



# Improving the Reliability of Decision-Support Systems for Nuclear Emergency Management Using Software Diversity Methods

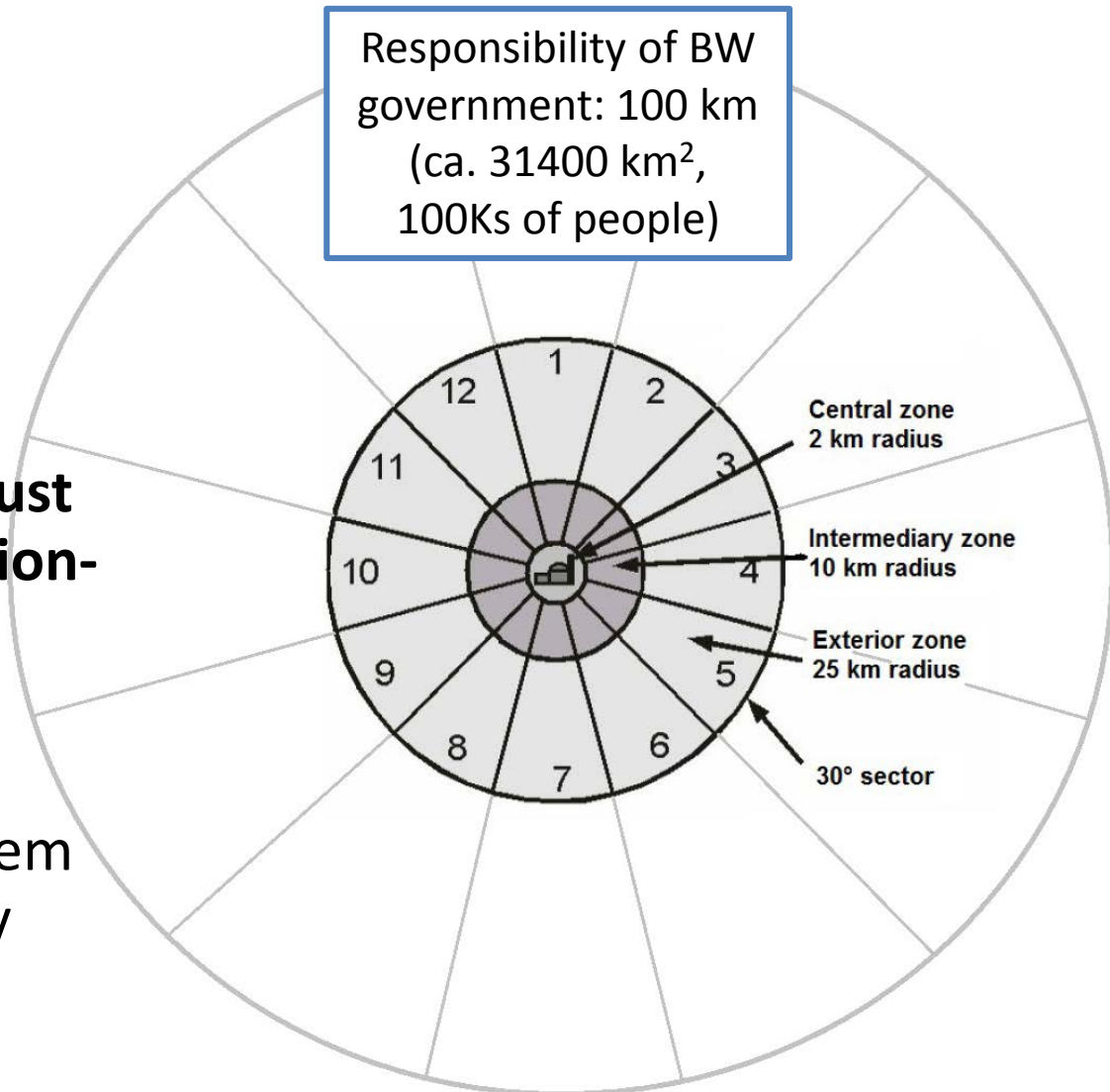
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**Institute of Nuclear Technology and Energy Systems**  
**Stuttgart, Germany**

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Dispersion Modelling for Regulatory Purposes  
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# Taking Counter-Measures in Nuclear Emergencies

- Resources are limited
- Time is critical
- Emission data is scarce
- ... (unknown factors)
  
- **Can decision-makers trust the results of a simulation-based DSNE system in emergency situations?**
  
- Fukushima: SPEEDI system was not used effectively
  - Source: Japanese Diet's Report on Fukushima



# Motivation

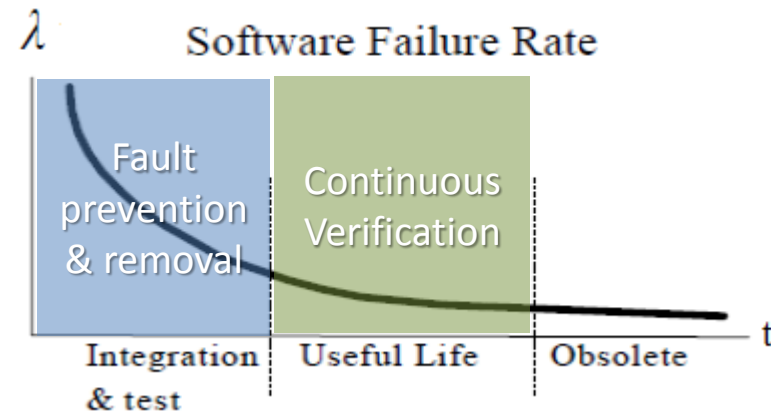
- NASA-STD-8719.13B standard for safety-critical software, paragraph 4.1.1.2.a:
  - As soon as the software *“processes data or analyzes trends that lead directly to safety decisions”* it must be considered safety critical  
→ **DSNE systems are safety-critical**
- From a Software Engineering point of view ...
  - Complexity is the main cause of software faults
  - Model refinements introduce more complexity into the simulation codes (Example: from 2D to 3D)
  - Codes contain an unknown number of software faults
- How to improving the reliability of dispersion codes?
- How to increasing the trustworthiness of dispersion simulation results?

# Software Reliability Engineering (SRE)

- Single version software reliability methods

- Fault prevention
  - Coding standards, software metrics
- Fault removal
  - Unit and integration testing

→ **Initial verification of codes**



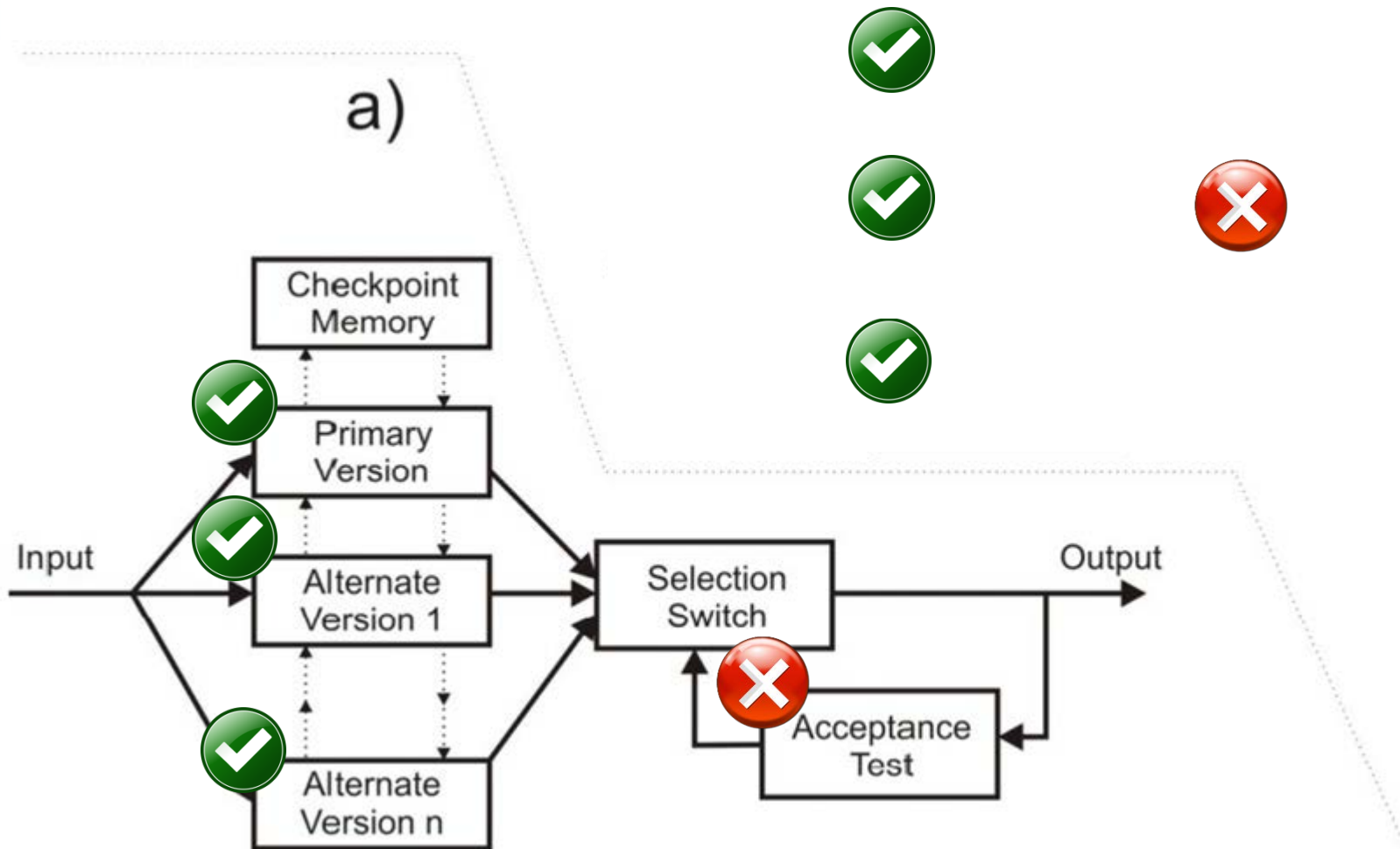
- Multi-version software reliability methods

- Error detection and confinement
- Acceptance tests
- Recovery Blocks

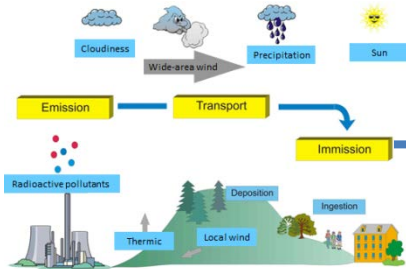
→ **Continuous verification of codes**

# a.) Recovery Blocks and b.) N-Version Programming

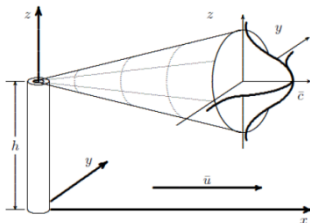
**Rationale:** software build differently is more likely to fail differently.



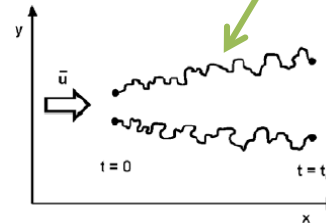
# From Models to Simulation Codes



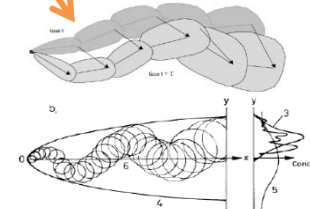
$$\frac{\partial \bar{c}}{\partial t} + \bar{u}_k \frac{\partial \bar{c}}{\partial x_k} = - \frac{\partial \overline{u'_k c'}}{\partial x_k} + \bar{P}_c$$



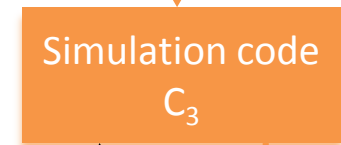
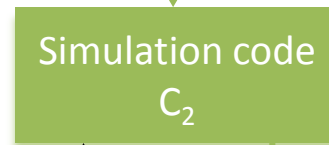
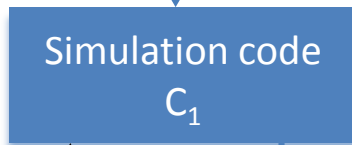
Gaussian Plume Model



Lagrange Particle Model



Puff Models



Input data and parameters:  
 $[P, d_P]$



Results  $C_1$   
 $[R_1, d_R]$

Results  $C_2$   
 $[R_2, d_R]$

Results  $C_3$   
 $[R_3, d_R]$

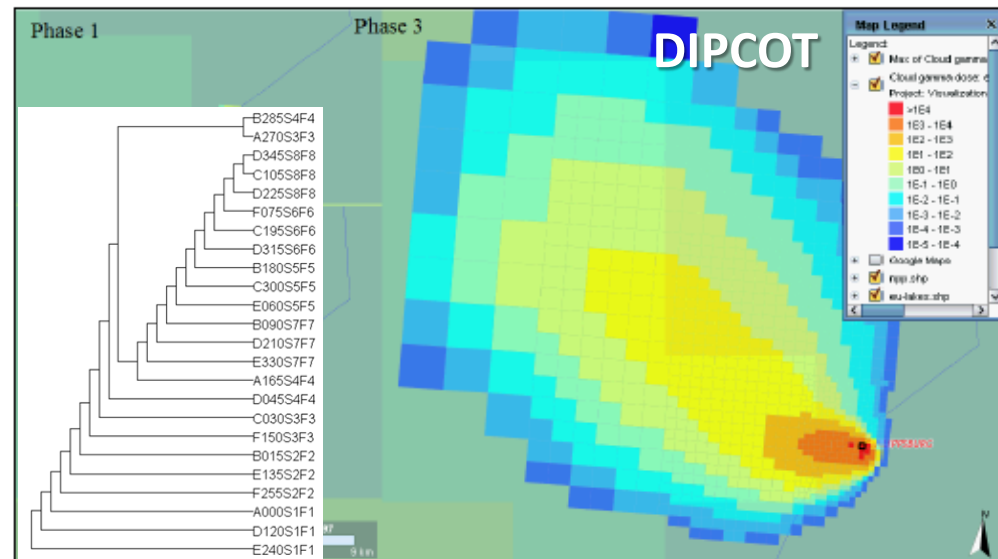
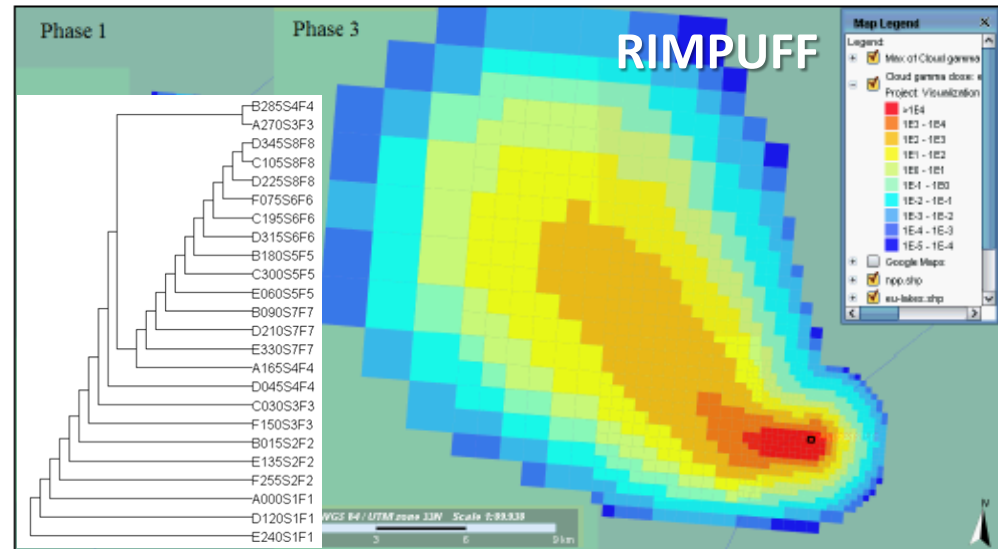


# Disperison codes and N-Version Programming

- **Example:** RODOS (Real-time Online Decision Support System for nuclear emergency management)
  - ATSTEP (Karlsruhe Institute of Technology)
    - Puff model with time-integrated elongated puffs
  - DIPCOT (National Centre for Scientific Research “Demokritos”, Greece)
    - Lagrange particle model
  - RIMPUFF (Risø DTU National Laboratory, Denmark)
    - Puff model
- Prerequisites for N-Version programming:
  -  Developed by completely independent teams
  -  Attempt to solve the transport equation numerically (same software requirements)

# Comparing Dispersion Simulation Results

- Problem:
  - How to compare individual results?
  - Inherent model differences
  - Continuous mathematical space
  
- Idea:
  - Compare taxonomies of results instead of individual results
  - Discrete mathematical space





# Reference Input Case Ensemble

- 24 input cases with varying parameters
  - Wind speed (1–8 m/s) and direction (0–360°)
  - Diffusion (A-F) and release category (F1–F8)

**A000S1F1** **B180S5F5**  
**D120S1F1** **C300S5F5**  
**E240S1F1** **E060S5F5**

**B015S2F2** **C195S6F6**  
**E135S2F2** **D315S6F6**  
**F255S2F2** **F075S6F6**

**A270S3F3** **B090S7F7**  
**C030S3F3** **D210S7F7**  
**F150S3F3** **E330S7F7**

**A165S4F4** **C105S8F8**  
**B285S4F4** **D225S8F8**  
**D045S4F4** **D345S8F8**

**A** **000** **S1** **F1**

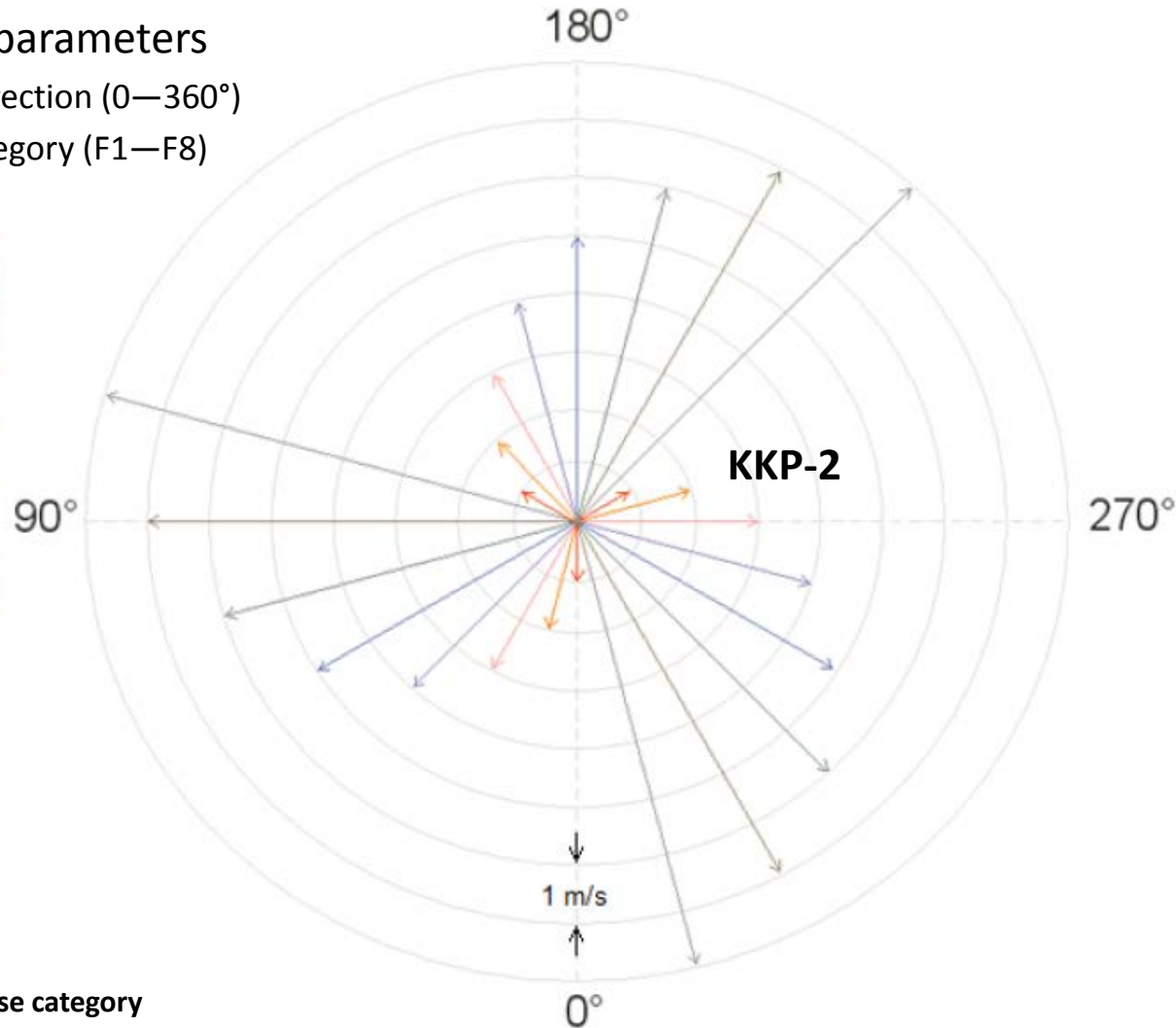


Diffusion category

Wind direction

Release category

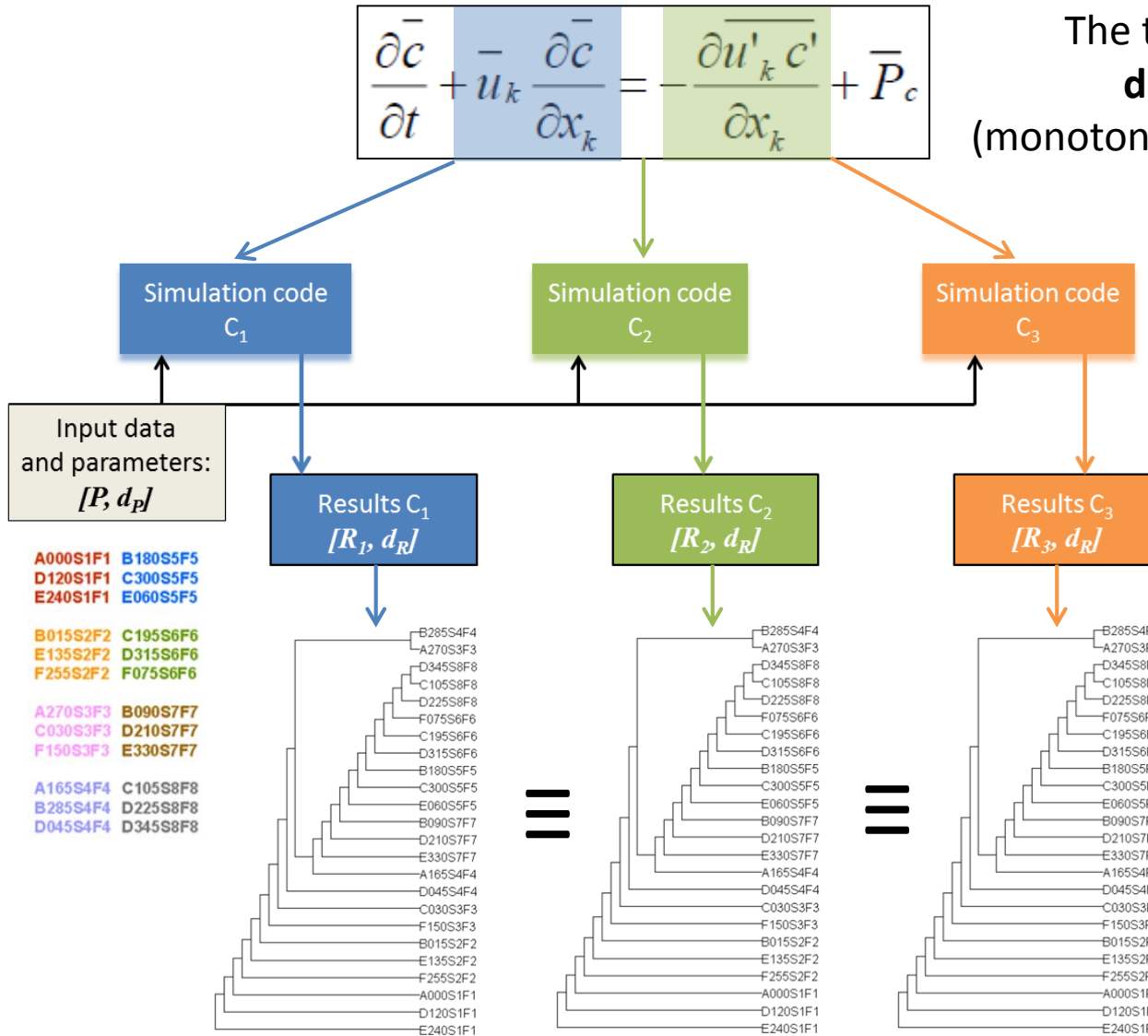
Wind speed



# A Voter for Dispersion Simulation Results

$$\frac{\partial \bar{c}}{\partial t} + \bar{u}_k \frac{\partial \bar{c}}{\partial x_k} = - \frac{\partial \bar{u}'_k c'}{\partial x_k} + \bar{P}_c$$

The transport equation is a **deterministic model**  
(monotonicity, distance preservation)



$$C_k: [P, d_p] \rightarrow [R_k, d_R]$$

**Isometric map**  
(distance preserving function)

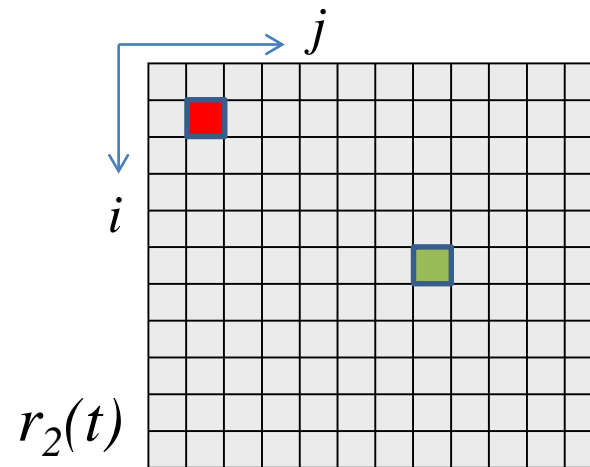
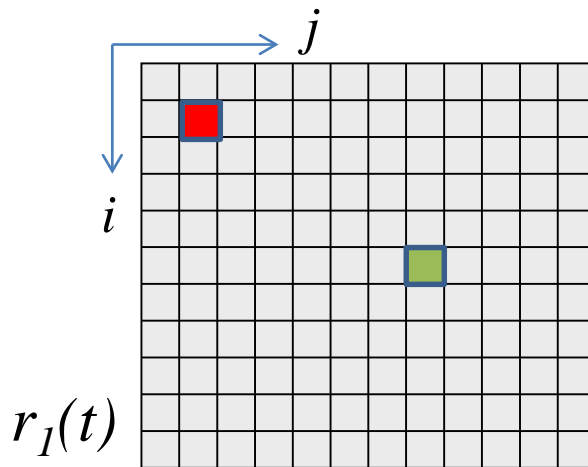
Taxonomies of results will be identical if and only if codes correctly implement models

# A Metric for Dispersion Simulation Results

- **Dispersion simulation results** = distributions of continuous variables in a finite space

Residual sum of squares:  $RSS = \sum_{i=1}^n [y_i - f(x_i)]^2$

Observed values (Results of  $C_1$ )      Estimated values (Results of  $C_2$ )



Generalized RSS:  $d_R(r_1, r_2) = GRSS(r_1, r_2) = \sqrt{\sum_{t=1}^{i \leq TS} \sum_{i=1}^{i \leq N} \sum_{j=1}^{j \leq M} (r_1[t, i, j]^p - r_2[t, i, j]^p)^2}$

$0 < p \leq 1$

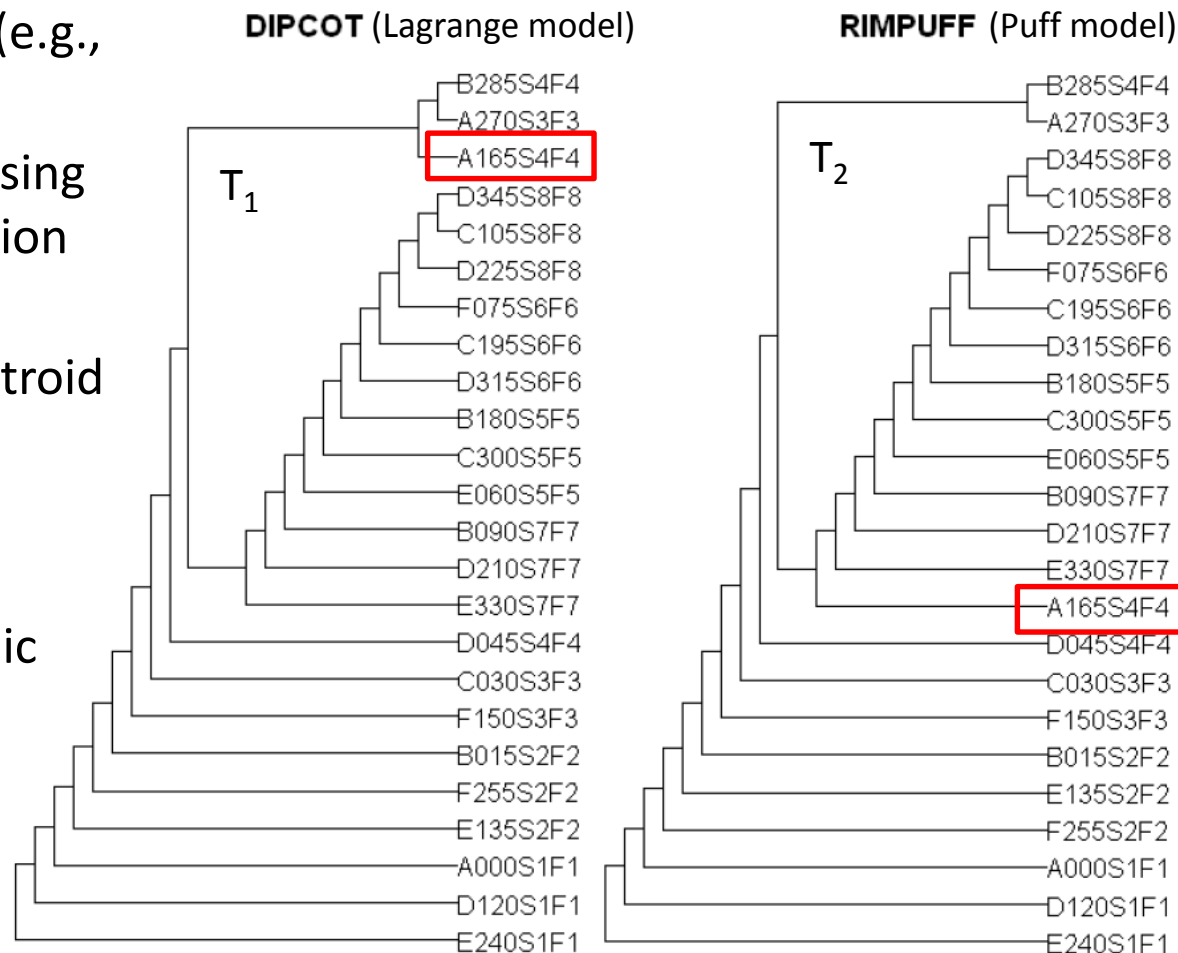
$p < 0.5 \rightarrow$  concentration of emitted substance is dominant

$p \geq 0.5 \rightarrow$  wind speed and direction are dominant

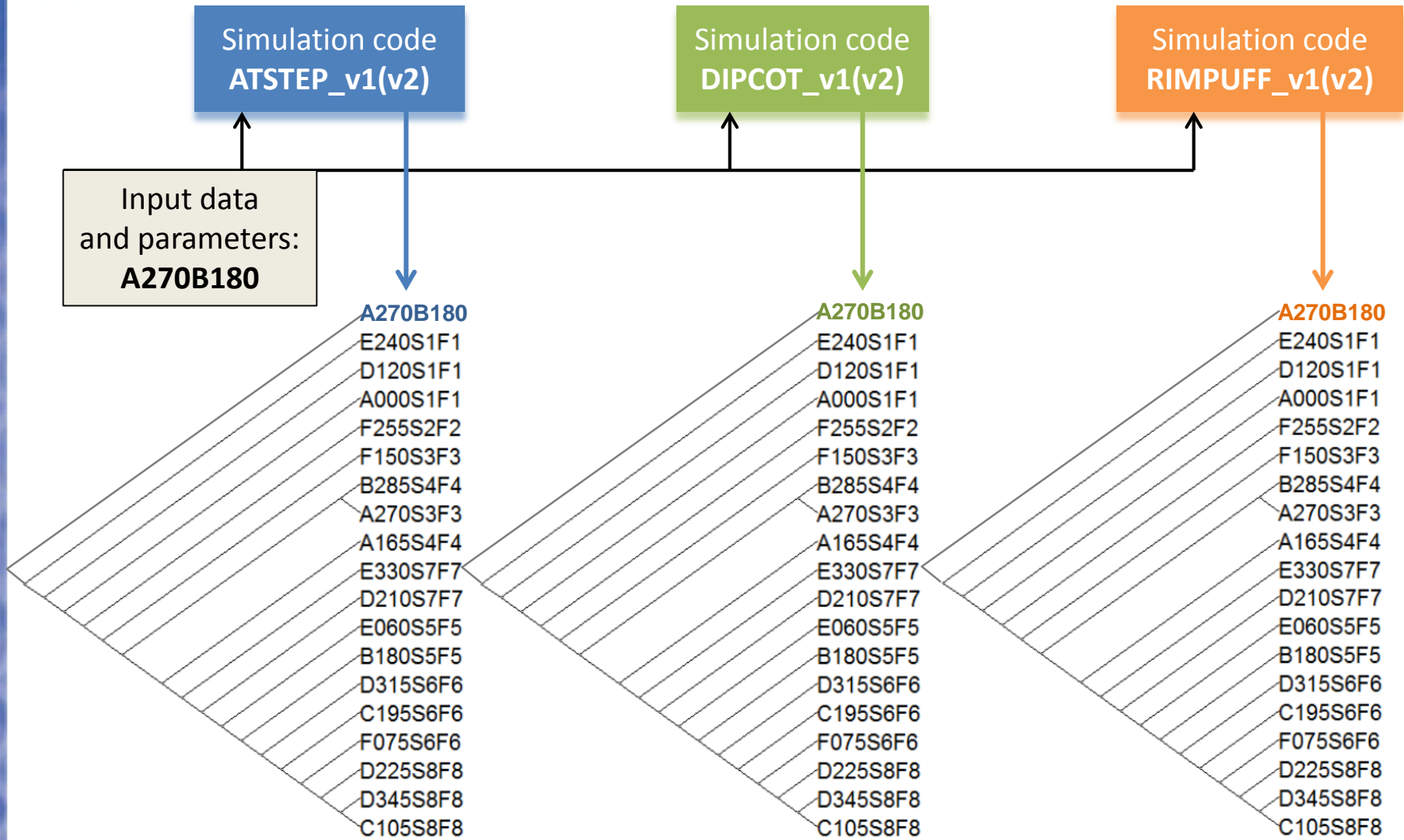
# Building and Comparing Taxonomies of Results

1. Run simulations on reference input case ensemble using different simulation codes (e.g., ATSTEP, DIPCOT, RIMPUFF)
2. Compute distance matrix using GRSS on dispersion simulation results
3. Hierarchical clustering (centroid method)  $\rightarrow$  taxonomies of results
4. Compute the topological distance between taxonomic trees:  $RF(T_1, T_2)$ 
  - $\max RF(N) = 2N-6$
  - $\max RF(24) = 42$

$$RF(DIPCOT, RIMPUFF, GRSS_{p=0.6}) = 4 (9.52\%)$$



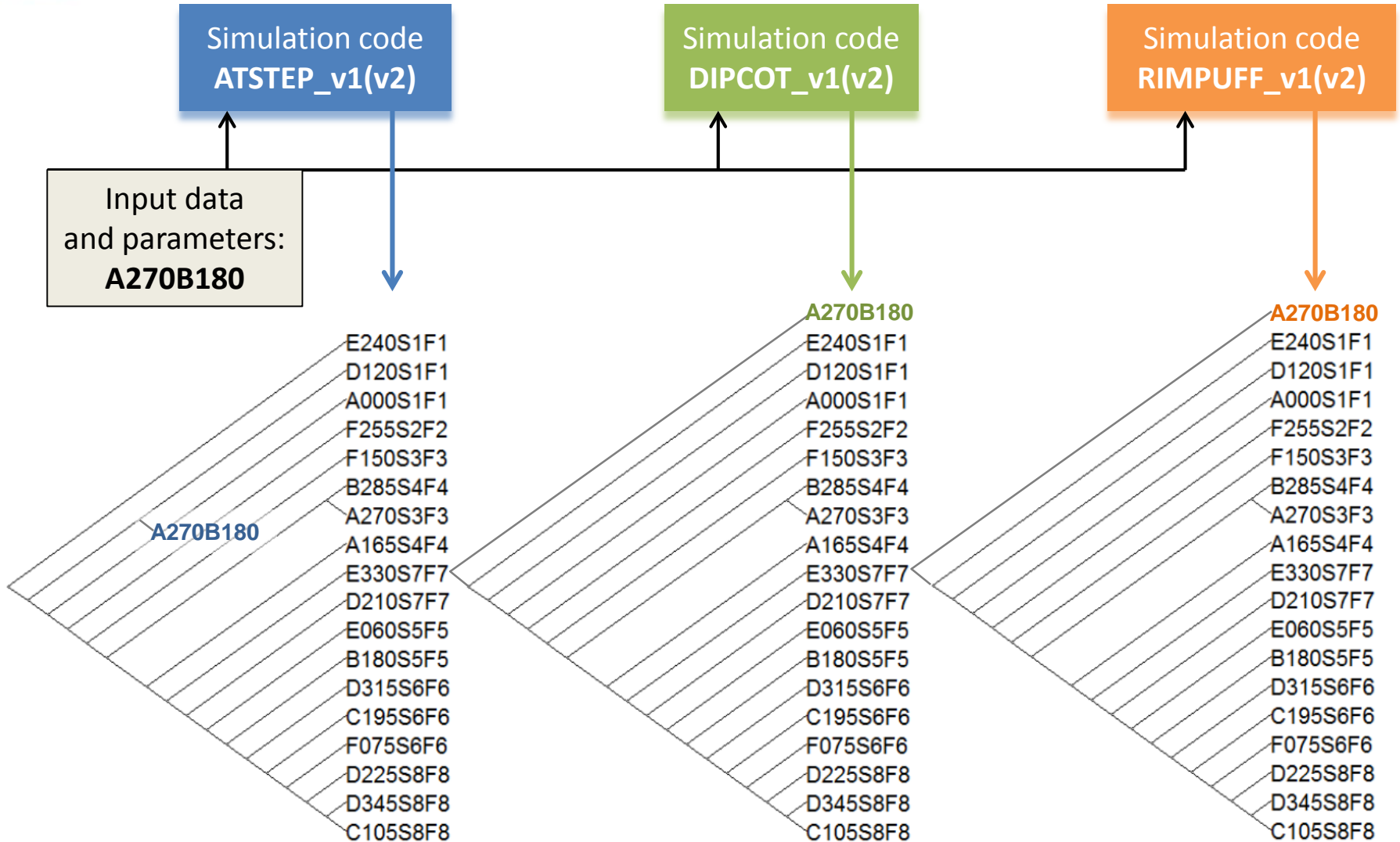
# A Taxonomy-Based Voter for Dispersion Simulation Results



Strict Consensus

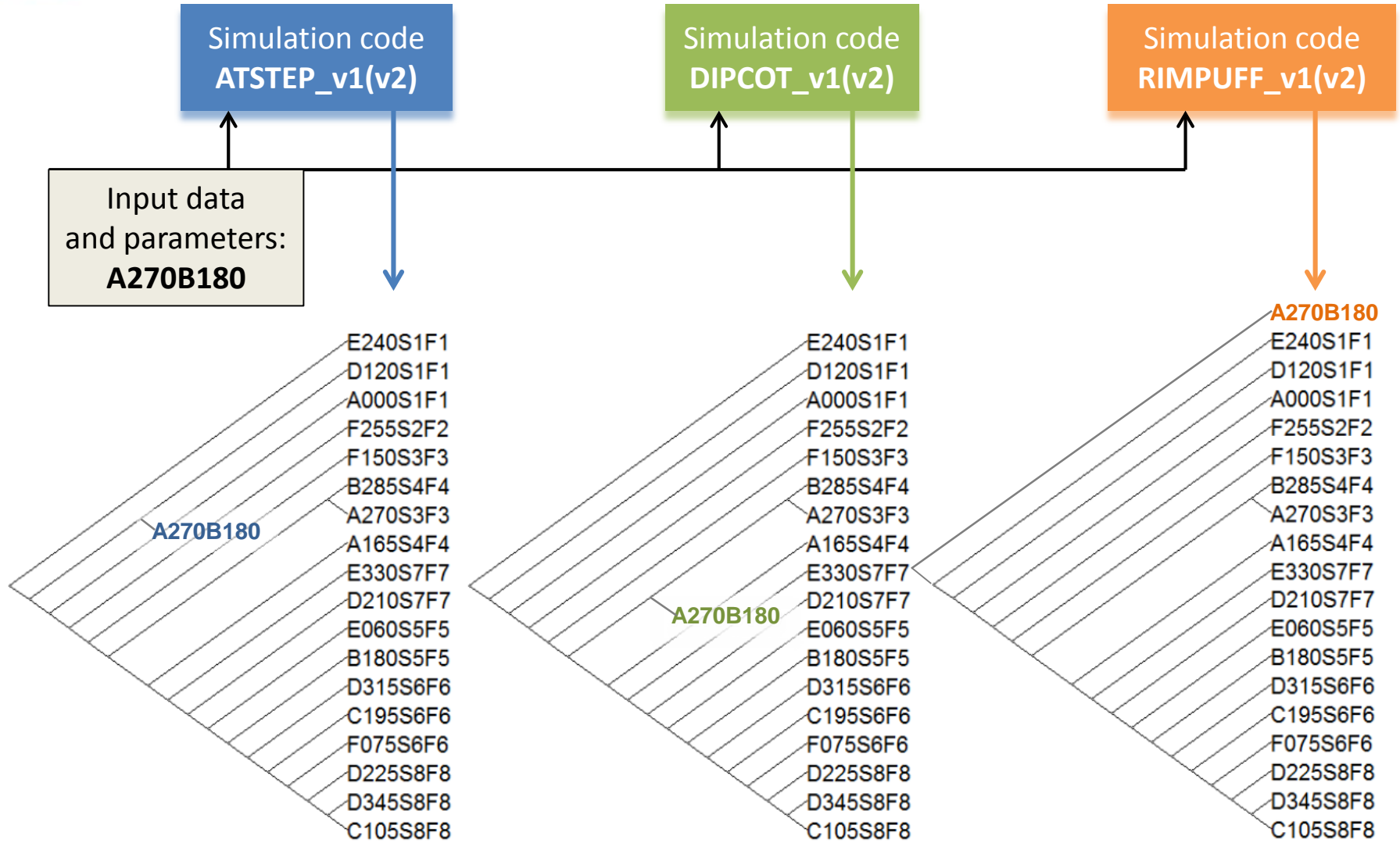


# A Taxonomy-Based Voter for Dispersion Simulation Results





# A Taxonomy-Based Voter for Dispersion Simulation Results



**Disagreement**

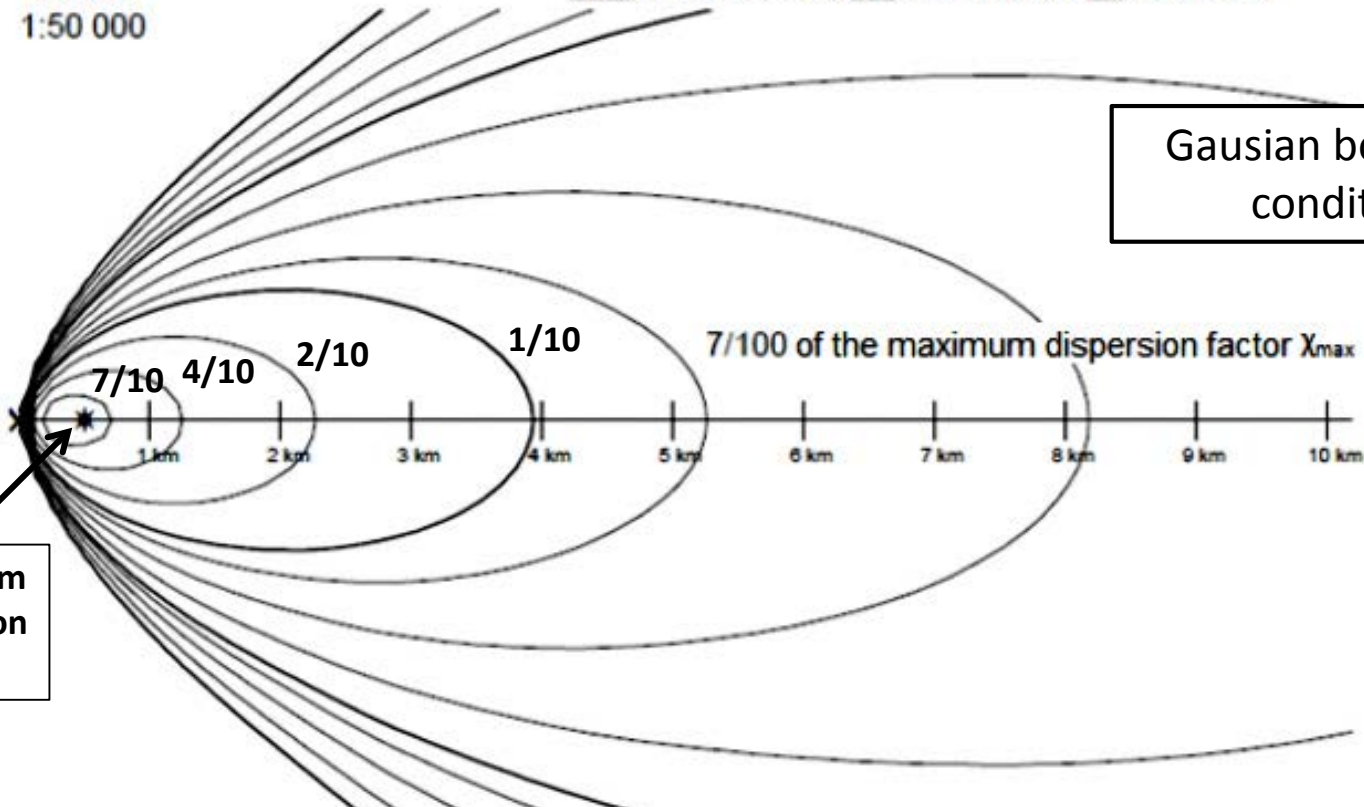
# An Acceptance Test for Dispersion Simulation Results

Source: „Leitfaden für den Fachberater Strahlenschutz der Katastrophenschutzleitung bei kerntechnischen Notfällen“

Scale  
1:50 000

Concentration levels with respect to the maximum dispersion factor (from right to left):  
1/1000, 2/1000, 4/1000, 7/1000, 1/100, 2/100, 4/100, 7/100, 1/10, 2/10, 4/10, 7/10

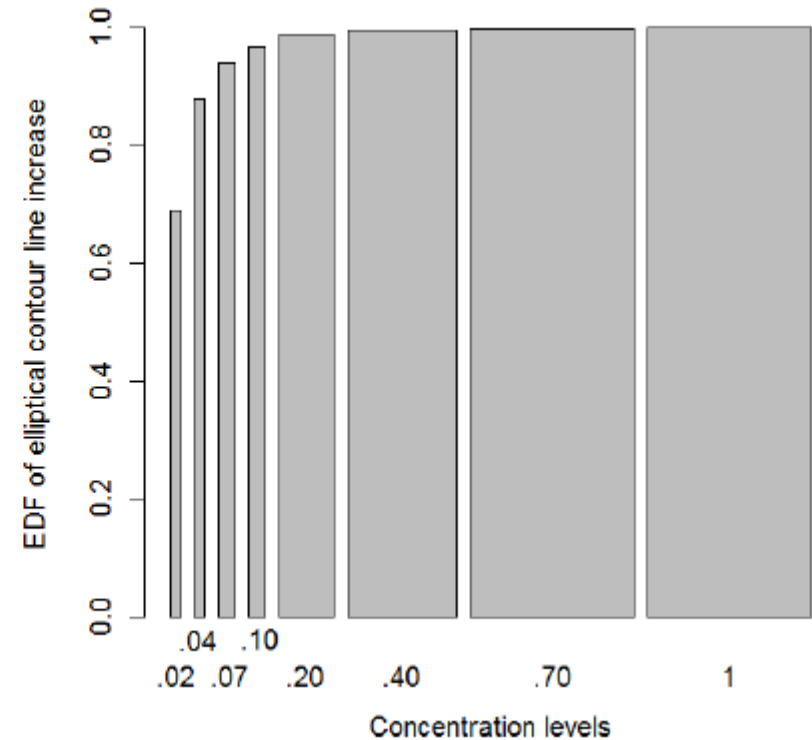
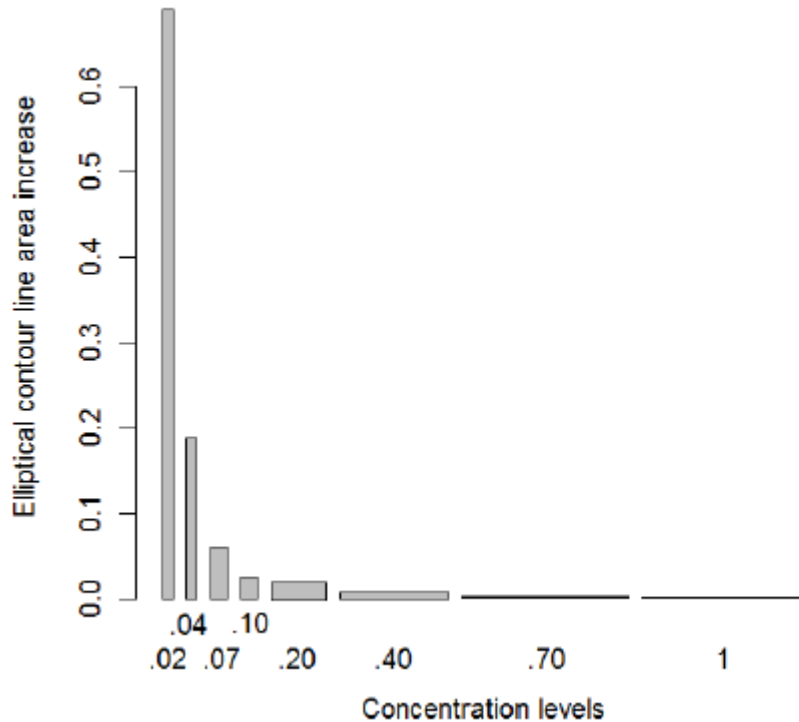
Gaussian boundary condition



Maximum dispersion factor

X Emission source \* Max. dispersion factor (at around 500 m downwind from the source):  $3,2 \cdot 10^{-6} \text{ s/m}^3$   
Unstable conditions (A and B atmospheric stability classes); wind speed: 1 m/s; emission height: 150 m

# An Acceptance Test for Dispersion Simulation Results



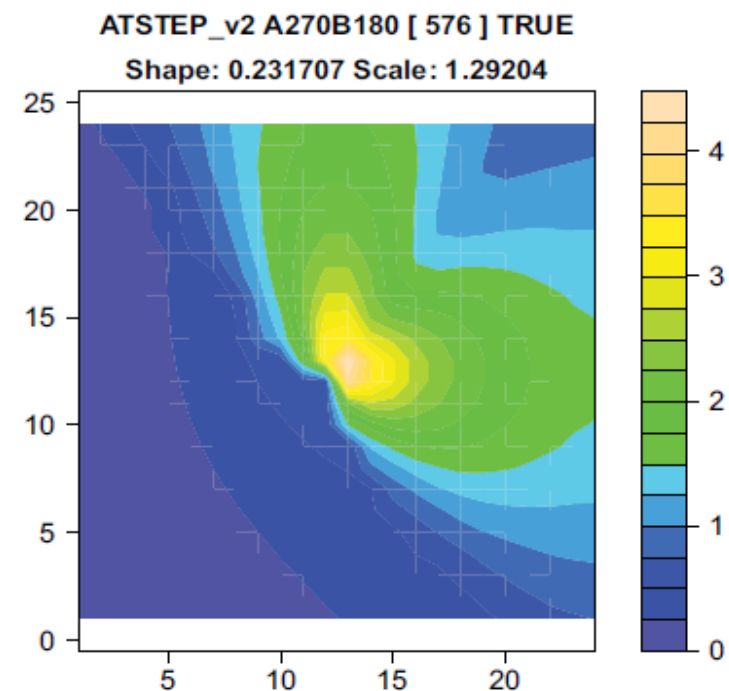
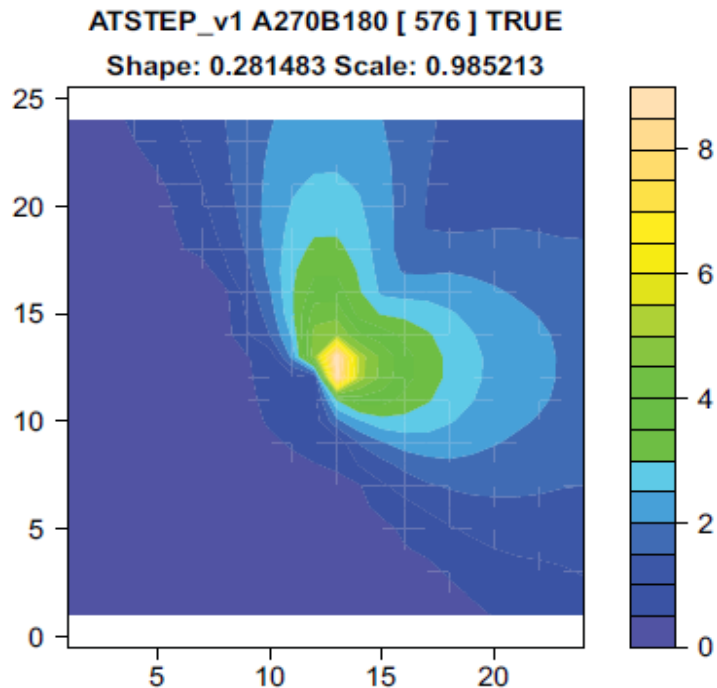
Weibull distribution:  $F_0(x) = 1 - e^{-(x/\lambda)^k}$

- $k$  Shape parameter of the Weibull distribution
- $\lambda$  Scale parameter of the Weibull distribution

**Acceptance test:** Check if empirical distribution (from results) fits the hypothetical distribution by means of a goodness of fit test (Kolmogorov-Smirnov).

# Experimental Validation of the Approach

- Two versions of the RODOS system
  - RODOS\_v1 (ATSTEP\_v1, DIPCOT\_v1, RIMPUFF\_v1)
    - Bug fixing and improvements brought to the system
  - RODOS\_v2 (ATSTEP\_v2, DIPCOT\_v2, RIMPUFF\_v2)
- Reference input case ensemble (24 cases)
- Extended input case ensemble – with rotating wind (24 cases)



# Results: Kolmogorov-Smirnov Test

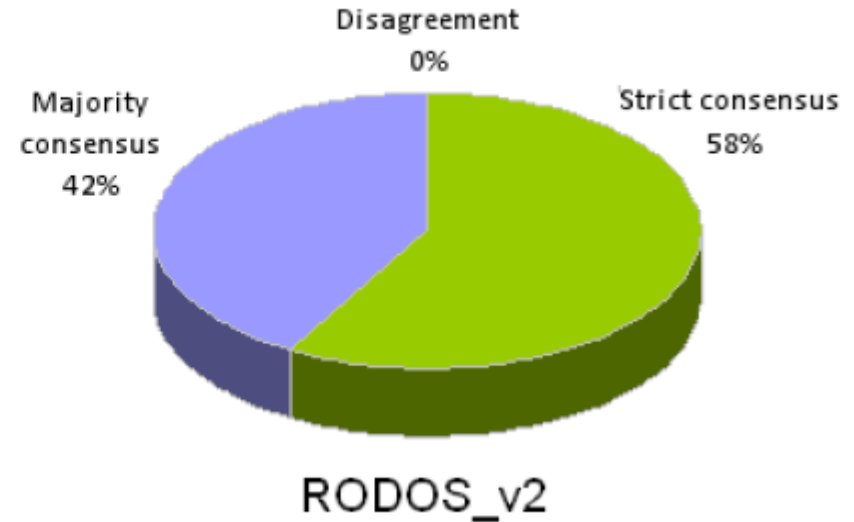
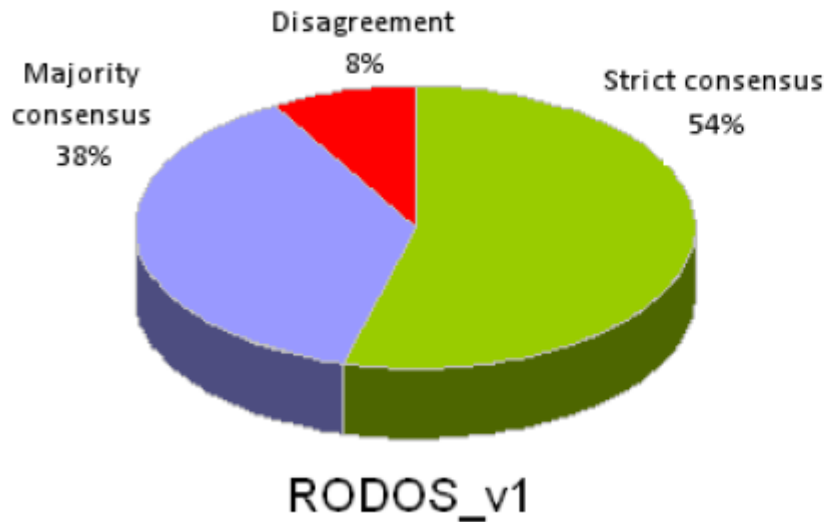
**Table 1.** Kolmogorov-Smirnov test results for the two input case ensembles for RODOS\_v1 and RODOS\_v2.

<i>Reference Input Case Ensemble</i>						
$\alpha = 1\%$	ATSTEP_v1	ATSTEP_v2	DIPCOT_v1	DIPCOT_v2	RIMPUFF_v1	RIMPUFF_v2
Passed	16 / 24	22 / 24	20 / 24	19 / 24	21 / 24	21 / 24
Percent	66.67%	<b>91.67%</b>	83.33%	79.17%	87.50%	87.50%
<i>Second Input Case Ensemble</i>						
Passed	17 / 24	20 / 24	15 / 24	19 / 24	20 / 24	23 / 24
Percent	70.83%	<b>83.33%</b>	62.50%	<b>79.17%</b>	83.33%	<b>95.83%</b>

- RODOS\_v2
  - Improves over RODOS\_v1 in 4 out of 6 cases
  - RIMPUFF handles wind rotation better than constant wind direction



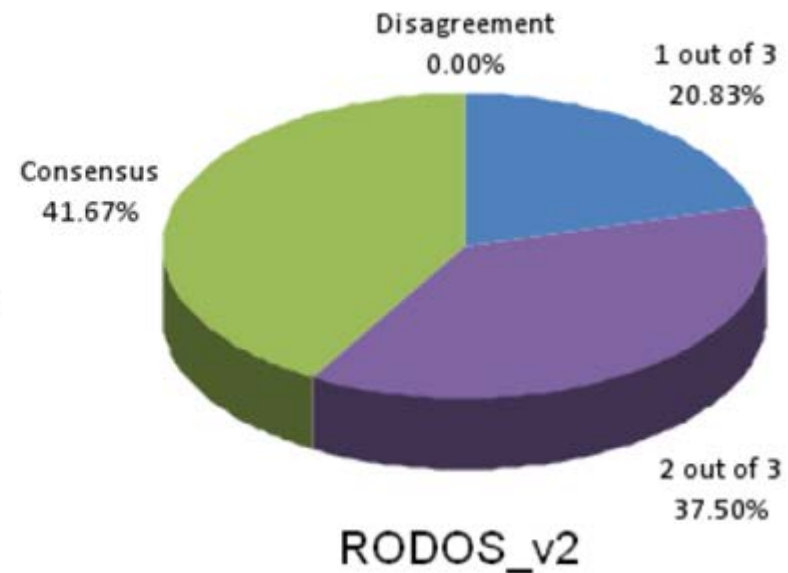
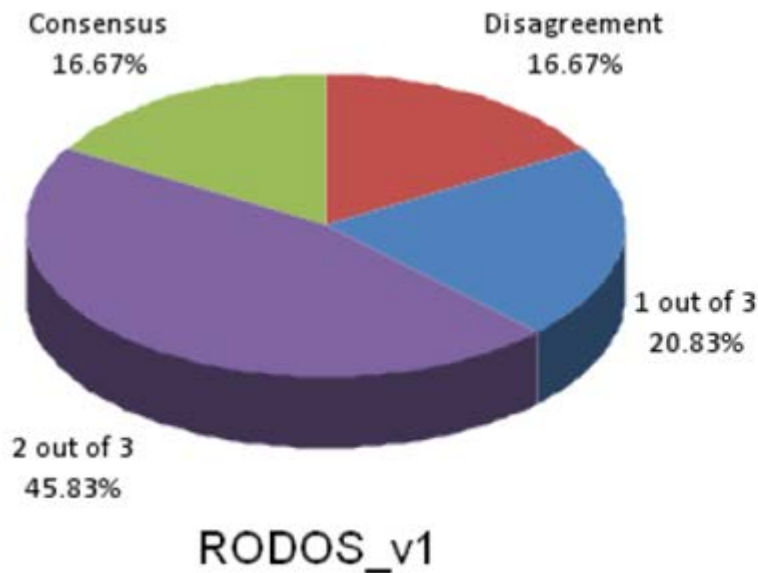
# Results: Taxonomy-Based Voter



- RODOS\_v2
  - No cases of disagreement
  - More cases of strict and majority consensus



# Results: Taxonomy Voter & Acceptance Test



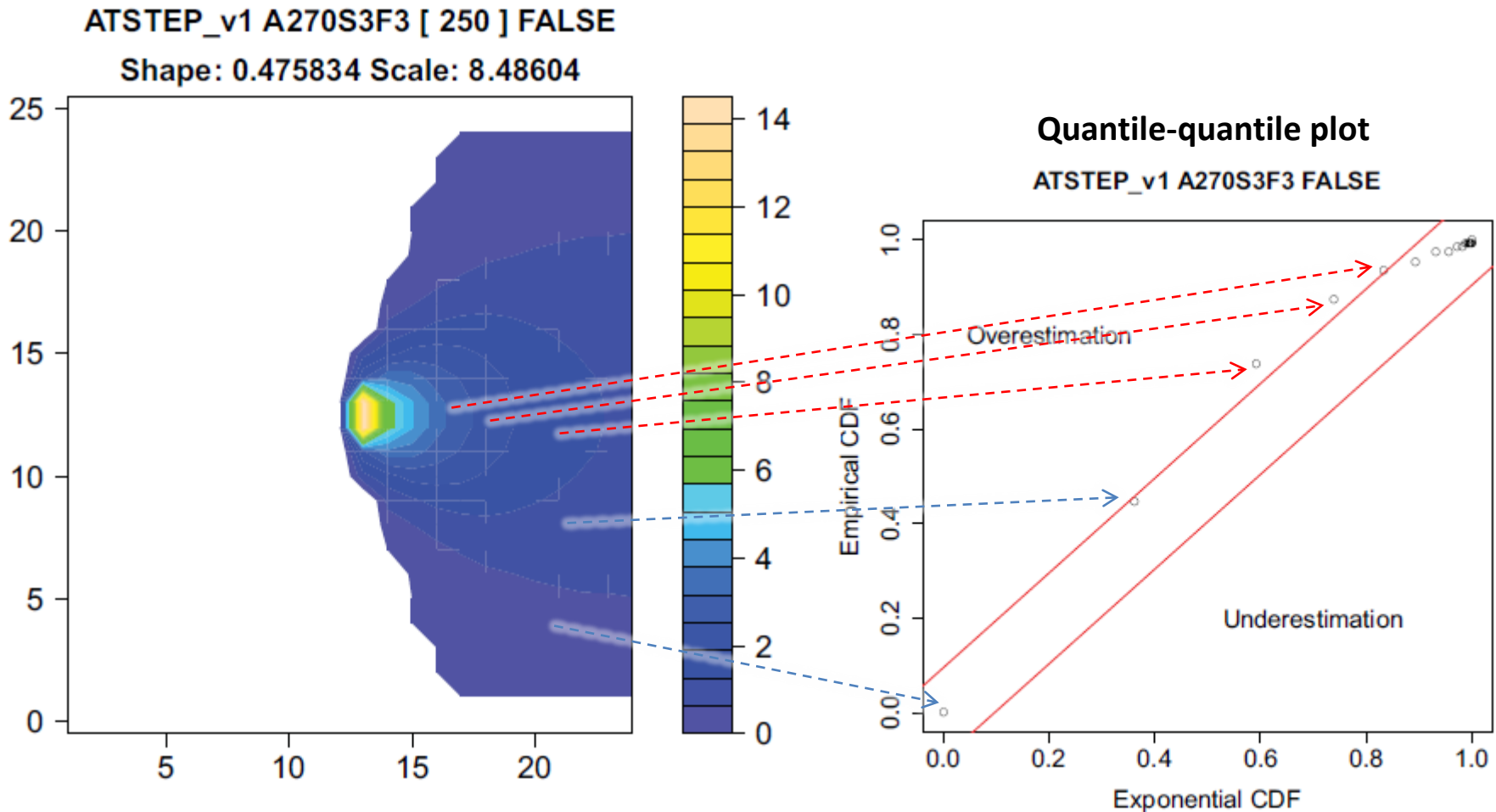
- RODOS\_v2
  - No cases of disagreement
  - Many more cases of consensus

## Conclusion

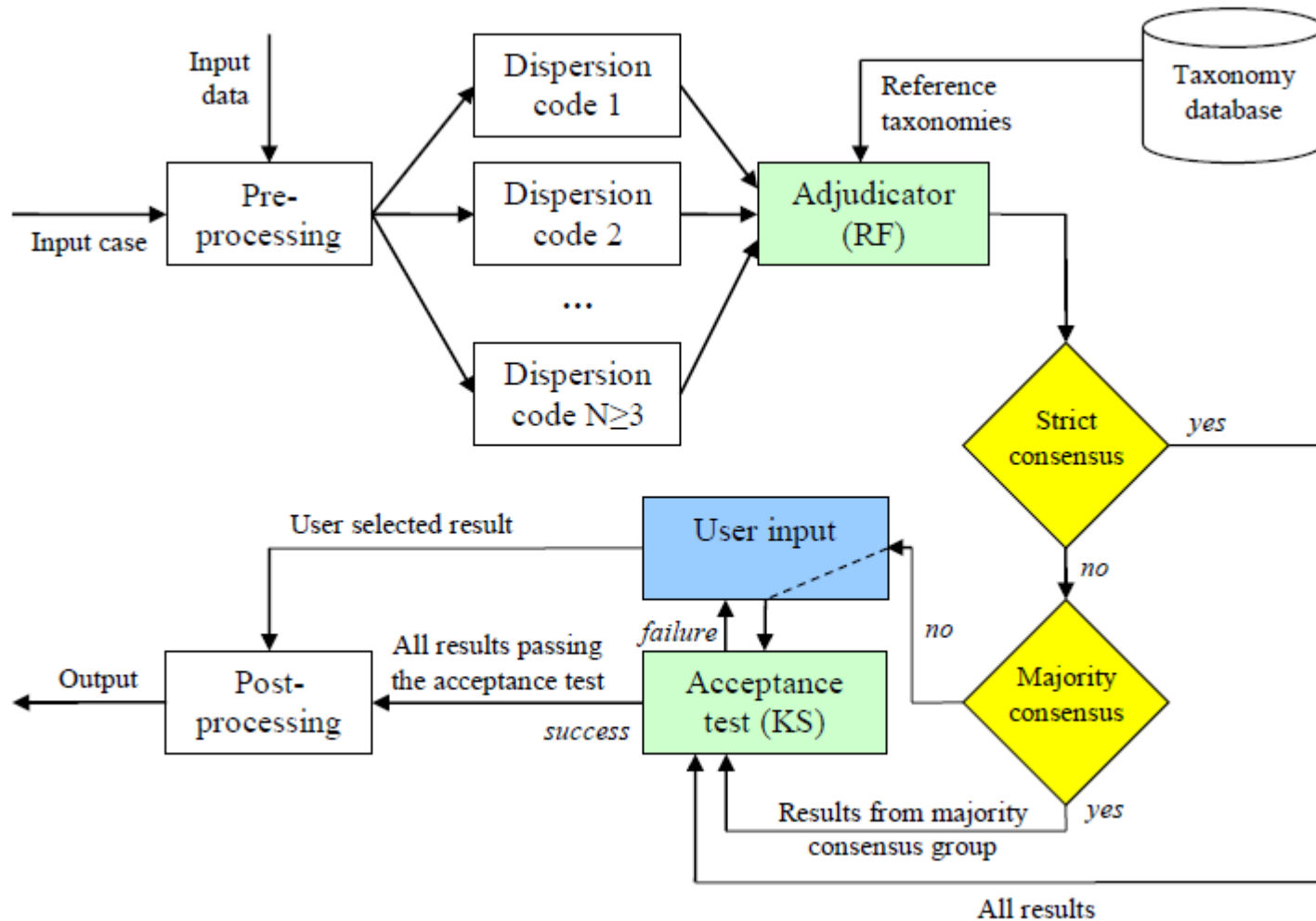
- The **acceptance test** and the **taxonomy-based voter** are sensitive to the improvements brought to the RODOS system
- Fully automated software metrics for the continuous verification of dispersion simulation codes
- Complementary to visual inspection and other means of verification
- Can be used for
  - Model/code inter-comparisons based on many input cases
  - Ensemble-based dispersion modelling systems
- Source code available

# Visualization of Kolmogorov-Smirnov Test Results

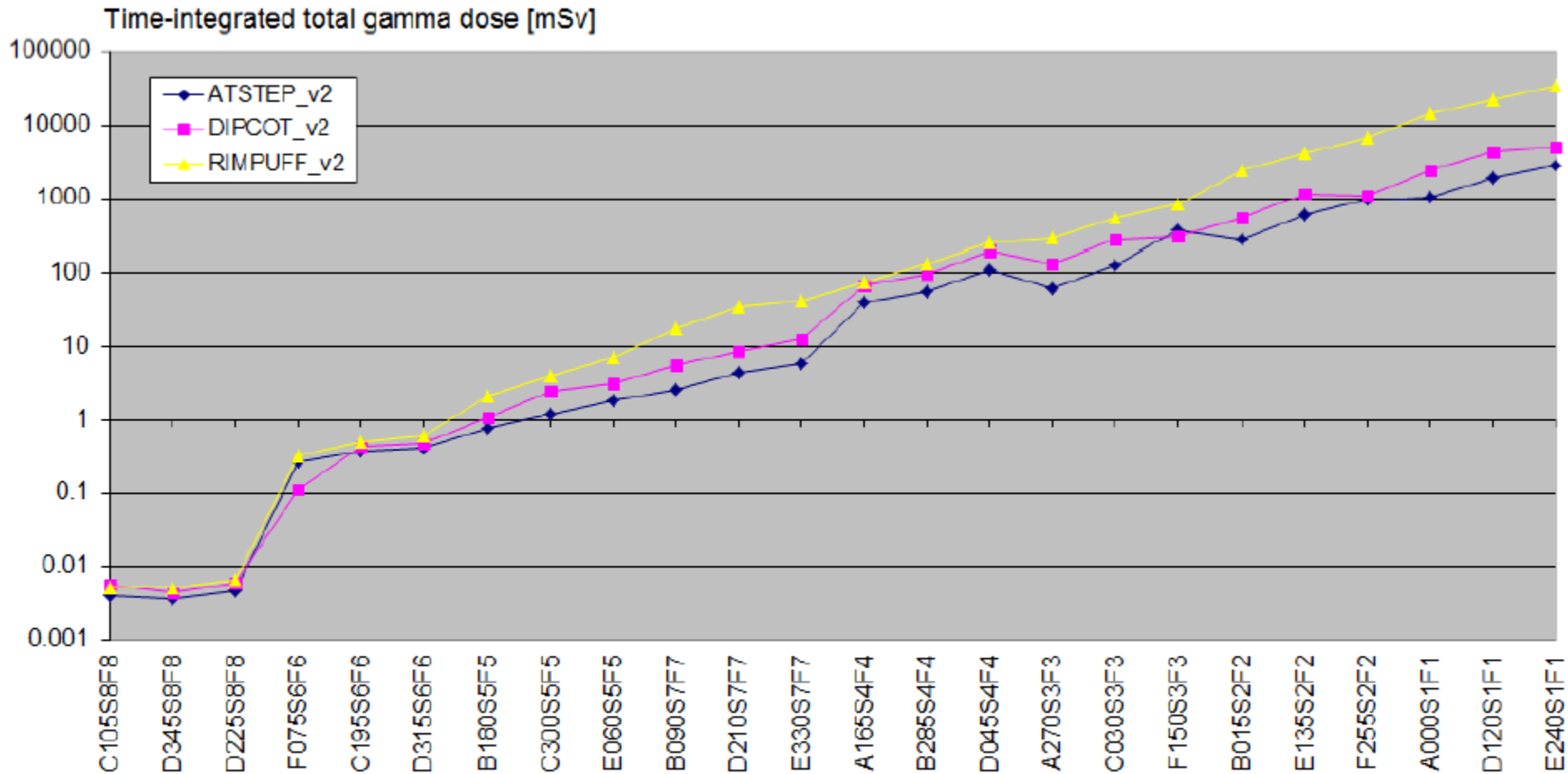
- Generated in *R* (statistical computing)



- Workflow for a dispersion forecasting system supporting functionally redundant simulation codes and continuous verification of results.



# Monotonicity of Time-Integrated Doses



**Figure 29:** The time-integrated gamma dose for all input cases as computed by ATSTEP, DIPCOT, and RIMPUFF (corresponding to RODOS\_v2). The values are summed up over the entire monitored area.