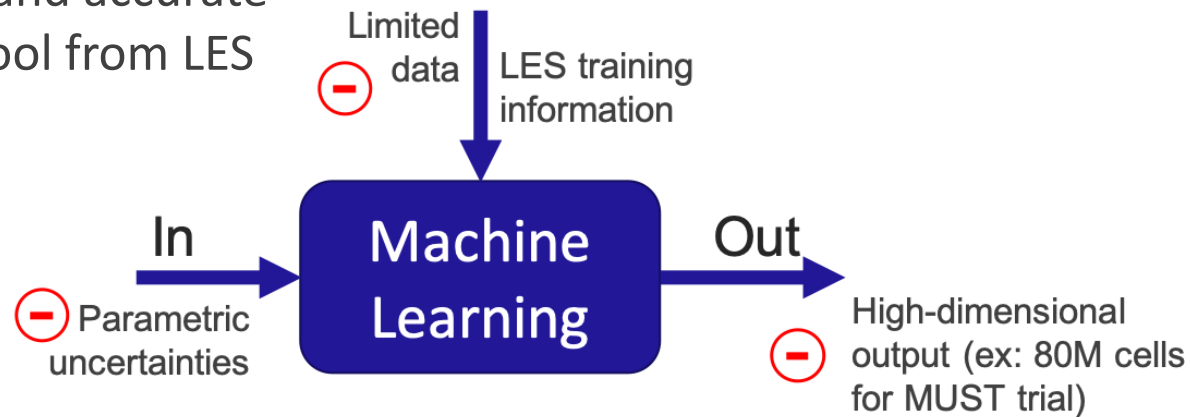
AVBP

- Compressible Navier-Stokes equations on unstructured meshes (*artificial compressibility approach for low-Mach flows*)
- Proven on many application cases (ex: aeronautical industrial applications) and evaluated for environmental flows



Objective

Build a fast and accurate predictive tool from LES information



Artist's view of the MUST case



What is the most suitable machine learning metamodel for the LES microscale?

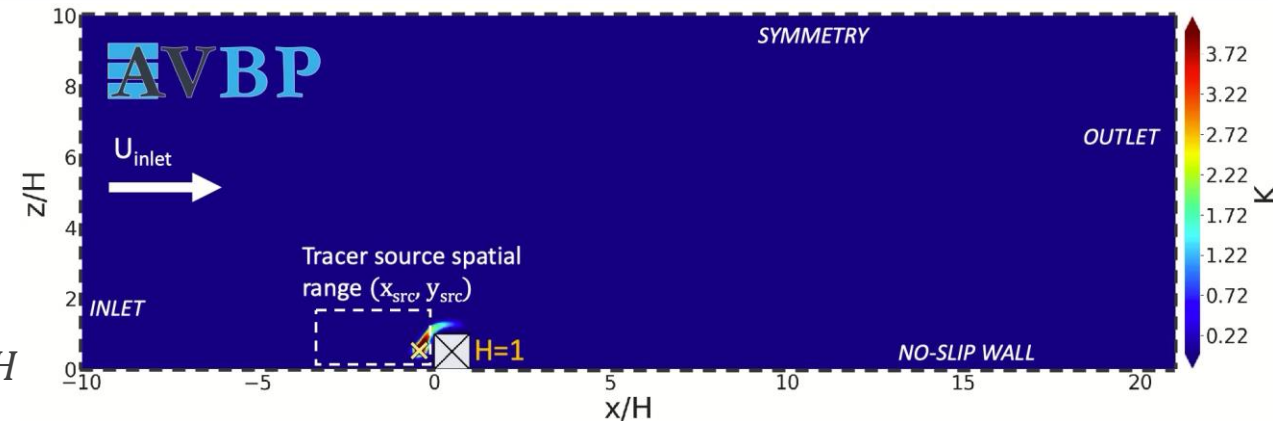
Outline

- ❖ Definition of the test case
- ❖ Metamodelling approach
- ❖ Results



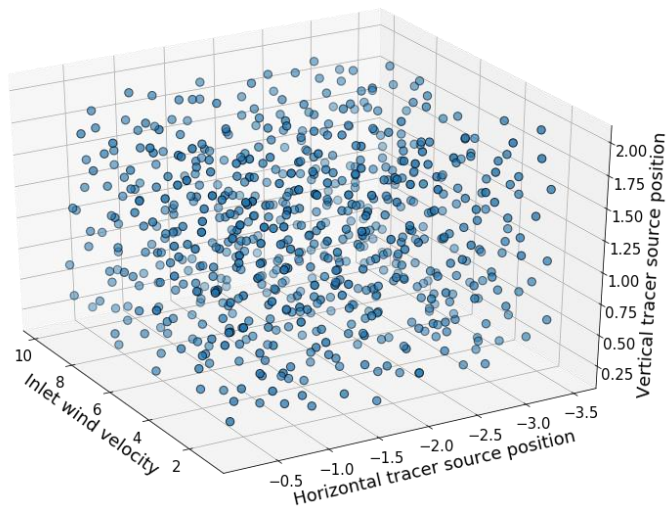
2-D flow around a surface-mounted obstacle

- Quantity of Interest K: time-averaged tracer concentration field
- Passive tracer
- Parametric uncertainties:
 - Inlet wind intensity: $U_{inlet} \in [1,10] m s^{-1}$
 - Emission source position: $(x_{src}, y_{src}) \in [-3.5, -0.2]H \times [0.2,2]H$



Example of a tracer concentration field K for a source centered at $(-0.5, 0.5)$ and an inlet wind of $5.5 m s^{-1}$

3-D parameter space

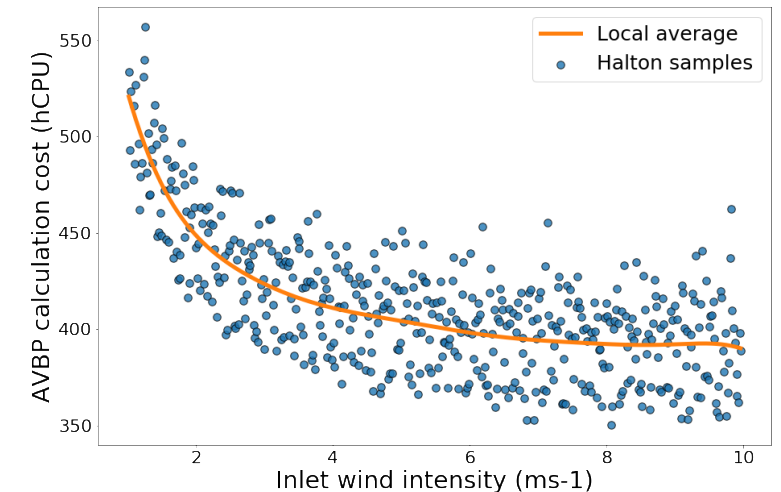


LES data set

- Densely sampled uncertain 3-D space
- 700 AVBP simulations
- Mesh resolution: $\Delta x = \Delta z = 0.04 cm$ resolution, leading to $N_{nodes} = 240,000$ mesh nodes

Optimization of computational cost

- Simulation time depending on the inlet wind intensity
- Average calculation cost: 400hCPU/run





TEST CASE

Quantity of interest

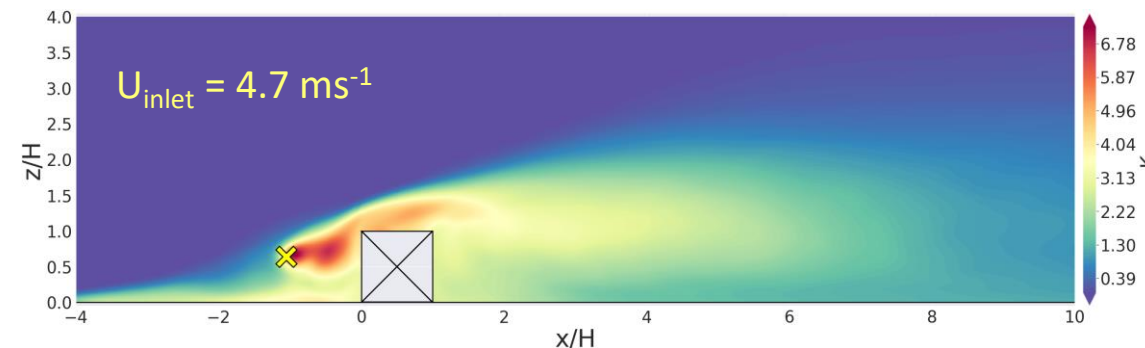
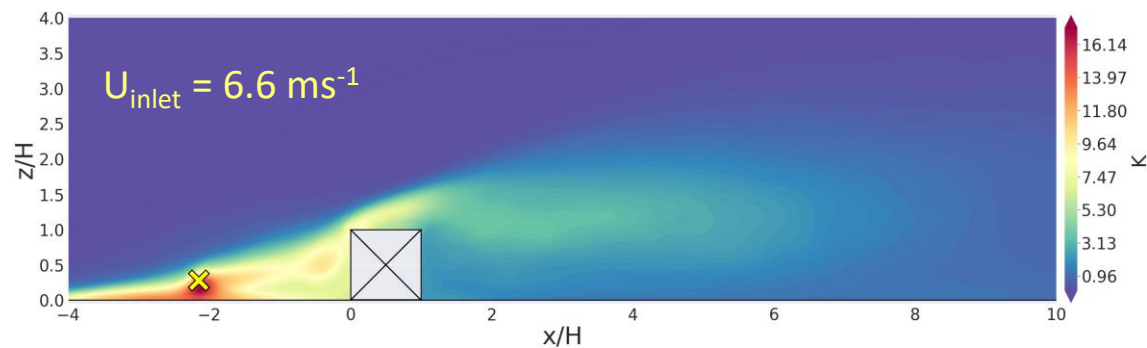
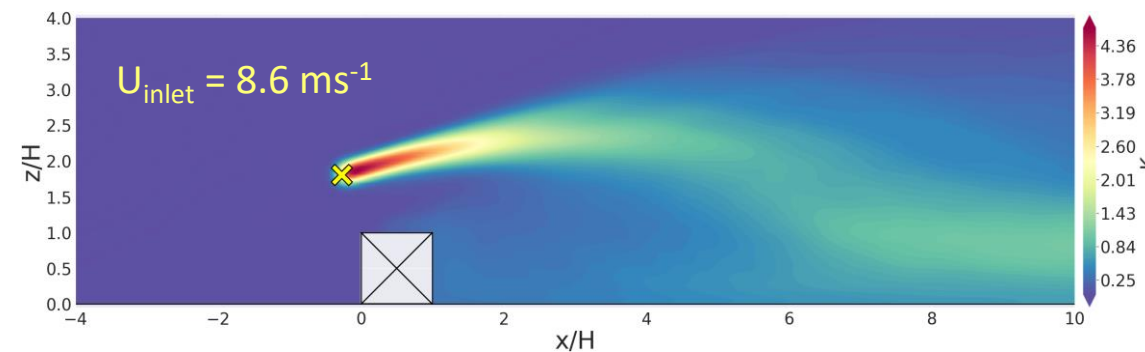
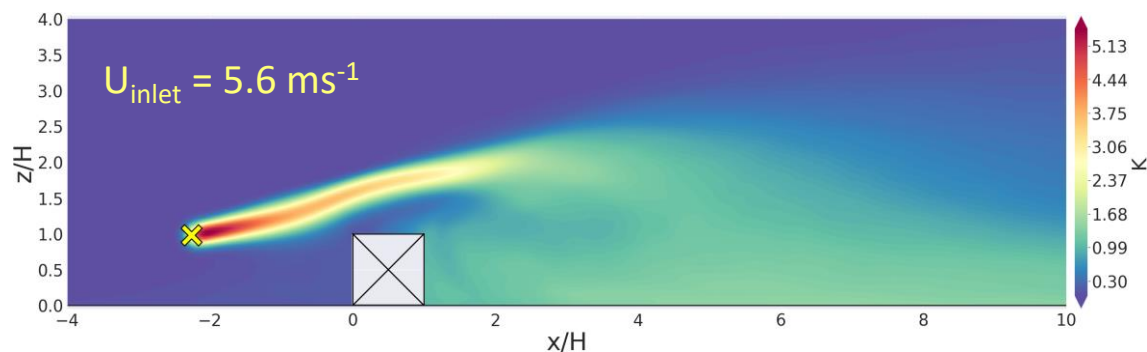
Multiple outputs for LES

- Wind flow: horizontal and vertical velocities
- Plume dispersion: averages, fluctuations
- Cross statistics between flow and tracer dispersion

Time-averaged tracer concentration statistics

- An easy way to start
- Search for metamodells that are able to reproduce the most important flow features

A few examples of the LES dataset (mean concentration fields)



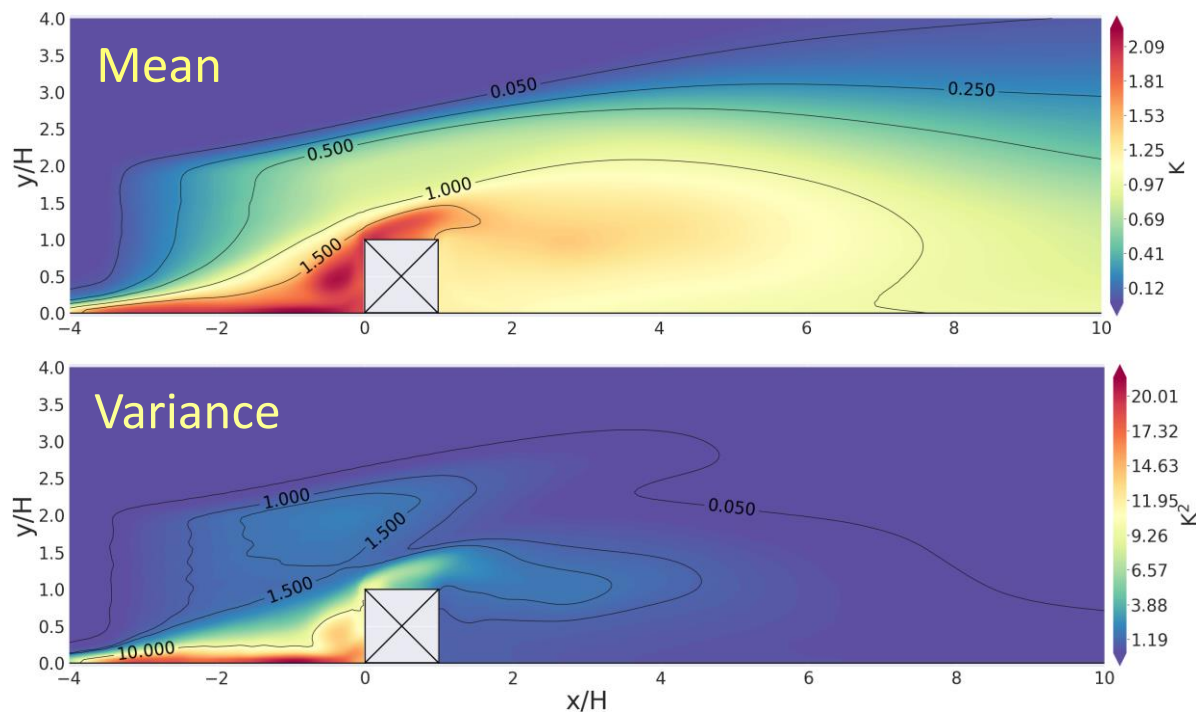


METAMODELLING METHOD

Output dimension reduction

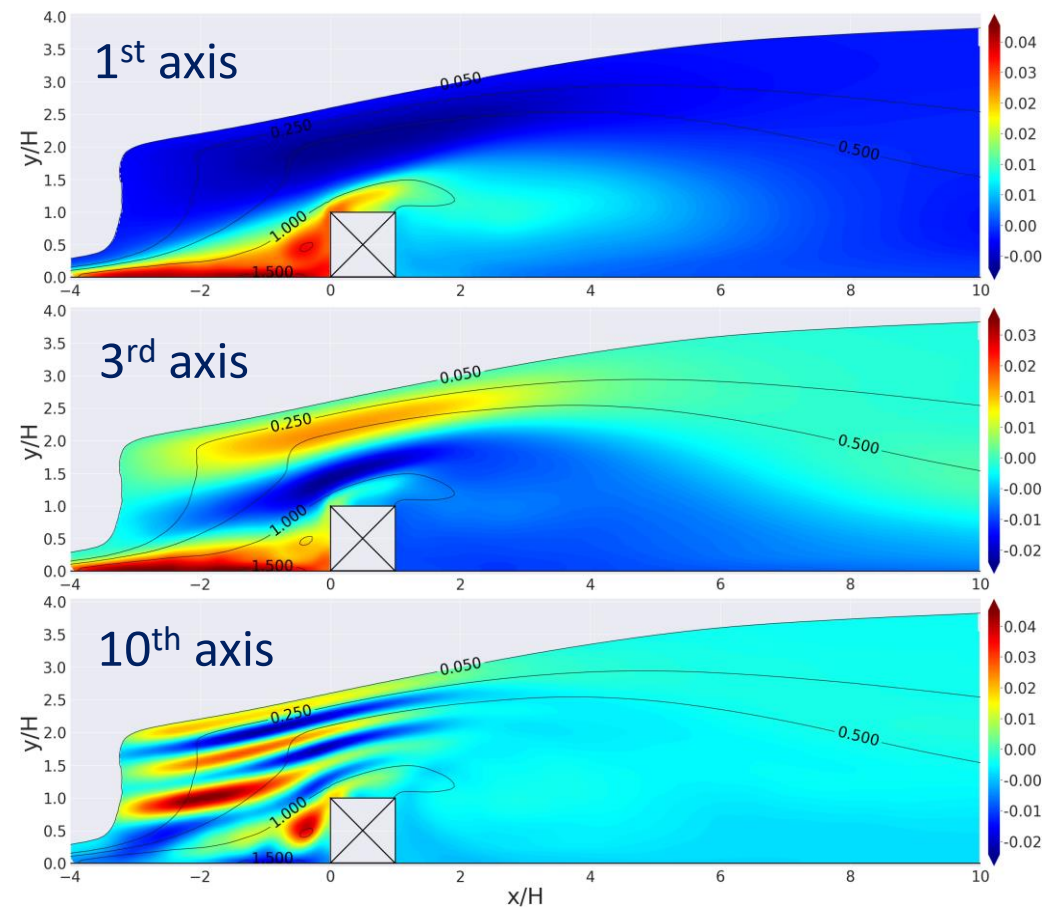
Scientific issue: High dimension output

- Account for spatial correlations
- Reduce space dimension from $N_{\text{nodes}} = 240,000$ to $N_{\text{POD}} = 200$
- Total explained variance 200 axes > 99.9 %.



Ensemble statistics over the 700 LES dataset

First POD axes



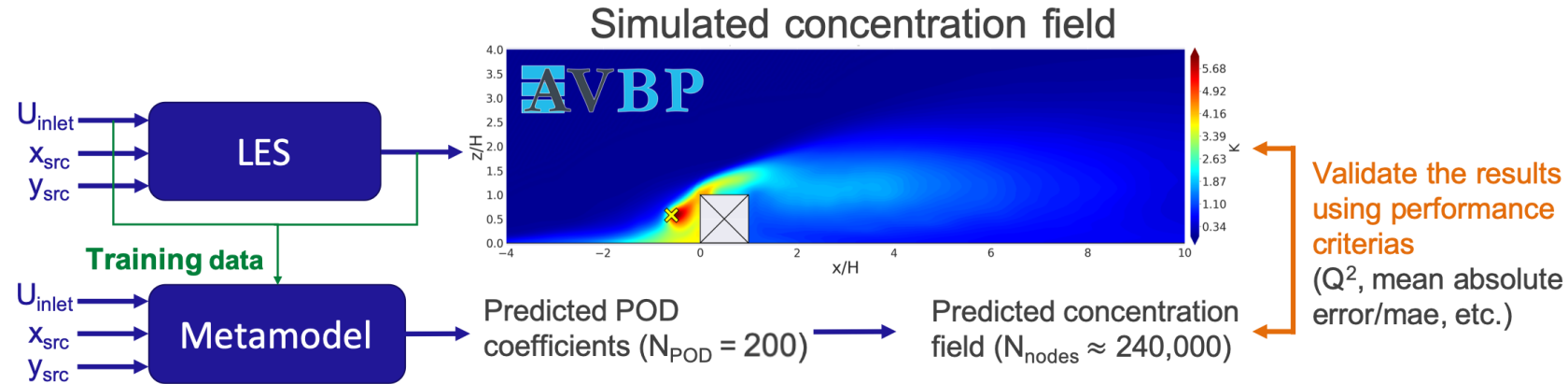
Finer scale structures

METAMODELLING METHOD

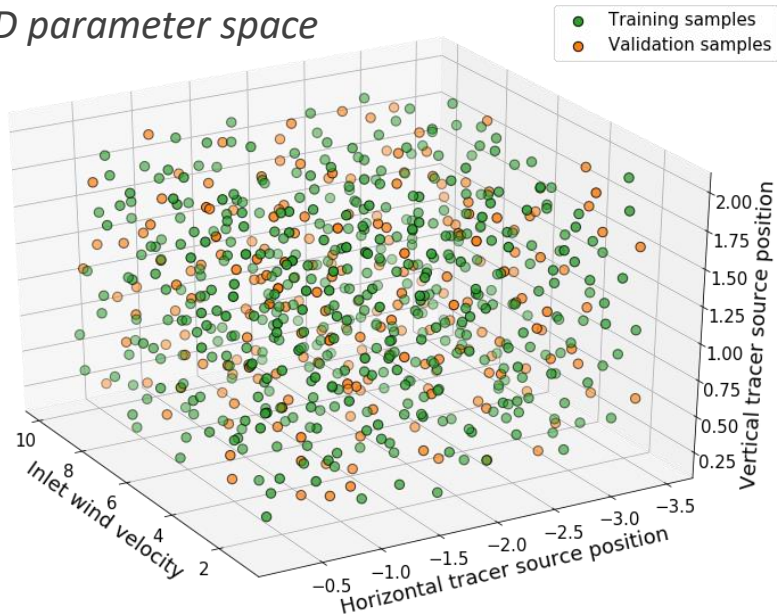
Metamodelling fomulation

700 LES dataset split

- 70% training data (490 LES) used for fitting the metamodel hyperparameters
- 30% validation data (210 LES) used for performance evaluation

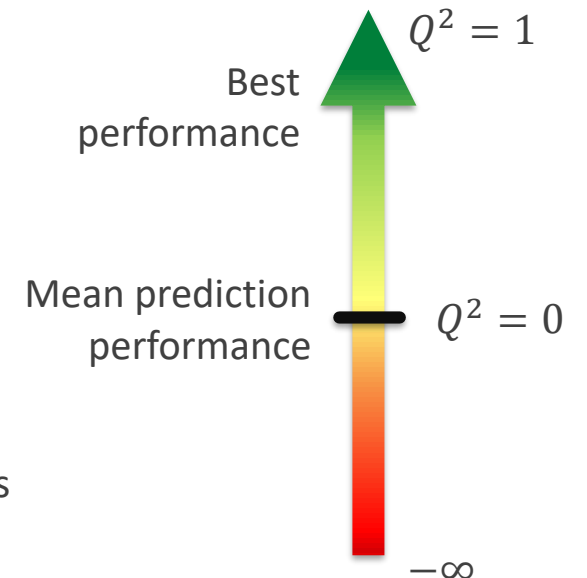


3-D parameter space



Several performance criteria

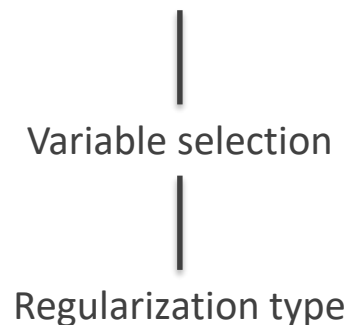
- $Q^2 = 1 - \frac{\sum_{i=1}^{210} (y_i - \bar{y})^2}{\sum_{i=1}^{210} (y_i - \hat{y}_i)^2}$
 - $MAE = \sum_{l=1}^{210} |y_i - \hat{y}_i|$
- $\left\{ \begin{array}{l} - y_i, \text{ LES outputs} \\ - \bar{y}, \text{ LES ensemble mean} \\ - \hat{y}_i, \text{ Metamodel predictions} \end{array} \right.$



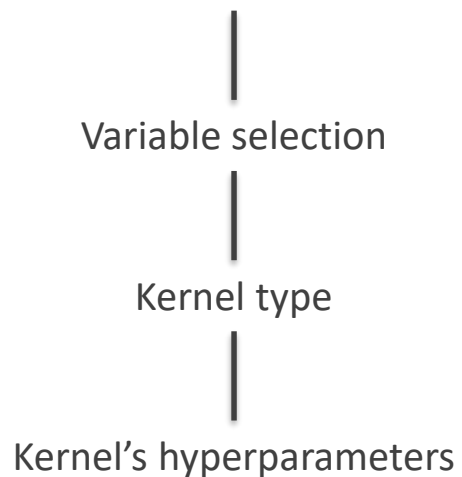


Looking for the most appropriate metamodels for the LES microscale

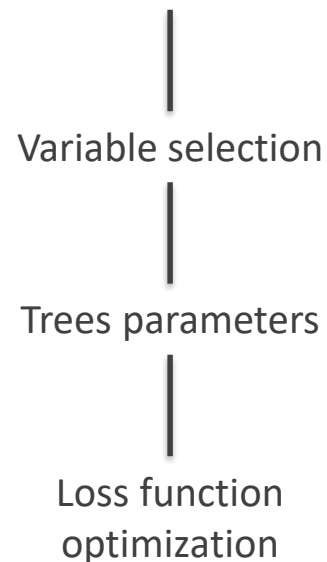
Multiple polynomial regression



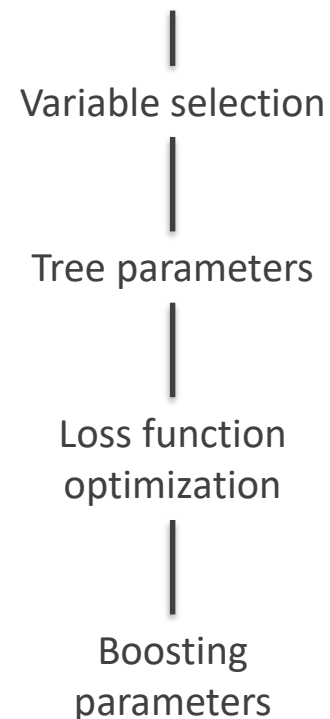
Gaussian processes



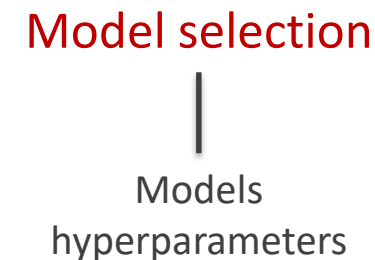
Random Forest



Gradient boosting



Compound model



Model selection

- Every POD axis leads to a selective process
- One metamodel is kept per axis
- Selection relies on best Q^2 performance

Multiple polynomial regression

Multiple polynomial regression

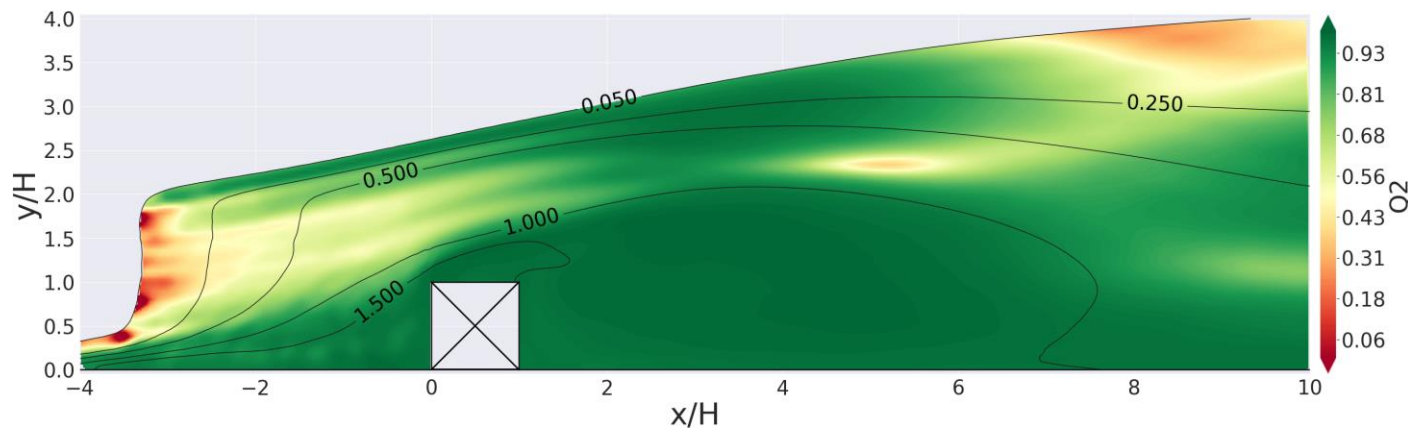
Variable selection

Regularization type

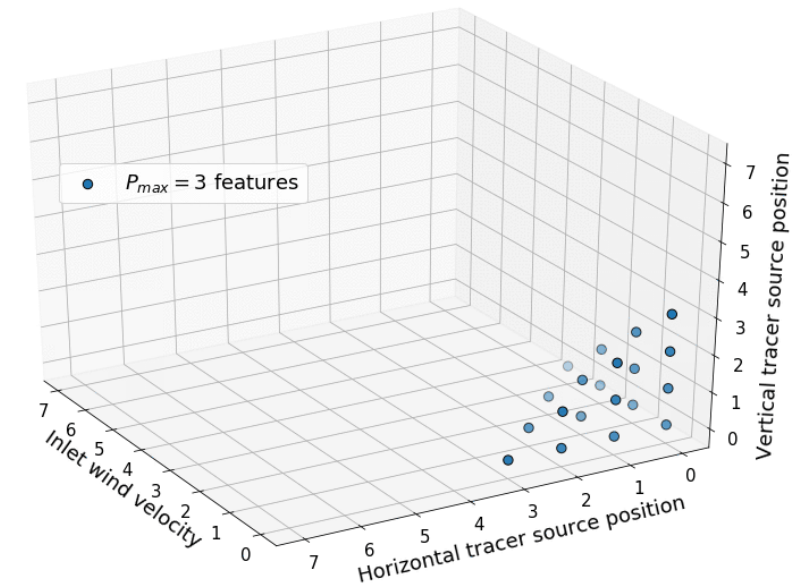
P_{max}	3	5	7
Nb. Variables	20	56	120
Q ² of MPR	76.6 %	82.7 %	80.8 %
Q ² of Ridge $\ \cdot\ _2$	$\leq 76.6\%$	$\leq 82.7\%$	82.1 %
Q ² of LASSO $\ \cdot\ _1$	$\leq 76.6\%$	$\leq 82.7\%$	79.5 %
Q ² of Matching Pursuit $\ \cdot\ _0$	$\leq 76.6\%$	$\leq 82.7\%$	83.0 %

MPR expression

$$\hat{y} = \sum_{i+j+k \leq P_{max}} \lambda_{i,j,k} U_{inlet}^i x_{src}^j y_{src}^k$$



Q² response surface for the MPR *without penalty* and $P_{max} = 5$



Variable selection using the 3-D uncertain parameter polynomial combinations

Prediction procedure

1. The metamodel predicts the 200 POD coefficients
2. Predicted coefficients are projected in the spatial domain using inverse POD operation

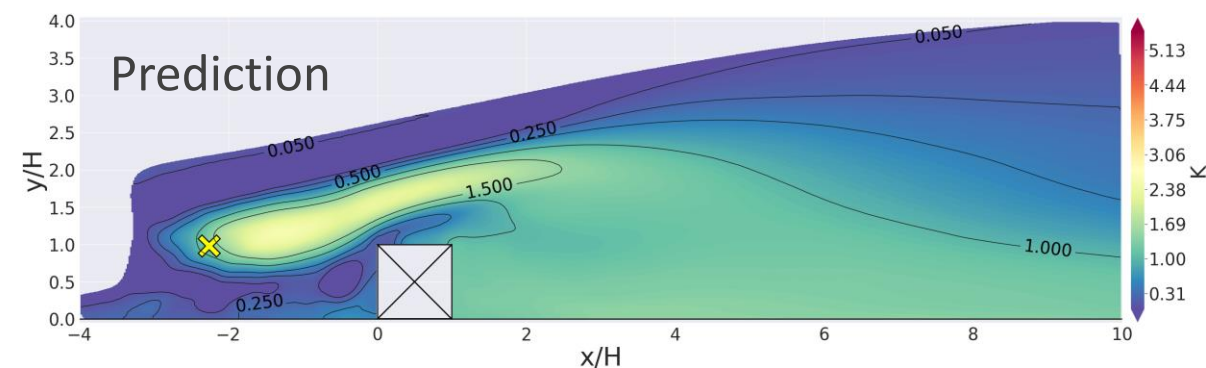
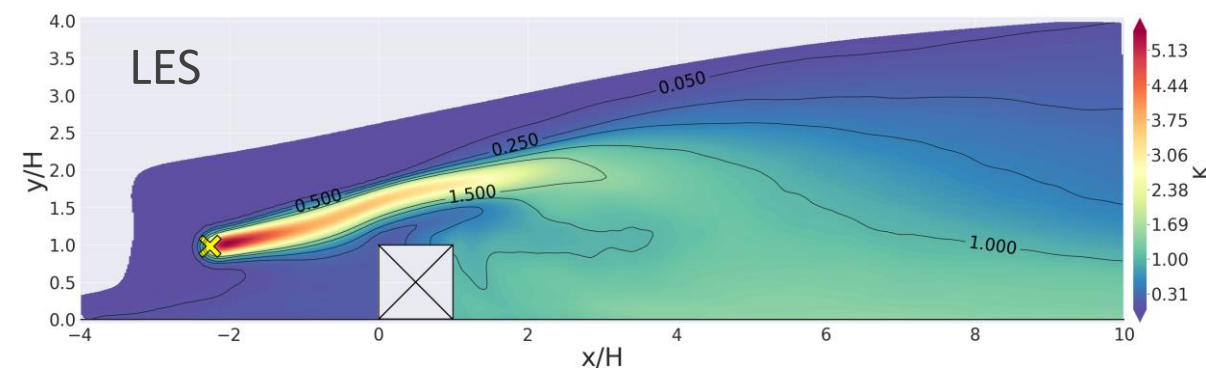
Observations

Upstream

- Coarse structure in the wake of the emission source (wider range, under-predicted peak intensity)
- Distorted over-predicted areas close to the ground

Downstream

- More steady concentration lines than LES
- Small prediction errors slightly offset the isolines



Mean concentration fields for a validation simulation
with $U_{inlet} = 5.6 \text{ ms}^{-1}$

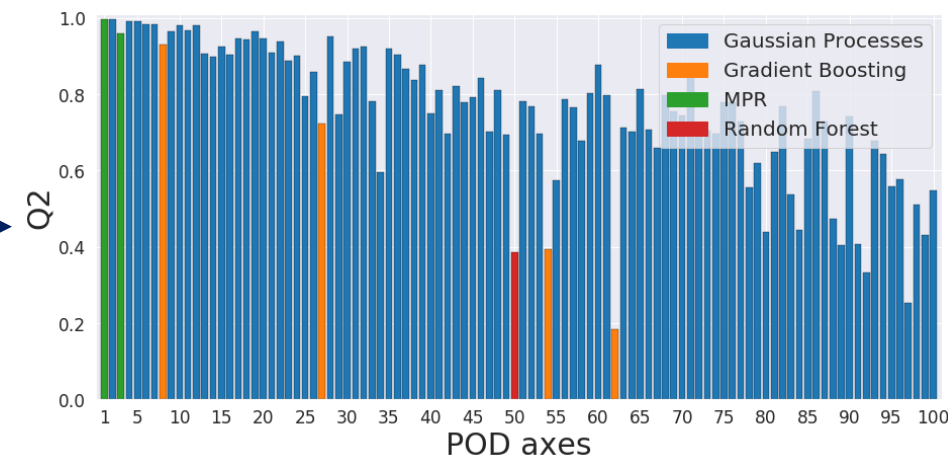
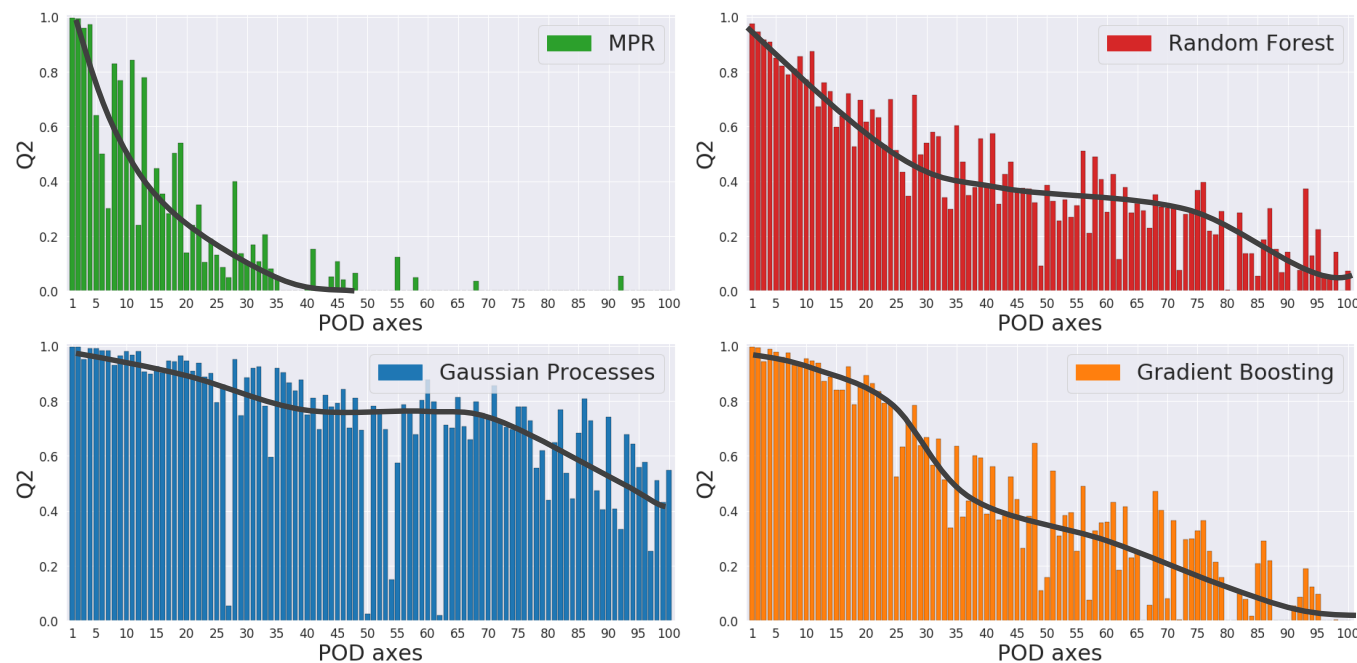
Compound model selection

Q² performance evaluation of metamodels

- MPR performs well on the 5 first POD axes
- Gradient Boosting performances decrease linearly from axis 20
- Random Forest performs poorly on first axes but the decay is slower than gradient boosting
- Gaussian processes maintain a good level of performance on the first 100 axes

Compound model composition

- 4 MPR
- 6 Gradient Boosting
- 15 Random Forest
- 172 Gaussian Processes



In this case the compound model is essentially a combination of Gaussian process metamodels

Q² performances on the first 100 POD axes of 4 families of metamodels

Compound prediction fields

Gradient Boosting

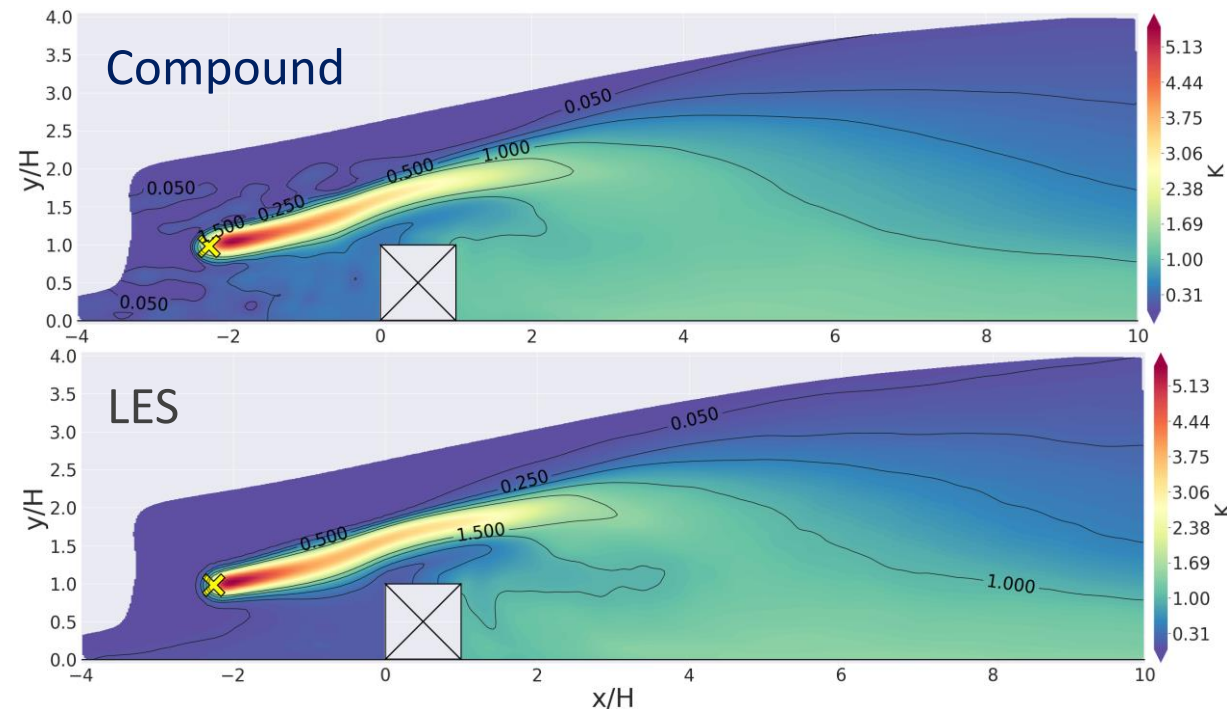
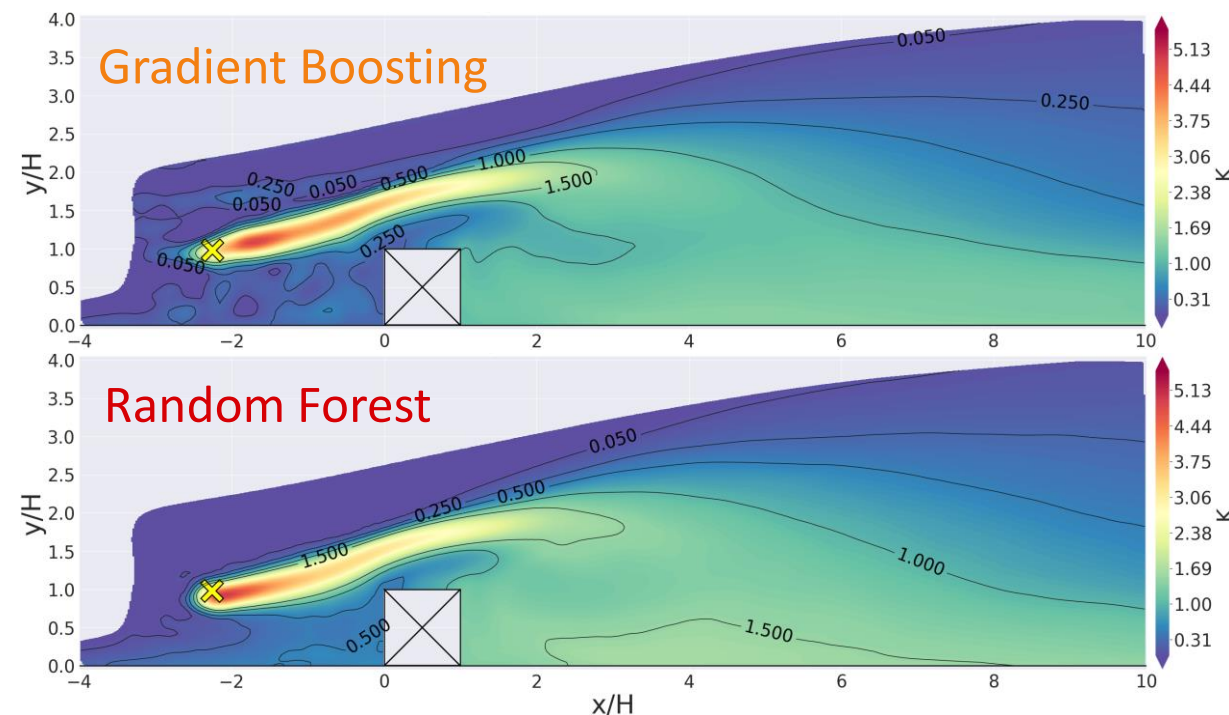
- Noisy prediction near the source
- Underestimation of peak concentrations

Random Forest

- Smooth prediction
- shifted predictions near the source
- Underestimation of peak concentrations

Compound

- Similar results to [Gaussian processes](#)
- Noisy prediction near the source
- Good prediction of the plume structure and peak concentrations



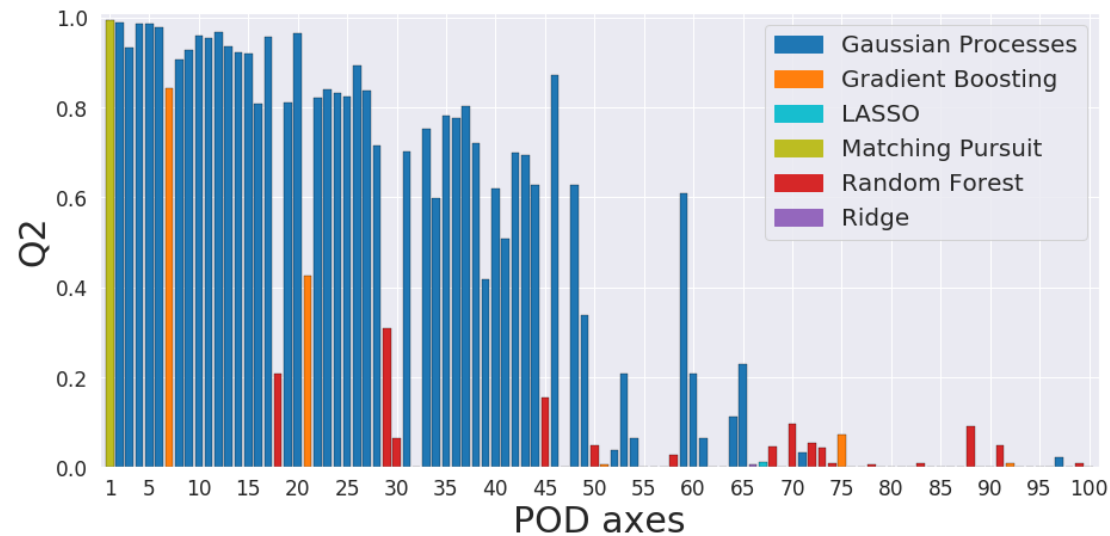
Mean concentration fields for a validation simulation with $U_{inlet} = 5.6 \text{ m s}^{-1}$

Robustness to the lack of training data

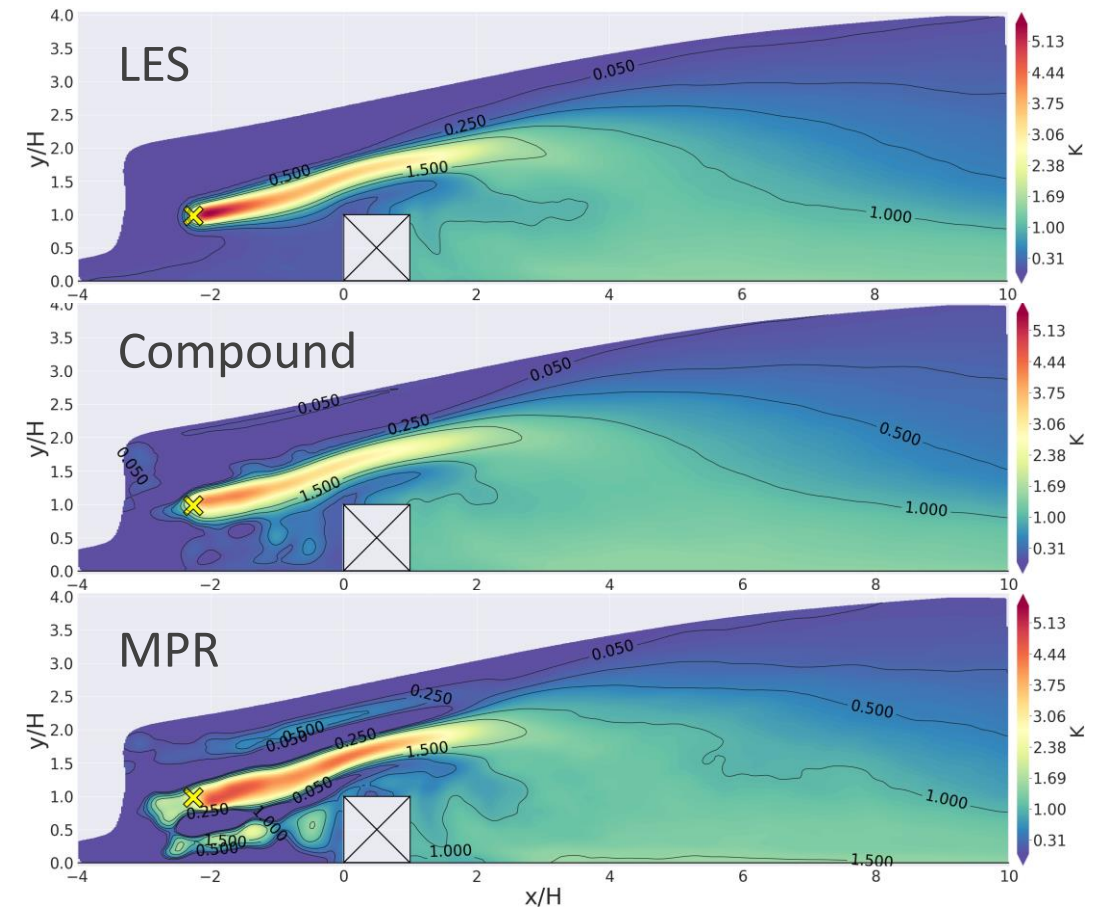
Training data is reduced to 100 LES

POD basis is reduced to 100 axes

- High POD modes can't be considered due to lack of data
- Very noisy predictions near the emission source
- Strong errors in predicting peak concentrations



Q^2 performances on the first 100 POD axes of 4 families of metamodels



Mean concentration fields for a validation simulation with $U_{inlet} = 5.6 \text{ ms}^{-1}$



Towards a real-test case: Mock Urban Test-Case/MUST

High cost of simulation: 60,000 hCPU

Issue

- 2-D test case study showed a minimum ensemble of 100 simulations was necessary for good convergence of performance statistics
- Need for reducing simulation cost

Idea: new problem decomposition

- use LES to metamodel atmospheric flows without tracer
- Simulate plume flow using cheaper CFD models (e.g. RANS)