

# Reduction and Emulation of ADMS Urban

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## Introduction

- ADMS Urban is an air quality static model at urban scale.
- Input vector  $p \in \mathbb{R}^K$  : meteorological variables, background concentrations, hour of the day, Julian day.
- $p$  varies from one simulated hour to the next.
- High-dimensional output concentration vector  $y = \mathcal{M}(p)$ .

But a full-year simulation of  $\text{NO}_2$  concentrations over a city can take dozens of days of computation!

## Objective

Replace ADMS Urban with an emulator.

## Principle

- $y$  is first projected onto a reduced subspace.
- The relations between the projection coefficients and the input vector  $p$  are then emulated.

## Dimension reduction

- A reduced basis  $[\Psi_1 \dots \Psi_N]$  must represent the variability of the concentration field and is determined by Principal Component Analysis over a training period.
- In practice just few principal components are enough to provide a good approximation.

$$y \simeq \sum_{j=1}^N \alpha_j \Psi_j$$

where  $\alpha_j = y^T \Psi_j$  projection coefficient on  $j$ -th principal component.

## Case study

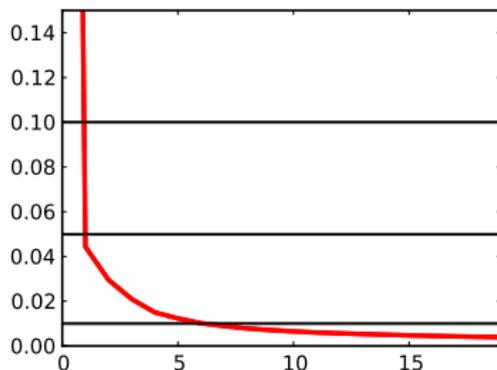
The application is the simulation of  $\text{NO}_2$  concentrations every 3 hours across the city Clermont-Ferrand (France) for the full year 2008.

**Input variables**  $p$  contains  $K = 10$  components.

- 5 meteorological input scalars from a meteorological station: wind speed, the wind direction, the temperature, the cloud coverage and the rain intensity.
- 3 background concentrations for  $\text{NO}_2$ ,  $\text{NO}_x$  and  $\text{O}_3$ .
- 2 emission variables: emissions vary according to the Julian day and the hour of the day (spatial distribution of the emissions and emissions factors are part of the model).

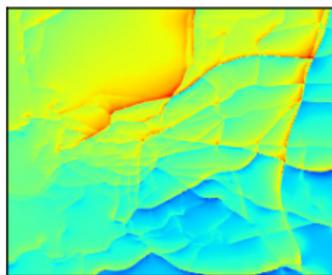
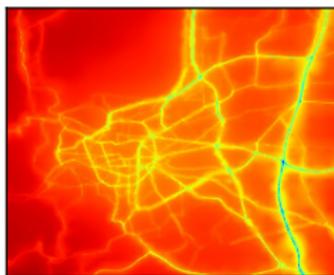
## Dimension reduction

- We applied the principal component analysis to the full year 2008.
- Unexplained variance over the full year against the size of the projection basis  $N$ :



99% of the total variance with only  $N = 8$  principal components.

$$y \simeq \sum_{j=1}^8 \alpha_j \Psi_j$$



$\Psi_1$  and  $\Psi_3$ : effects of mean emissions and wind from south.

## Scores

The simulation over the full year 2008 is compared to its projection on 8 principal components.

Mean $\mu\text{g m}^{-3}$	Bias $\mu\text{g m}^{-3}$	Corr. %	RMSE $\mu\text{g m}^{-3}$	Rel. RMSE %
23	0	99	2.37	10

## Emulation

Every component  $f_j(p) = \mathcal{M}(p)^T \Psi_j$  is replaced by a statistical emulator  $\hat{f}_j$  whose computational cost is negligible.

- $M$  training samples  $f_j(p^{(i)})$  by latin hypercube sampling.
- The emulator in  $p$  is made of two parts:

$$\hat{f}_j(p) = \underbrace{\sum_{k=1}^K \beta_{j,k} p_k}_{\text{Regression}} + \underbrace{\sum_{i=1}^M w_{j,i}(p, \dots, p^{(M)}) \left( f_j(p^{(i)}) - \sum_{k=1}^K \beta_{j,k} p_k^{(i)} \right)}_{\text{Interpolation of the residuals}}$$

- Interpolation of the residuals:
  - Interpolation with radial basis functions.
  - Mean of the closest neighbors.
  - Kriging (computationally intensive).

## Case study

The components  $\alpha_j = y^T \psi_j$  of the projection are emulated, and the emulator is applied over a full year.

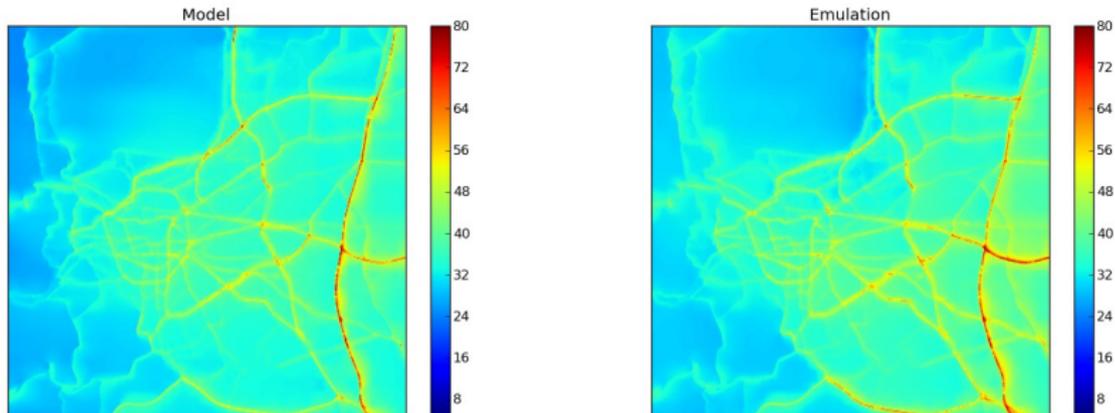
### Emulation

- $M = 2000$  samples to build the 8 emulators.
- Linear regression.
- Interpolation of residuals : radial basis function (Python module Scipy).

### Scores

	Bias $\mu\text{g m}^{-3}$	Corr. %	RMSE $\mu\text{g m}^{-3}$	Rel. RMSE %
Radial basis functions	-0.2	90	6.7	30

## Comparison of ADMS Urban and the RBF emulator



200 frames over the year 2008

## Demonstration of the RBF emulator

## Conclusion

- The dimension reduction needs a 6-month simulation.
- Building the complete emulator requires the equivalent of a 8-month simulation.
- Then the prediction for any  $p$  is essentially instantaneous!

## Perspectives

- Improve the interpolation part of the emulator, with error control: inverse distance weighting or even kriging.
- Generate an ensemble of simulations for uncertainty quantification (Monte Carlo simulation).
- Operational air quality forecast: Urban Air System by Numtech.
- Impact studies: focusing on yearly or monthly averages.
- All the new methods that were previously out of reach because of the computational cost of the model!

- $\hat{f}_j(p) = \sum_{k=1}^K \beta_{j,k} p_k + \sum_{i=1}^M w_{j,i}(p, \dots, p^{(M)}) \left( f_j(p^{(i)}) - \sum_{k=1}^K \beta_{j,k} p_k^{(i)} \right)$
- Let the residual be  $r_j(p) = f_j(p) - \sum_{k=1}^K \beta_{j,k} p_k$ , and the emulated residual be  $\hat{r}_j(p) = \hat{f}_j(p) - \sum_{k=1}^K \beta_{j,k} p_k$
- $\hat{r}_j(p) = \sum_{i=1}^M \alpha_{j,i} d(p, p^{(i)})$  where  $d$  is a distance, here  $d$  is a metric in  $K$  dimensions.
- We want to obtain the exact value at training points:  
 $\hat{r}_j(p^{(k)}) = r_j(p^{(k)}) = \sum_{i=1}^M \alpha_{j,i} d(p^{(k)}, p^{(i)})$
- We denote  $\Delta_j$  the matrix whose element  $(k, i)$  is  $d(p^{(k)}, p^{(i)})$ , and  $D_j(p)$  the vector whose  $i$ th component is  $d(p, p^{(i)})$
- We get:  $\alpha_j = \Delta_j^{-1} R_j$  if  $R_j = (r_j(p^{(1)}), \dots, r_j(p^{(M)}))^T$
- Note that  $\hat{r}_j(p) = \alpha_j^T D_j(p) = R_j^T \Delta_j^{-1} D_j(p) = D_j^T(p) \Delta_j^{-1} R_j$
- We therefore obtain:  $w_j(p) = D_j^T(p) \Delta_j^{-1}$ .